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# Pull-based supply chain allocation for multi-product in multi-echelon distribution system 

## by

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## A dissertation submitted to the graduate faculty in partial fulfillment of the requirements for the degree of DOCTOR OF PHILOSOPHY

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## TABLE OF CONTENTS

LIST OF FIGURES ..... vii
LIST OF TABLES ..... viii
ACKNOWLEDGMENTS ..... xiii
ABSTRACT ..... xiv
CHAPTER 1 INTRODUCTION ..... 1
1.1 Introduction ..... 1
1.2 Objectives of Research ..... 7
1.3 Tasks to Be Performed ..... 8
1.4 Research Assumptions ..... 9
1.5 Contributions of the Study ..... 10
1.6 Organization of the Research ..... 12
CHAPTER 2 SUPPLY CHAIN MANAGEMENT AND LITERATURE REVIEW ..... 13
2.1 Basics of Supply Chain Management ..... 13
2.1.1 Definition of Supply Chain Management ..... 13
2.1.2 Integration along the Supply Chain ..... 15
2.1.3 Natures of Supply Chain Management Problems ..... 16
2.1.4 Important Issues in Efficient Supply Chain Planning ..... 19
2.1.5 Push-based versus Pull-based Supply Chain ..... 20
2.1.5.1 Push-based Supply Chain System ..... 21
2.1.5.2 Pull-based Supply Chain System ..... 22
2.2 Literature Review ..... 23
2.2.1 Supply Chain Management, SCM ..... 24
2.2.2 Facility Location Problem for Distribution Planning ..... 26
2.2.3 Differences between the Present Study and the Earlier Studies ..... 28
CHAPTER 3 MODEL DEVELOPMENT FOR SUPPLY CHAIN LOCATION ..... 30
PROBLEM
3.1 Required Data for Model Development ..... 31
3.2 Model Characteristics ..... 31
3.2.1 Assumptions - Applicable to Both Models ..... 32
3.2.2 SCTFL Model ..... 32
3.2.3 MCTFL Model ..... 33
3.3 Total Systemwide Costs (TC) in Generalized Supply Chain ..... 33
Facility Location Problems
3.3.1 Production Cost $\left(P_{c}\right)$ ..... 34
3.3.2 Transportation Cost $\left(T_{c}\right)$ ..... 35
3.3.3 Inventory Carrying $\operatorname{Cost}\left(I_{c}\right)$ ..... 35
3.3.4 Warehousing Cost $\left(W_{c}\right)$ ..... 36
3.4 Mathematical Formulation and Notations ..... 36
3.5 Single-product Capacitated Two-echelon Facility Location Problem ..... 38(SCTFL)
3.5.1 Mixed Integer Linear Programming ..... 38
3.5.2 Solution Procedure for SCTFL ..... 40
3.5.2.1 Optimal Solution Properties ..... 43
3.5.2.2 Lagrangian Decomposition Heuristic Procedures (LD) ..... 44
3.5.2.3 Updating Multipliers, $\mu_{j}$ ..... 45
3.6 Multi-product Capacitated Two-echelon Facility Location Problem ..... 46 (MCTFL)
3.6.1 Mixed Interger Linear Programming ..... 46
3.6.2 Solution Procedure for MCTFL ..... 48
3.7 Solution Procedures for LP1 and LP2 ..... 49
3.7.1 Solving Bender's Subproblem ..... 52
3.7.1.1 Modified Vogel's Approximation Method for LP1 ..... 55
3.7.1.2 Modified Vogel's Approximation Method for LP2 ..... 59
3.7.1.3 Finding Dual Subproblem Solution from the Primal ..... 63
Subproblem Solution
3.7.2 Solving Bender's Master Optimal Problem, BMO ..... 70
3.8 Chapter Summary ..... 74
CHAPTER 4 MODEL DEVELOPMENT FOR A PULL-BASED SUPPLY ..... 76
SUPPLY CHAIN SYSTEM
4.1 General Introduction ..... 76
4.2 Generic Supply Chain Model ..... 76
4.3 General Solution Concept and Techniques ..... 80
4.4 Solution Methodology for A Pull-based Supply Chain in A Single ..... 85
Product Problem (PSCSP)
4.5 Solution Methodology for A Pull-based Supply Chain in Multi-product ..... 87
Problem (PSCMP)
4.6 Chapter Summary ..... 91
CHAPTER 5 COMPUTATIONAL PERFORMANCE ..... 93
5.1 Numerical Examples ..... 93
5.2 Comparison of Results for SCTFL versus Other Two Heuristic Methods ..... 95
5.3 Comparison of Results for MCTFL versus Other Three Heuristic Methods ..... 98
5.4 Comparison of Results for PSCSP versus Other Two Heuristic Methods ..... 104
5.5 Comparison of Results for PSCMP versus Other Three Heuristic Methods ..... 124
CHAPTER 6 SUMMARY AND CONCLUSION ..... 150
6.1 Summary of Results ..... 151
6.2 Conclusion ..... 153
6.3 Insights Gained ..... 155
6.4 Possible Extensions ..... 155
APPENDIX A EXAMPLE OF CUSTOMER ORDERS ..... 157
APPENDIX B EXAMPLE RESULTS OF SUPPLY CHAIN NETWORK ..... 167
APPENDIX C EXAMPLE RESULTS OF A PULL-BASED SUPPLY CHAIN ..... 172
DECISIONS FROM THIS STUDY
REFERENCES ..... 183
BIOGRAPHICAL SKETCH ..... 192

## LIST OF FIGURES

1.1 Channels of distribution for industrial goods ..... 5
1.2 Channels of distribution for consumer goods ..... 6
1.3 A two-echelon supply chain system consisting of three plants, ..... 7four warehouses, and six retailers
2.1 A push-based supply chain system ..... 22
2.2 A pull-based supply chain system ..... 23
3.1 The LD heuristic in each interation ..... 45
3.2 The MCTFL heuristic procedure ..... 49
4.1 Two echelon distribution network ..... 77
4.2 One echelon distribution network ..... 78
4.3 A pull-based heuristic procedure ..... 87
4.4 A heuristic for a pull-based supply chain of multi-product case ..... 90
5.1 MCTFL total costs of 10 testing problems ..... 103
5.2 Graph of result from Table 5.42 ..... 123
5.3 Graph of result from Table 5.84 ..... 149

## LIST OF TABLES

1.1 Examples of decision-making related to logistics planning in each level ..... 3
5.1 Results of SCTFL problems using the shortest distance method ..... 96
5.2 Results of SCTFL problems using lowest transportation cost method ..... 96
5.3 Results of SCTFL problems using SCTFL heuristic method ..... 97
5.4 Comparison of SCTFL problems using shortest distance, lowest transportation ..... 98 cost, and the SCTFL heuristic methods.
5.5 Results of MCTFL problems using the shortest distance method ..... 100
5.6 Results of MCTFL problems using the lowest transportation cost method ..... 100
5.7 Results of MCTFL problems using the single warehouse preference method ..... 101
5.8 Results of MCTFL problems using MCTFL heuristic method ..... 101
5.9 Comparison of MCTFL problems using shortest distance, lowest ..... 102 transportation cost, single warehouse preference, and the MCTFL heuristic method
5.10 Comparison of MCTFL problems among shortest distance, lowest ..... 102 transportation cost, and single warehouse preference methods
5.11 PSCSP results of test no. 1 using the shortest distance method ..... 106
5.12 PSCSP results of test no. 2 using the shortest distance method ..... 106
5.13 PSCSP results of test no. 3 using the shortest distance method ..... 107
5.14 PSCSP results of test no. 4 using the shortest distance method ..... 107
5.15 PSCSP results of test no. 5 using the shortest distance method ..... 108
5.16 PSCSP results of test no. 6 using the shortest distance method ..... 108
5.17 PSCSP results of test no. 7 using the shortest distance method ..... 109
5.18 PSCSP results of test no. 8 using the shortest distance method ..... 109
5.19 PSCSP results of test no. 9 using the shortest distance method ..... 110
5.20 PSCSP results of test no. 10 using the shortest distance method ..... 110
5.21 PSCSP results of test no. 1 using the lowest transportation cost method ..... 111
5.22 PSCSP results of test no. 2 using the lowest transportation cost method ..... 111
5.23 PSCSP results of test no. 3 using the lowest transportation cost method ..... 112
5.24 PSCSP results of test no. 4 using the lowest transportation cost method ..... 112
5.25 PSCSP results of test no. 5 using the lowest transportation cost method ..... 113
5.26 PSCSP results of test no. 6 using the lowest transportation cost method ..... 113
5.27 PSCSP results of test no. 7 using the lowest transportation cost method ..... 114
5.28 PSCSP results of test no. 8 using the lowest transportation cost method ..... 114
5.29 PSCSP results of test no. 9 using the lowest transportation cost method ..... 115
5.30 PSCSP results of test no. 10 using the lowest transportation cost method ..... 115
5.31 PSCSP results of test no. 1 using PSCSP heuristic method ..... 116
5.32 PSCSP results of test no. 2 using PSCSP heuristic method ..... 116
5.33 PSCSP results of test no. 3 using PSCSP heuristic method ..... 117
5.34 PSCSP results of test no. 4 using PSCSP heuristic method ..... 117
5.35 PSCSP results of test no. 5 using PSCSP heuristic method ..... 118
5.36 PSCSP results of test no. 6 using PSCSP heuristic method ..... 118
5.37 PSCSP results of test no. 7 using PSCSP heuristic method ..... 119
5.38 PSCSP results of test no. 8 using PSCSP heuristic method ..... 119
5.39 PSCSP results of test no. 9 using PSCSP heuristic method ..... 120
5.40 PSCSP results of test no. 10 using PSCSP heuristic method ..... 120
5.41 Comparison of the PSCPP weekly cumulative costs over 13 weeks ..... 121using shortest distance, lowest transportation cost, and PSCSP heuristic methods
5.42 The weekly cumulative costs of all three methods based on test no. 10 ..... 122
5.43 PSCMP results of test no. 1 using the shortest distance method ..... 126
5.44 PSCMP results of test no. 2 using the shortest distance method ..... 126
5.45 PSCMP results of test no. 3 using the shortest distance method ..... 127
5.46 PSCMP resuits of test no. 4 using the shortest distance method ..... 127
5.47 PSCMP results of test no. 5 using the shortest distance method ..... 128
5.48 PSCMP results of test no. 6 using the shortest distance method ..... 128
5.49 PSCMP results of test no. 7 using the shortest distance method ..... 129
5.50 PSCMP results of test no. 8 using the shortest distance method ..... 129
5.51 PSCMP results of test no. 9 using the shortest distance method ..... 130
5.52 PSCMP results of test no. 10 using the shortest distance method ..... 130
5.53 PSCMP results of test no. 1 using the lowest transportation cost method ..... 131
5.54 PSCMP results of test no. 2 using the lowest transportation cost method ..... 131
5.55 PSCMP results of test no. 3 using the lowest transportation cost method ..... 132
5.56 PSCMP results of test no. 4 using the lowest transportation cost method ..... 132
5.57 PSCMP results of test no. 5 using the lowest transportation cost method ..... 133
5.58 PSCMP results of test no. 6 using the lowest transportation cost method ..... 133
5.59 PSCMP results of test no. 7 using the lowest transportation cost method ..... 134
5.60 PSCMP results of test no. 8 using the lowest transportation cost method ..... 134
5.61 PSCMP results of test no. 9 using the lowest transportation cost method ..... 135
5.62 PSCMP results of test no. 10 using the lowest transportation cost method ..... 135
5.63 PSCMP results of test no. 1 using the single warehouse preference method ..... 136
5.64 PSCMP results of test no. 2 using the single warehouse preference method ..... 136
5.65 PSCMP results of test no. 3 using the single warehouse preference method ..... 137
5.66 PSCMP results of test no. 4 using the single warehouse preference method ..... 137
5.67 PSCMP results of test no. 5 using the single warehouse preference method ..... 138
5.68 PSCMP results of test no. 6 using the single warehouse preference method ..... 138
5.69 PSCMP results of test no. 7 using the single warehouse preference method ..... 139
5.70 PSCMP results of test no. 8 using the single warehouse preference method ..... 139
5.71 PSCMP results of test no. 9 using the single warehouse preference method ..... 140
5.72 PSCMP results of test no. 10 using the single warehouse preference method ..... 140
5.73 PSCMP results of test no. 1 using PSCMP heuristic method ..... 141
5.74 PSCMP results of test no. 2 using PSCMP heuristic method ..... 141
5.75 PSCMP results of test no. 3 using PSCMP heuristic method ..... 142
5.76 PSCMP results of test no. 4 using PSCMP heuristic method ..... 142
5.77 PSCMP results of test no. 5 using PSCMP heuristic method ..... 143
5.78 PSCMP results of test no. 6 using PSCMP heuristic method ..... 143
5.79 PSCMP results of test no. 7 using PSCMP heuristic method ..... 144
5.80 PSCMP results of test no. 8 using PSCMP heuristic method ..... 144
5.81 PSCMP results of test no. 9 using PSCMP heuristic method ..... 145
5.82 PSCMP results of test no. 10 using PSCMP heuristic method ..... 145
5.83 Comparison of the PSCMP weekly cumulative costs over 13 weeks using ..... 147shortest distance, lowest transportation cost, single warehouse preference,and PSCMP heuristic methods.
5.84 The weekly cumulative cost of all four methods based on test no. $10 \quad 147$

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#### Abstract

In today's highly competitive market environment, only companies with a highly efficient supply chain management, which integrates all decisions in various levels of planning and operations, can survive. These decisions must be coordinated and under the same goal, which is to minimize the total systemwide costs of the firm while products are manufactured and distributed to end-customers or retailers.

In this study, the focus is on a pull-based supply chain, customer demand driven, multiple products and multiple echelon distribution system consisting of $m$ manufacturing centers, $n$ distribution centers, and $p$ retailers or customers. The objectives of this study can be categorized into two parts. The first objective is to present a general framework of the design and configuration of the supply chain network at strategic and tactical planning levels in a single-product and multi-product multi-echelon supply chain systems. The problems deal with determining the appropriate number, location, and size of each manufacturing facility and distribution center/warehouse that should be used within the logistics network. The second objective of the research is to present a methodology for using a pull-based supply chain system both for a single-product system and multi-product system at the operational planning level. The problems deal with determining which products customers will receive from each available manufacturing facility and distribution center, what production quantities of the products should be manufactured by a particular manufacturing facility, and what quantities of each product and ways of shipment should be used from manufacturing facilities to distribution centers and to customers.


Based on the nature of these large-scale mixed integer programming problems, decomposition heuristic algorithms based on relationships between primal and dual decompositions are developed. The mathematical models and the heuristic algorithms are then demonstrated and evaluated on several sets of randomly generated problems. Although the heuristic algorithms do not guarantee optimum solutions, their results of the test problems suggest that the heuristics are effective in solving fairly large problems with reasonable computational time. Furthermore, they produce superior performances as compared to the other techniques that are tested.

## CHAPTER 1

## INTRODUCTION

### 1.1 Introduction

In this study we consider a problem faced by many companies that try to integrate decisions along the supply chain system in order to maintain acceptable service level while minimizing the fixed costs of operating manufacturing centers, distribution centers (DCs), inventory holding costs at the DCs, and transportation costs between plants and DCs, and DCs and customers.

In today's global markets, each company must effectively manage its supply chain to meet the heightened expectations of customers and the short life cycles of products. Only companies that have efficient communication and transportation technologies along with a highly efficient supply chain management can survive in today's highly competitive market environment. To deal with this threat, companies need to improve their systemwide management policies within their supply chain to increase both the quality and service level of their products, and at the same time, also try to cut their systemwide costs. Companies' supply chain management, which integrates all decisions in the various levels of operations, must be implemented, so that their products with lower per-unit production costs are manufactured and distributed to end-customers or retailers at the right time, at the right quantities, and to the right locations. Supply chain management often involves all of a firm's activities and needs to be defined at a firm's strategic, tactical, and operational planning levels. Although each planning level requires different perspective and time horizon, it is important for each company to come up with an integrated plan, which supports
and synchronizes all planning levels. Table 1.1 shows examples of decision making related to supply chain planning in each level according to Ballou (1999). The supply chain network usually consists of suppliers, manufacturers, warehouses or distribution centers, and retail outlets and sometime end customers, as well as raw materials, work-in-process inventory, and finished products that flow between the facilities.

All business interfaces within the supply chain must be considered as a whole since uncoordinated decisions could cause more investments and poor management that could lead to building up of inventory along the supply chain. Decisions on purchasing should not only be concemed with the low per unit costs for raw material, but also the production practices to achieve the lowest per-unit production costs. All decisions within business interfaces, or supply chain, must be made under the same goal, which is to minimize the total operating costs of the firm. Management should strive to minimize the total operating costs rather than the cost of each activity. Attempts to reduce the cost of individual activities may lead to increase in total cost. For example, consolidating finished goods inventory in a small number of distribution centers will reduce inventory carrying costs and warehousing costs but may lead to increase in freight expenses. On the other hand, savings associated with large volume purchases may increase inventory carrying cost. Therefore, reductions in one cost may result to increase in the costs of other activities. These uncoordinated decisions may end up leading to higher overall operating cost.

| Type of <br> Decision | Level of Decision |  |  |
| :--- | :--- | :--- | :--- |
| Location | Strategic | Tactical | Operational |
|  | Numbers of <br> facilities, sizes, and <br> locations. | Inventory <br> positioning | Routing, expediting <br> and dispatching |
| Transportation | Mode selection | Seasonal service <br> mix | Replenishment <br> quantities and <br> timing |
| Order <br> processing | Selecting and <br> designing order <br> entry system | Priority rules for <br> customer orders | Expediting orders |
| service | Setting standards | Setting <br> pretransaction, <br> transaction, and post <br> transaction <br> elements. | Providing the proper <br> levels of service to <br> meet customer <br> needs. |
| Warehousing | Layout, site <br> selection | Seasonal space <br> choices | Order filling |
| Purchasing | Policies | Contracting, vender <br> selection | Order releasing |

Table 1.1 Examples of decision-making related to logistics planning in each level. (Ballou, 1999)

Regardless of the product design, marketing, and advertising issues, basically supply chain management can be divided into four major decision areas: customer service standards, facility location, inventory policy or deployment, and transportation mode selection and routing. The first priority in supply chain management is to set a proper customer service level since the level of service has a direct impact on the design of logistics systems. High levels of service normally use decentralized inventories at several locations and the use of, sometime, more expensive forms of transportation. Low levels of service generally require the use of less expensive forms of transportation and allows for centralized inventories at few locations. It is known that high levels of service mean high logistics costs.

Selecting the best number, location, sizes of facilities and stocking points are the other key areas in supply chain management, on which a company would need to make
decisions. This selection process in literatures is called "Facility location problem". Generally facility location problem involves the determination of where to place the stocking points and the sourcing points in the logistics system. This also includes assigning market demand to each facility. Facility location problem includes all product movements and associated costs as they take place starting from plants all the way to end-customers or retailers. Finding the minimum assignment cost is the ultimate goal of this problem subject to monitoring the required service level.

The third key decision area in supply chain management is a company's inventory policy. A company needs to set an inventory policy, and this is usually either a push or a pull inventory policy. Push inventory refers to the produce-to-stock policy and pull inventory refers to the demand-driven policy. More details about push and pull inventory can be found in Chapter 4 of this manuscript. An effective inventory policy tries to reduce the number of stocking points throughout the supply chain. This will reduce the amount of inventory carried in the system, including total safety stocks. However, this reduced cost is a trade-off with higher transportation costs.

The last decision area in supply chain management is transport system selection and routing. Transportation selection and routing decision directly affects logistics decisions. The number, size and location of stocking points depend on the transportation policies of the company as much as on inventory policies. As the number of stocking points increases, fewer customers will be assigned to any one point and transportation costs will rise. The decisions basically relate to how to fill each customer's order from among the stocking points and which types of transportation modes must be used.

Other important and related issue in the supply chain is the distribution channel of a company. Distribution channels focus on the way the company structures its marketing function with customers. This marketing function depends usually on each company's marketing strategy, size, finance, and especially type of product. Channels of distribution affect the speed of delivery or delivery time, customer service, stocking points, and vitally the total logistics cost. For example a direct manufacturer-to-user channel usually gives management greater control over the performance of marketing functions, but distribution costs normally are higher. On the other hand, indirect channels have lower distribution costs, but the company marketing functions depend more on wholesalers or other external agencies. Figures 1.1 and 1.2 show examples of distribution channels both for consumer goods and industrial goods according to Lambert and Stock (1993).


Figure 1.1 Channels of distribution for industrial goods (Lambert and Stock, 1993).


Figure 1.2 Channels of distribution for consumer goods (Lambert and Stock, 1993).

It is obvious that finding the right solution for these integrated decisions of the supply chain is challenging. Recently, researchers and practitioners have been increasing the attention placed on the performance, design, and analysis of these issues. Within manufacturing and production research, the supply chain concept grew largely out of twostage multi-echelon inventory models, and it is important to note that considerable progress has been made in the design and analysis of two echelon system. More detail about this research area and its trend can be found in Beanmon (1998).

In this study a framework of two-echelon supply chain system with a single product and multi-products will be developed. A graphical illustration of the two-echelon supply chain system is as shown in Figure 1.3. The system consists of a set of multiple facilities of retailers or customers, warehouses or distribution centers, and production or manufacturing plants. In each echelon of the supply chain, all higher-level facilities can retrieve products from all lower-level facilities; such as at warehouses vs. retailers, all retailers can retrieve products from all warehouses.


Figure 1.3. A two-echelon supply chain system consisting of three plants, four warehouses, and six retailers.

### 1.2 Objectives of Research

The integration of decisions in a supply chain network is the general purpose of this research. The objectives of this research can be categorized into two parts. The first objective of the research is to present a general framework of the design and configuration of a supply chain network at strategic and tactical planning levels in a single-product and multiproduct multi-echelon supply chain systems. The problems deal with determining the appropriate number, location, and size of each manufacturing facility and distribution center/warehouse that should be used within the logistics network. This also includes determining which products will be produced by which manufacturing facilities and stored at which storage points. To solve this problem, two deterministic mathematical models are formulated: one for the single-product case and the other for the multi-product case. The objective for both models is the minimization of the total systemwide costs (which is
discussed in detail, in Chapter 3). A decomposition heuristic algorithm is then developed to solve the models more efficiently, especially when dealing with a large-size supply chain system. The solutions obtained from these models provide the distribution network configuration of the supply chain system for each scenario.

The second objective of the research is to present a procedure for using a pull-based supply chain system both for a single-product system and multi-product system. The problems deal with determining which products customers will receive from each available manufacturing facility and distribution center, what production quantities of the products should be manufactured by a particular manufacturing facility, and what quantities of each product and ways of shipment should be used from manufacturing facilities to distribution centers and to customers. Beyond these common distribution and allocation tasks, the decisions of replenishing product quantities and the timing of the replenishment are also considered in the pull-based supply chain model by using the reorder point concept. A heuristic procedure is then developed to solve this pull-based supply chain problem. The outcome obtained from this problem provides a solution at operational level for order filling and inventory replenishment for a company.

### 1.3 Tasks to Be Performed

The following tasks will be undertaken in this study to realize the research objectives:

1) Present a framework of the supply chain system and define the total systemwide costs, which consists of all costs starting from the raw material stage through product delivery to customers.
2) Develop a mixed integer linear programming model to represent the supply chain network configurations, which includes all decision constraints such as the maximum capacity for each stocking point, maximum production capacity for each manufacturing facility, and the volume of customer demand at each demand point.
3) Develop a heuristic algorithm to select the best supply chain network configuration, the production plans, inventory stocking points, and transportation and distribution strategies, that will minimize the total systemwide costs.
4) Develop a heuristic procedure to determine the optimal customers' order filling and inventory replenishment decisions when a pull-based supply chain is applied.
5) Implement the heuristic algorithms on a personal computer.
6) Evaluate the heuristic computational performance and the results obtained from the pull-based supply chain system.

### 1.4 Research Assumptions

In pursuing the proposed research, the following assumptions are made:

1) Any plant can manufacture any product and supply to any distribution center.
2) Any distribution center can supply products to any customers.
3) The location and capacity of each candidate plant and distribution site is known and fixed. The candidate points are discrete and finite.
4) Average demand (units per year) for each demand point is known and is used for the network configuration design problem.
5) Actual demand (units per order) for each customer is known and is used for a pull-based supply chain problem.
6) In a pull-based supply chain system, each distribution center makes use of a continuous review $\left(Q_{i}, r_{i}\right)$ policy, where $Q_{i}$ is an order quantity for product $i$ at each distribution center, and $r_{i}$ is a reorder point for product $i$ at each distribution center.
7) All distribution centers are resupplied only from the plants. That is, lateral supply among the facilities is not allowed. In practice, some lateral shipments do occur but on an informal basis so that we avoid to degrade the real system by not allowing lateral shipment to take place in our models.

### 1.5 Contributions of the Study

A framework of an integrated supply chain management system is presented so that all key decisions within the supply chain can be made toward the same goal, which is to minimize the total systemwide costs. By employing the supply chain model in this study, the fotlowing benefits can be derived:

1) The supply chain models developed can serve as tools for determining the number, size, and locations of all facilities within a supply chain. The models help to determine the whole logistics network and system configuration. This will give a measurable guideline for a firm's logistics planning both at the strategic and tactical levels. Especially, at the tactical levels, this will heip the firm to adjust its inventory positioning, set priority rules for customer orders, and enter into purchasing contracts and select suppliers. Expanding the production capacity or stocking points are also the result of this study.
2) By applying a puil-based system and using fast information flow to transfer information about customer demands, all suppliers, stocking points or distribution centers, and manufacturers can fill customer order, supply raw materials or products, and refill inventory in each logistics levels in an economical fashion. This will lead to a decrease in lead times, in inventories throughout the supply chain, and in the performance variability in the system. It is known that a pullbased system gives a significant reduction in system inventory and system costs when compared to a push system. The heuristic procedure in the pull-based supply chain system will help a firm to deal with its logistics strategy and planning at operational level.
3) Most papers on supply chain system dealt with a single echelon system, which did not link together the decisions of production planning, inventory control, distribution, and logistics. In this study, all key decisions within the supply chain can be made at the time of fulfilling customers' orders.
4) The computational time of the heuristic algorithm in this study is exceptionally fast. Moreover, the algorithm is designed to deal with large scale problems while providing promising solutions as well.
5) The decomposition methodology developed in this study can be used in any types of multi-stage allocation or assignment problems such as capacitated facility location problems (CFL), and generalized assignment problems (GA) with some adjustments.

### 1.6 Organization of the Research

For ease of presentation and understanding by a reader, the remainder of this thesis is organized into five additional chapters. Chapter 2 reviews previous research, which have been done in areas related to the study. Chapter 3 defines the total systemwide supply chain costs in a supply chain and presents the framework of the supply chain network configuration. Two mix integer linear programming models, one for a single-product and another for multi-product cases, and their solution methodologies are also described in the chapter. Chapter 4 describes the concept of a pull-based supply chain system. The heuristic procedure to fill customers' orders and replenishment inventory both for the single-product and the multi-products cases are presented in the chapter. Chapter 5 employs numerical examples to test and demonstrate the effectiveness of the solution methodologies developed in Chapter 3, and 4. Finally, Chapter 6 presents the summary of results, conclusion, insights gained and possible extensions to the work presented in this study.

## CHAPTER 2

## SUPPLY CHAIN MANAGEMENT AND LITERATURE REVIEW

In the past few years, interest in supply chain management has grown dramatically. This interest has forced many firms to adjust and analyze their supply chains. In most cases, however, this has been done based on experience and intuition; very few analytical models or design tools have been used in this process, Simchi-Levi et al.(2000). In this chapter, we summarize the basics of supply chain management, BSCM, and some relevant research and issues that we refer to throughout this study.

### 2.1. Basics of Supply Chain Management.

### 2.1.1. Definition of Supply Chain Management

Supply chain management or logistics management refers to the management of the flow of goods from points-of-origin to points-of-consumption. In the past, a variety of names have been used according to Lambert and Stock (1993):

Physical distribution
Distribution
Distribution engineering
Business logistics
Marketing logistics
Distribution logistics
Nowadays, supply chain management and logistics management seem to be the most widely accepted term. The Council of Logistics Management, one of the largest and most
prestigious groups of logistics professionals, provides the excellent definition of logistics management as following:
"Logistics management is the process of planning, implementing and controlling the efficient, cost effective flow and storage of raw material, in-process inventory, finished goods, and related information from point-of-origin to point-of-consumption for the purpose of conforming to customer requirements."

Another good, but similar, definition of supply chain management is defined by Simchi-levi et al. (2000) as following:
"Supply chain management is a set of approaches utilized to efficiently integrate suppliers, manufacturers, warehouse, and stores, so that merchandise is produced and distributed at the right quantities, to the right locations, and at the right time, in order to minimize systemwide costs while satisfying service."

Supply chain management or logistics management is a vital part of a firm's operation. Logistics is the third-largest source of cost of doing business for a typical firm after manufacturing and marketing. Efficient and effective management of the logistics function can have a substantial impact. Logistics cost is reduced, profitability is improved, and the level of customer service is increased. There are a number of key factors in supply chains, Arnold and Chapman (2000):

- A supply chain includes all activities and processes to supply a product or service to an end customer.
- Any number of companies can be linked in the supply chain.
- A customer can be a supplier to another customer so the total chain can have a number of supplier/customer relationships.
- While the distribution system can be direct from supplier to customer, it can contain a number of intermediaries (distributors) such as wholesalers, warehouses, and retailers.
- Product or services usually flow from supplier to customer and design and demand information usually flows from customer to supplier.


### 2.1.2. Integration along the Supply Chain

Basically, the integrated supply chain management concept refers to administering all supply chain activities as an integrated system. Integrating all distribution-related activities in the supply chain as mentioned in the previous section can reduce total operating costs of a company. Without this integrated approach, the costs to satisfy customer demand and expectations will be higher. A company must make a decision that coordinates all set of activities within the supply chain or business interfaces. The following are the list of critical business interfaces within the supply chain.

- Supplier-purchasing
- Purchasing-production
- Production-marketing
- Marketing-distribution
- Distribution-intermediary (wholesaler and/or retailer)
- Intermediary-customer/end-user

These business interfaces must be considered as a whole since uncoordinated decisions involving these activities could cause a build up of inventory along the supply chain. Now, the decisions of purchasing are not only concerning about the low per unit
costs for raw material, but also need to consider the production to achieve the lowest per-unit production costs. All decisions within the business interfaces must be made under the same goal, which is minimize the inventory holding costs and logistics costs or total operating costs of the firm. Management should strive to minimize the total operating costs rather than the cost of each activity. Attempts to reduce the cost of individual activities may lead to increased total costs. For example, consolidating finished goods inventory in a small number of distribution centers will reduce inventory carrying costs and warehousing costs but may lead to an increase in freight expense or a lower sales volume. On the other hand, savings associated with large volume purchases may increase the inventory carrying costs. So, reductions in one cost may lead to increase in the costs of other activities. Effective supply chain management can be accomplished only by viewing logistics as an integrated system, and also minimizing its total operating cost subject to the company's customer service objectives.

### 2.1.3. Natures of Supply Chain Management Problems

Generally supply chain management problems involve the decision on how products are to move through the supply and distribution channels, and at the operational level, this includes decision on how to fill a recently received customer order, how to respond to a temporary transportation rate reduction, and how to route the current customer orders. Each day the supply chain system operates to move the products smoothly and efficiently through the channel. Basically the planning in supply chain management can be divided into four major decision areas: customer service standards, distribution network configuration, inventory policy or deployment, and transportation system selection and routing.

Customer service standards: the design of supply chain system greatly affects the level of customer service. Conversely, the level of customer service to be provided definitely impacts the design of supply chain systems. High levels of service normally use decentralized inventories at several locations and the use of, sometime, more expensive forms of transportations. Low levels of service generally require the use of less expensive forms of transportations and allow centralized inventories at few locations. It is known that high levels of service equates to high logistics costs. So, the first priority in supply chain planning must be the proper setting of customer service levels. Ballou (1999) suggests that effective supply chain planning should start with a survey of customer service needs and desires.

Distribution network configuration: distribution network decision involves how to place the stocking points and the sourcing points in the supply chain system. This also includes the number, location, and size of the facilities and assigning market demands to each facility. Generally distribution network problem includes all product movements and associated costs starting from plants/suppliers all the way to end customers. Finding the minimum assignment cost is the ultimate goal of distribution network planning. The following are the key questions in distribution network problem:

- What are the best number, location, and size of stocking points?
- Which plants/suppliers should serve which stocking points/facilities?
- Which products should be shipped directly from plants/suppliers to customers and which should be transshipped through the warehousing system?

Inventory policy: in general two strategies, push inventory and pull inventory, are involved in managing inventory throughout a supply chain. The push inventory strategy
refers to a make-to-stock policy while a puil inventory policy refers to a demand-drive policy. More details on the push and pull inventory policies will be presented again in a later section. An effective inventory policy tries to reduce the number of stocking points throughout the supply chain system. This will reduce the amount of inventory carried in the system including the safety stocks. However, the cost reduction associated with inventory consolidation is in trade-off with higher transportation costs. With fewer stocking points, smaller outbound shipment sizes with higher shipping charges must be weighed against larger shipment sizes of inbound goods that travel through longer distances to the marketplace. Therefore, the distribution network decision must be sensitive to the inventory deployment and control policies used. This indicates that inventory policy directly affects the distribution network decision and the whole supply chain planning. The following are common questions related to inventory policy:

- What turnover ratio should be maintained?
- Which products should be maintained at which stocking points?
- What level of product availability should be maintained in inventory?
- Which method of inventory control is best?
- Should push or pull inventory strategies be used?

Transport selection and routing: transportation selection and routing decisions directly affect the supply chain decisions. The number, size and location of stocking points depend on the transportation policies of the company as much as inventory policies. As the number of stocking points increases, fewer customers will be assigned to any one point, the mode of transportation may change and this will affect the transportation cost.. The following are questions related to the transportation system selection and routing:

- Which customers should be served out of which stocking points?
- Which transportation types, truckload (TL) or less than truckload (LTL), should be assigned to which customers?
- Which modes of transportation, Rail, Truck, Air, Water, or Pipeline, should be used?


### 2.1.4. Important Issues in Efficient Supply Chain Planning

Cost trade-offs: supply chain planning needs to balance all conflicting costs such as transportation costs versus inventory costs, production costs versus distribution costs, and ultimately customer service costs versus all supply chain costs. All issues in the supply chain must be considered as a whole to avoid any suboptimal plans. Both facility location and distribution issues must be addressed at the same time, since output of facilities location decision is the input to the distribution system and are economically related to one another.

Consolidation: consolidation happens when small shipments are consolidated to form a large shipment to gain the economies of scale. For example, two or more customer orders might be combined with other customer orders received at other time periods to form a large shipment if possible. Consolidation strategy will lower average per-unit shipping costs. This also avoids shipping small quantities of items over long distances at high perunit transport rate. In general, the concept of consolidation will be useful when the quantities shipped are small.

Postponement: the key idea of postponement is "to ship as much as you can as far as you can before committing to the end product." The final product processing and distribution are delayed until a customer order is received. This is done to avoid increasing
total inventory level throughout the company logistics network and the possibility of obsolete stocks. Postponement can be classified into five types; Labeling, Packaging, Assembly, Manufacturing, and Time. For more details on these issues, the reader is referred to Zinn and Bowersox (1988).

Mixed strategy: a mixed strategy allows an optimal strategy to be established for separate product groups. Usually mixed strategy leads to lower costs than a single or global strategy. In general, single strategies can benefit from economies of scales and administrative simplicity, however they ineffectively perform when the product groups vary in terms of cube, weight, order size, sales volume, and customer service requirements. Examples of a mixed strategy include using of some public warehousing along with privately owned space, shipping product directly from the plants along with from the warehouses, and filling customer order from a single warehouse along with instances of shipping from multiple warehouses for some products.

### 2.1.5. Push-based versus Pull-based Supply Chain

Supply chain or logistics systems are normally categorized as push-based or pullbased systems. In a push-based supply chain system, long-term forecasts are used to determine a firm's production. On the other hand, in a pull-based supply chain system, production is demand driven, and therefore is directly related to actual customer demands instead of a forecast. With actual demands, a firm can decrease inventory both at the retail and the manufacturing levels, and also decrease the variability in the system due to lead-time reduction.

A significant reduction in system inventory level and costs make a pull-based system more superior to a push-based system. The trend today is toward pull-based system even though it is more difficult to implement than a push-based system. The succeeding sections summarize key concepts of these two supply chain systems.

### 2.1.5.1. Push-based Supply Chain System

In a push-based supply chain system, production decisions are based on long-term forecasts. Orders from the retailer's warehouses are used to forecast customer demand. This system is appropriate where production or purchase quantities exceed the short-term requirements of the inventories. However, a firm may have the problem of overstocking or excess inventory. The excess inventory could become obsolete, damaged, or nonfunctional because of age. High inventory leads to high inventory cost. A push-based system also produces larger and more variable production batches and this can impact the customer service levels, since the system has the inability to meet changing demand patterns. Moreover, a push-based supply chain increases transportation costs, heightens inventory levels and heightens manufacturing costs, due to inability to meet or react to changing market conditions. Figure 2.1 shows a push-based system.


Figure 2.1 A push-based supply chain system.

### 2.1.5.2 Pull-based Supply Chain System

In pull-based supply chain system, actual customer demands rather than forecast are used in driving production or orders. In a pull-based system, the supply chain uses fast information flow to transfer information about customer demand to all stocking points and manufacturing facilities. This leads to a decrease in lead times, a decrease in inventories throughout the supply chain, and a decreasing in variability in the system. Pull-based system gives a significant reduction in system inventory and system costs. However, it is often difficult to implement when lead times are long. Furthermore, it is more difficult to take advantage of economies of scale in manufacturing and transportation since systems are not planned far ahead in time. To successfully apply a pull-based system, it is important to determine the procurement costs and lead time effects against inventory carrying costs. Since demand and lead time sometimes cannot be known with certainty, a firm must plan for the situation where not enough stock may be on hand to fill customer requests. In addition to the regular stock that is maintained for the purpose of meeting average demand and average lead time, an increment of inventory, safety stock, is added. Currently, there are two methods for controlling inventory in a pull-based system; 1) the reorder point method
and 2) the period review method. Some firms also use a combination of these two. In this study, the reorder point method is used in the models developed. For more information about the reorder point method and inventory control, consult Ballou (1999). Figure 2.2 shows a pull-based supply chain system.


Figure2.2 A pull-based supply chain system

### 2.2. Literature Review

This section consists of a brief literature review of two streams of research that are associated with this study. The first stream of research concentrates on issues related to optimizing supply chain management. The second stream of research examines the issues related to determining the number and location of DCs in order to minimize the costs related to transportation and operating the DCs. The most fundamental form of this problem is known as the warehouse location problem and the location allocation problem. The nature of the problem usually focuses on solving a linear integer programming problem.

### 2.2.1 Supply Chain Management (SCM)

As mentioned above, a supply chain is an integrated manufacturing process wherein raw materials are converted into final products, then delivered to customers. Beamon (1998) classified SCM research into four categories: (1) deterministic analytical models, (2) stochastic analytical models, (3) economic models, and (4) simulation models. Regarding the focus of this study, literature review of SCM is limited to deterministic analytical problem since it is the branch most relevant here.

Cohen and Lee (1988) presented a model framework for integrated decisions throughout the supply chain. A heuristic optimization procedure was used to analyze inventories along the supply chain. They applied the heuristic to a problem that consisted of two finished products, three raw materials, one plant, two production lines within the plant, and three distribution centers. The distribution review period was one day and the production planning period consisted of 20 days.

Cohen and Moon (1990) proposed a constrained optimization model, called PILOT, to analyze the supply chain cost, and considered the additional problem of determining which manufacturing facilities and distribution centers should be opened. More specifically, Cohen and Moon considered a supply chain consisting of suppliers, manufacturing facilities, and distribution centers, and retailers. This system produced final products and intermediate products, using various types of raw materials. The objective function of the PILOT model was a cost function, consisting of fixed and variable production and transportation costs, subject to supply, capacity, assignment, demand, and raw material requirement constraints. Based on the results of their example, the authors concluded that there were a number of
factors that might dominate supply chain costs under a variety of situations, and that transportation costs played a significant role in the overall costs of supply chain operations.

Cohen et al. (1990) developed an extensive multi-echeion logistics and inventory management system, called Optimizer, to provide customers with prompt and reliable service from IBM's National Service Division. The implementation of Optimizer had made it possible to make strategic changes to the configuration and control of the IBM parts distribution network. With Optimizer, IBM could simultaneously reduce inventory investment and operating costs and improve service levels.

Arntzen et al. (1995) developed a mixed integer programming model, called global supply chain model, (GSCM) that that incorporates multiple facilities, stages (echelons), time periods, and transportation modes. More specifically, the GSCM minimized a mixed function of: (1) activity days and (2) total (fixed and variable) cost of production, inventory, material handling, overhead, and transportation costs. The model outputs included (1) the number and location of distribution centers, (2) the customer-distribution center assignment, (3) the number of echelons (amount of vertical integration), and (4) the product-plant assignment.

Voudouris (1996) developed a mathematical model designed to improve efficiency and responsiveness in a supply chain. The model maximized system flexibility, as measured by the time-based sum of instantaneous differences between the capacities and utilizations of two types of resources: inventory resources and activity resources. Inventory resources are resources directly associated with the amount of inventory held; activity resources, then, are resources that are required to maintain material flow. The models generated as output: (1) a
production, shipping, and delivery schedule for each product and (2) target inventory levels for each product.

Camm et al. (1997) developed an integer programming model, based on an uncapacitated facility location formulation, for Procter and Gamble Company. The purposes of the model were to: (1) determine the location of distribution centers (DCs) and (2) assign those selected DCs to customer zones. The objective function of the model minimized the total cost of the DC location selection and the DC -customer assignment, subject to constraints governing DC-customer assignments and the maximum number of DCs allowed.

Gachon and Lariviere (1999) examined how the choice of mechanism impacts retailer actions and supply chain performance. They analyzed turn-and-earn allocation, a method commonly used in the automobile industry. The scheme presented allocations on past sales and thus enabled retailers to influence their future allocations. They found that turn-andearn induced the retailers to increase theirs sales when demand was low, and the impact on the supply chain depended on how restrictive the capacity was.

### 2.2.2 Facility Location Problem for Distribution Planning

The distribution/locations family of problems covers formulations, which range in complexity from simple single-product linear deterministic models to multi-product nonlinear stochastic versions. Solution approaches include heuristics, optimizers, simulators, and some innovative hybrid procedures, which embody more than one of these (Aikens, 1985). The purpose of this section is to review some of the significant work, which are related and fundamental to this dissertation. The focus will be on a mathematical model
with specific reference to the use of heuristics or optimizers to extract solutions.
Distribution/location can be classified according to:

1) Whether the distribution network is capacitated or uncapacitated.
2) The number of warehouse echeions, or levels.
3) The number of commodities (single or multiple).
4) Whether the underlying cost structure is linear or nonlinear.
5) Whether the planning horizon is static or dynamic.
6) Whether the pattern of demand is deterministic or stochastic.
7) The ability to accommodate side constraints.

In 1977, Kaufman et al. proposed an algorithm, which solved a two-level distribution system using branch and bound. The algorithm was used to solve a small and simple uncapacitated multi-echelon facility location problem. Triple subscripting and the double set of binary variables were used in their model. A limitation of their model is the requirement that a warehouse must be located wherever a plant is located.

Warszawski (1973) was one of the pioneers to address multi-product problem. Warszawski examined both a branch and bound procedure and a heuristic for solving multiproduct uncapacitated facility location model. However, no computational results were provided for the branch and bound algorithm due to excessive computation time. In 1978, Erlenkotter developed two dual-based algorithms for solving the same problem based on a linear programming dual formation. A simple ascent and adjustment procedure was used to produce optimal dual solutions. The author found that the dual-based algorithm was superior to other existing methods at that time.

Nauss (1978) was one of the first to consider the capacitated location problem. Nauss proposed a branch and bound algorithm along with the use of Lagrangian relaxation, and tighter lower bounds. The relaxation was solved efficiently by decomposition method. This resulted in fewer branches.

The focus on the multi-product capacitated single-echelon facility location problem started in 1974 by Geoffrion and Graves. In the Geoffrion and Graves model, sole-sourcing of customers was mandatory, and transportation costs were determined by the total plant-tocustomer route. More amenable model of practical application was developed by Geoffrion, Graves and Lee in 1978. Their work appeared to represent the state-of-the-art for multiproduct capacitated location problems. A solution technique based on decomposition was developed, and successfully applied to a real problem.

### 2.2.3 Differences between the Present Study and the Earlier Studies

The work presented in this study differs in one form or the other from the studies reviewed above in the following aspects:

- The majority of work on supply chain management focused on a push-based supply chain system or make-to-stock principle but in this study the focus is on a pull-based supply chain system or make-to-order/make-to-assembly principle.
- In model formulations, a sole sourcing of customers was mandatory. In this study, the models are capable of formulating problems of a multiple sourcing of customers.
- The majority of work on supply chain management was not flexible and only focused on logistics planning in strategic and/or tactical levels like inventory
positioning and numbers of facilities, sizes, and locations. In this study, the models present all logistics planning decisions including in operational planning level. The models can be effectively used to fill customer order, replenish inventories, and generate production orders throughout the supply chain network.
- The model formulations were either single-product multi-echelon or multiproduct single-echelon problem. In this study, the formulations cover multiproduct multi-echeion problem.
- Problems of practical size also presented a problem for all the solution methodology. In this study, the heuristic is formulated specifically for large and small size problems.


## CHAPTER 3

## MODEL DEVELOPMENT FOR SUPPLY CHAIN LOCATION PROBLEM

As stated earlier, the objective of the present study is to develop a procedure for integrating decisions along the supply chain to minimize the total systemwide costs. In this chapter, the framework for the supply chain management system for a single-product and multi-product supply chain management problems at the strategic and tactical planning levels are addressed. At these levels, a company usually focuses on selecting a set of operating facilities within the supply chain. Closing, opening, or expanding production and storage facilities are also the decisions that a company makes at these levels. These types of decision-making have been recognized by researchers and practitioners for decades as "Facility Location Problem". Excellent references and surveys in facility location problem can be found in Aikens (1985) and Drezner (1995). However, a few researchers have focused on multi-product and multi-echelon location problem that link together all related costs within a supply chain (Beamon, 1998). The majority of these previous works mainly focused on either the uncapacitated or capacitated single echelon location problem and did not integrate other decisions in their models. The models generally emphasize either the production or the distribution component but not both components simultaneously. In this chapter, the integrated decision models of the single-product capacitated two-echelon facility location (SCTFL) and the multi-product capacitated two-echelon facility location (MCTFL) problems are presented. Firstly all required data for model development, model characteristic, and the total system-wide costs within a supply chain network are defined.

Next, two mixed integer linear programming problems, SCTFL and MCTFL, are developed and described. Finally, solution procedures and numerical examples of the problems are presented.

### 3.1 Required Data for Model Development

The data necessary for the development of both the SCTFL and MCTFL models are as followings:

- Average customer order for each product per year.
- A set of candidate warehouses or distribution centers and their maximum storage capacities.
- A set of candidate production plants and their maximum production capacities.
- An average per unit transportation cost per ton-miles between customer locations and distribution centers.
- An average per unit transportation cost per ton-miles between distribution centers and production plants.
- Fixed and variable operation costs when using a particular distribution center or production plant.


### 3.2 Model Characteristics

The objective of the models for both the single-product and the multi-product twoechelon problems is to determine a set of facility locations, which will minimize total system-wide cost. Two different models representing the single-product and multi-product
two-echelon facility location problems are considered. These models are briefly stated below. Details on each model are provided in sections 3.5 and 3.6 respectively.

### 3.2.1 Assumptions-Applicable to Both Models

The following assumptions are made in developing the two models:

- Any plants can manufacture any products and supply to any distribution centers.
- Any distribution center can supply finish products to any customer locations.
- The location and capacity of each production plant and distribution center are known and fixed.
- Average demand (units per year) for each customer demand point or location is known.
- All distribution centers are resupplied only from the plants. That is, lateral supply among the facilities is not allowed.
- All transportation costs, facility establishment costs, and other related costs are known.


### 3.2.2 SCTFL Model

A single-product two-echelon facility location (SCTFL) problem consists of a set of plants, distribution centers, and customer locations. In this problem, there is only one product in the supply chain system. The problem exists when a company has a policy to market and manage its product line individually or has only one product line. For example, a computer manufacturing company may divide its product line into printer, computer CPU, and scanner. The company can treat and organize these products individually starting from
production and inventory control to product distribution. In this aspect, SCTFL may be used for each product line to determine the best supply chain network configuration, which consists of a set of production plants and stocking point locations and capacities, and primary distribution channel to deliver finish products to the end-customers. This usually happens at the company's strategic and tactical planning levels.

### 3.2.3 MCTFL Model

Multi-product two-echelon facility location model (MCTFL) represents the supply chain location problem with more than one product line. In this case, there are several product lines, which each production plant manufactures and each distribution center responds to. A company markets and distributes these different products through the same distribution channel or distribution logistics. Each product can be stored at any warehouse or produced at any production facility. Each customer's demand may consists of one or multiple products. Example of this kind of demands exists in most consumer product cases when a retail store such as Kmart, Target, or Walmart orders several goods from a single manufacturer. MCTFL is, then, used to determine the multi-product supply chain configuration network.

### 3.3 Total Systemwide Costs (TC) in Generalized Supply Chain Network

To model the supply chain problem in this study, first, the total supply chain cost is addressed and broken down into four major categories: 1) production cost, 2) transportation cost, 3) Inventory carrying cost, and 4) warehousing cost. These costs reflect costs of acquiring raw materials, converting raw materials into specified final products, storing the
final products, and delivering the final products at desired points. The following is the total systemwide cost function.

$$
T C=P_{C}+T_{C}+I_{C}+W_{C}
$$

where, $T C=$ total systemwide cost,
$P_{C} \quad=$ Production cost,
$T_{C}=$ Transportation cost,
IC = Inventory carrying cost,
$W_{C} \quad=$ Warehousing cost.

### 3.3.1 Production Cost (Pd

$$
P_{C}=f_{c}+v_{c}
$$

Fixed costs (f): general administrative expense, taxes and insurance, rent, building and equipment depreciation, utilities, and other costs, that is invariant with the production volume.

Variable costs ( $\nu_{c}$ ): variable costs vary in proportion to quantity of output. These costs are usually for direct material and direct labor cost.

### 3.3.2 Transportation Cost ( $T_{C}$ )

$$
\begin{gathered}
T_{C}=i_{c}+o_{c} \\
\text { Or, } \\
T_{C}=i_{c}+t_{m d}+t_{d c}
\end{gathered}
$$

Inbound transportation costs (id): the costs of obtaining raw material or costs related to shipping between suppliers and the firm, sometime called "Material procurement costs".

Oulbound transportation costs (od): costs associated with the shipping charges between the firm and customers. These costs may vary by customer locations and by the firm's channels of distribution. Cost associated with shipping charges between manufacturing sites and distribution centers is denoted by $\boldsymbol{t}_{\boldsymbol{m} d}$ and between DCs and customers is denoted by $t_{d c}$.

### 3.3.3 Inventory Carrying Cost (Id)

$$
I_{C}=s_{c}+t_{c}
$$

Storage space costs ( $s_{d}$ ): all expenses associated with the quantity or the level of inventory stored. If the space is privately owned or contracted, space costs appear as fixed costs. When the space belongs to a public warehouse, the charges are based on the amount of products moved into and out of the warehouse and the amount of inventory held in storage. Rented or leased warehouse space is normally contracted for a specified period of time. The amount of space rented is based on the maximum storage requirements during the period covered by the contract.

Throughput cost ( $t_{d}$ : this cost is related to selling the product in a given market by moving it in and out of warehouse.

### 3.3.4 Warehousing Cost (Wd)

Warehousing fixed cost (Wc): this cost is primarily fixed and is related to supervision or associated management costs to maintain or operate the warehouses.

### 3.4 Mathematical Formulation and Notations

To be able to investigate and formulate the mathematical model for the supply chain problem, the total systemwide cost as expressed in the previous section is simplified further as following:

$$
T C=C_{1}+C_{2}+C_{3}+C_{4}+C_{5}+C_{6}
$$

Where,
$C_{1}=$ Fixed production cost ( $\left.\boldsymbol{f}_{\mathcal{L}}\right)$
$C_{2}=$ Outbound transportation cost from plants to warehouses and variable production cost per unit $\left(v_{c}+t_{m d}\right)$.
$C_{3}=$ Outbound per unit transportation cost from warehouses to customers ( $t_{d c}$ ).
$C_{4}=$ Warehousing costs and storage space fixed costs $\left(W c+s_{c}\right)$.
$C_{5}=$ Inventory throughput cost per unit cost $\left(t_{d}\right)$.
$C_{6}=$ Material procurement cost per unit cost (id).
Now, to model the supply chain network configuration problem, the idea of using separate transportation variables for plant-to-warehouse and warehouse-to-customer shipments, which are less complex, are employed. The approach is different from the wellknown, but more complicated, work by Geoffrion and Craves (1974). In their model, triple subscribed variables were used in order to avoid losing the origin of a product once it arrives at a DC or warehouse. This seemed useful when there were no data tracking tools and

Internet technology. With current technology, there is no need to incorporate the origin of a product into the mathematical model. Part tracking information, nowadays, can be captured by bar coding system throughout the supply chain and always stored in a company database.

The use of separate variables not only brings us a new look at the problem, but also seems less complex, more flexible, and essentially easier to approach. It is also easy to incorporate with some supply chain strategies like pull-based supply chain system, order consolidations, postponement, or mixed strategy, which are limited when the triple subscribe variables are used. Beside these issues, by using separate variables, the problem, now, can be decomposed into a set of smaller and easier-to-solve subproblems. The mathematical formulation of the problem throughout this chapter uses the following notation.
$p$ index for commodities,
$i$ index for plants,
$j$ index for possible distribution center (DC) sites, or warehouse locations,
$k$ index for customers or retailers,
$P \quad$ a set of commodities,
I a set of plants,
$J \quad$ a set of warehouses or DC,
K a set of potential customers,
$a_{i j}^{p} \quad$ the unit transportation cost of product $p$ from plant $i$ to warehouse $j$,
$b_{i} \quad$ fixed costs for plant $i$,
$c_{j k}^{p} \quad$ the unit transportation cost of product $p$ from warehouse $j$ to customer/retailer k ,
$d_{j} \quad$ fixed establishment and operating costs of warehouse/DC $j$, $e_{j}^{p} \quad$ the unit throughput cost of product p at warehouse/DC j ,
$f_{i}^{p} \quad$ the unit procurement cost of product p at plant i ,
$A_{i j}^{p} \quad$ the total unit logistics cost of product p from plant i to warehouse j ,
$C_{i j}^{p} \quad$ the total unit logistics cost of product p from warehouse j to customer/retailer k ,
$D_{k}^{p} \quad$ demand of customer/retailer k of product p,
$U_{j}^{p}$ maximum inventory capacity of product p at warehouse j,
$P_{i}^{p} \quad$ maximum production capacity of product $p$ at plant i ,
$x_{i j}^{p} \quad$ quantity of product $\mathbf{p}$ from plant i to warehouse $/ \mathrm{DC} \mathrm{j}$,
$w_{i k}^{p} \quad$ quantity of product p from warehouse/DC j to customer/retailer k,
$y_{i} \quad a 0-1$ variable that isl if a plant is located at site i , and 0 otherwise.
$z_{j} \quad a 0-1$ variable that is 1 if warehouse/DC is located at site j and 0 otherwise.

### 3.5 Single-product Capacitated Two-echelon Facility Location Problem (SCTFL)

### 3.5.1 Mixed-Integer Linear Programming

Although the main focus in this study is on the multi-product supply chain problem, we believe that it is better to understand the nature of the easier but similar problem of SCTFL first before moving on to the more complicated MCTFL problem. SCTFL provides
not only the fundamental insight required to model the multi-product supply chain problem, but also the heuristic solution to solve similar problems. With the superscript $p$ dropped from the parameters for the singie product case, the following is the mixed integer linear programming model for SCTFL.

## Problem 1 (P1):

Minimize $\sum_{i=1}^{I} \sum_{j=1}^{J} a_{i j} x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=1}^{J} \sum_{k=1}^{K} c_{j k} w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$

$$
\begin{equation*}
+\sum_{j=1}^{J} \sum_{k=1}^{K} e_{j} w_{j k}+\sum_{i=1}^{l} \sum_{j=1}^{J} f_{i} x_{i j} \tag{3.1}
\end{equation*}
$$

Or
Minimize $\sum_{i=1}^{I} \sum_{j=1}^{J}\left(a_{i j}+f_{i}\right) x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=1}^{J} \sum_{k=1}^{K}\left(c_{j k}+e_{j}\right) w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$
Or
Minimize $\sum_{i=1}^{I} \sum_{j=1}^{J} A_{i j} x_{i j}+\sum_{i=1}^{l} b_{i} y_{i}+\sum_{j=1}^{J} \sum_{k=1}^{K} C_{j k} w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k} \geq D_{k}, & \forall k \in K, \\
\sum_{k=1}^{K} w_{j k} \leq U_{j} z_{j}, & \forall j \in J, \\
\sum_{i=1}^{I} x_{i j}=\sum_{k=1}^{K} w_{j k}, & \forall j \in J, \\
\sum_{j=1}^{J} x_{i j} \leq P_{i} y_{i}, & \forall i \in I, \\
x_{i j} \geq 0, & \forall i \in I, j \in J, \\
w_{j k} \geq 0, & \forall j \in J, k \in K, \\
y_{i}, z_{j} \in\{0,1\}, & \forall i \in I, j \in J, \tag{3.10}
\end{array}
$$

In this problem, we have a set of potential locations for plants and warehouses with fixed costs and capacities. A product, for a set of customers with known demands, is to be supplied from plants via warehouses. The unit logistics cost for the product supplied from the plants to all customers via warehouses are given. The problem is to find the subset of plants and warehouses that will minimize the total fixed and logistic costs such that the demand for all the customers can be satisfied without violating the capacity constraints of the plants and warehouses. Equation (3.3) is the problem objective function to minimize the total supply chain cost. Constraint (3.4) requires that demand is satisfied and constraints (3.5) and (3.7) prevent upper bound violations of supplies for the warehouses and plants respectively. Constraints (3,6) balance in-flow product and out-flow product at warehouses. Notice that constraints (3.5) and (3.7) can accommodate both upper and lower limits on supply. Constraints (3.5) and (3.7) also ensure that supplies can only be generated from a facility if and only if the facility exists.

### 3.5.2 Solution Procedure for SCTFL

In this section, a method based on a Lagrangian relaxation is presented. The Lagrangian relaxation scheme has been used successfully in various location and assignment problems (Swain, 1974, Nauss, 1978, Geoffrion and McBride, 1978, Christofides and Beasley, 1983, Sridharan, 1993, Pirkul and Jayaraman, 1996, Park, Lim and Lee, 1998, Holmberg and Hellstrand, 1998). Lagrangian relaxation is an approach used for solving mixed integer and pure integer programming problems. In this section, we present a solution procedure based on Lagrangian relaxation for a Single-product Capacitated Twoechelon Facility Location Problem (SCTFL). We denote our original SCTFL problem by P1
and its relaxed problems by LP ( $\mu$ ), where $\mu$ refers to the vector of Lagrangian multipliers used.

According to problem P1, the set of constraints 3.6 is the hard constraint set. Without these constraints SCTFL becomes two separate capacitated single-product singleechelon problem, one for the warehouse location problem and the other for the plant location problem. These two problems are usually called "Capacitated Facility Location Problem (CFL)" and could be solved by many existing methods. By relaxing constraint 3.6 using the Lagrangian multipliers, the relaxation problem becomes as follow:

## Lagrangian relaxation of problem $1(\operatorname{LP}(\mu))$ :

Minimize $\sum_{i=1}^{I} \sum_{j=1}^{J} A_{i j} x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=1}^{J} \sum_{k=1}^{K} C_{j k} w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$ $+\sum_{j=1}^{J} \mu_{j}\left(\sum_{i=1}^{l} x_{i j}-\sum_{k=1}^{K} w_{j k}\right)$

Or

Minimize $\sum_{j=1 i=1}^{J} \sum_{i j}^{I}\left(\mu_{j}\right) x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=l k=1}^{J} \sum_{j k}^{K}\left(C_{j k}\right) w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to Constraints 3.4, 3.5,3.7.3.8, 3.9 and 3.10

Now, assuming a solution $\mathrm{Z}_{\mathrm{P} 1}$ is the optimal solution to P 1 . It is well-know that $\mathrm{Z}_{\mathrm{LP}}$ ${ }_{(\mu)} \leq \mathrm{Z}_{\mathrm{PI}}$. However, in general, it is not possible to guarantee finding $\mu$ for which $\mathrm{Z}_{\mathrm{LP}(\mu)}=$ $\mathrm{Z}_{\mathrm{PI}}$, but this frequently happens for particular problem instances. $\mathrm{Z}_{\mathrm{LP}(\mu)} \leq \mathrm{Z}_{\mathrm{PI}}$ allows LP to be used in place of Pl to provide lower bounds for the problem. Moreover, good feasible solutions to Pl can be obtained by perturbing nearby feasible solutions to $\operatorname{LP}(\mu)$. The result
of LP $(\mu)$ also can be used as an analytic tool for establishing worst-case bounds on the performance of heuristics.

It is obvious that our $\mathrm{LP}(\mu)$ problems can be further decomposed into the following two subproblems.

## Subproblem LP1

Minimize $\sum_{j=k=1}^{J} \sum_{j k}^{K}\left(C_{j k}-\mu_{j}\right) w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k} \geq D_{k}, & \forall k \in K, \\
\sum_{k=1}^{K} w_{j k} \leq U_{j} z_{j}, & \forall j \in J \\
w_{j k} \geq 0, & \forall j \in J, k \in K, \\
z_{j} \in\{0,1\}, & \forall j \in J,
\end{array}
$$

## Subprohlem LP2

Minimize $\sum_{j=1}^{J} \sum_{i=1}^{I}\left(A_{i j}+\mu_{j}\right) x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to

$$
\begin{array}{rr}
\sum_{i=1}^{I} x_{i j} \leq U_{j} z_{j}, & \forall j \in J, \\
\sum_{j=1}^{J} x_{i j} \leq P_{i} y_{i}, & \forall i \in I, \\
\sum_{i=1}^{I} \sum_{j=1}^{J} x_{i j} \geq \sum_{k=1}^{K} D_{k}, & \\
x_{i j} \geq 0, & \forall i \in I, j \in J, \\
y_{i} \in\{0,1\}, & \forall i \in I, \\
z_{j} \in\{0,1\}, & \forall j \in J,
\end{array}
$$

In order to solve LP2 separately and feasibly, we add constraints 3.19 and constraints
3.21 into the original set of constraints. Constraints 3.19 are used to prevent upper bound
violations of in-flow product into warehouses. Constraint 3.21 is a surrogate constraint. which is added to LP2 to produce tighter lower bounds and also increases the chance of obtaining a feasible solution to P1 during a given Lagrangian relaxation procedure. It makes sure that the in-flow product into warehouse can satisfy total customers' demand.

### 3.5.2.1 Optimal Solution Properties

It is obvious that the objective value of the relaxation $\operatorname{LP}(\mu)$ can be found after solving LP1 and LP2 separately. Now let $Z_{L P 1}$ be the optimal value of LP1 and $Z_{L P 2}$ be the optimal value of LP2. The following is the objective value of $L P(\mu)$.

$$
\begin{equation*}
Z_{L P(\mu)}=Z_{L P 1}+Z_{L P 2}-\sum_{j=1}^{J} d_{j} z_{j}^{\prime} \tag{3.25}
\end{equation*}
$$

Since the fixed costs of using particular warehouses or distribution centers appear on both LP1 and LP2 objective functions, the objective value of $\operatorname{LP}(\mu)$ in equation 3.25 is the sum of $Z_{\mathrm{LP} 1}$ and $\mathrm{Z}_{\mathrm{LP} 2}$ less the fixed costs of the particular warehouses $\left(\mathrm{d}_{\mathrm{j}}\right)$, which are opened or used (i.e., $z_{j}^{\prime}=1$, in both LP1 and LP2).

Now, to guarantee that the value in constraint 3.25 is feasible and optimal, the following properties must hold.

Property 3.1: Let $Z_{l}(\mu)$ be the set of opened warehouses in LP1, and $Z_{2}(\mu)$ be the set of opened warehouses in LP2. When $\mathrm{Z}_{1}(\mu)=\mathrm{Z}_{2}(\mu)$, but $\sum_{i=1}^{l} x_{i j} \geq \sum_{k=1}^{K} w_{j k}, \forall j \in J$, the feasible solution of $\operatorname{LP}(\mu)$ can be obtained by equation 3.25 .

Property 3.2: Let $\mu^{*}$ be the set of optimal multipliers. The optimal solution of $\operatorname{LP}\left(\mu^{*}\right)$ can be found when $Z_{1}(\mu)=Z_{2}(\mu)$ and $\sum_{i=1}^{I} x_{i j}=\sum_{k=1}^{K} w_{j k}, \forall j \in J .$, where $w_{j k}$ and $x_{i j}$ are the solutions of $\mathrm{LPl}\left(\mu^{*}\right)$ and $\mathrm{LP} 2\left(\mu^{*}\right)$ respectively.

However, in general the relaxation $\operatorname{LP}(\mu)$ might not be able to find $\mu^{*}$ which satisfies Property 3.2. To prevent this situation the following property is used to terminate the Lagrangian Decomposition (LD) heuristic.

Property 3.3: Let $\mu^{*}$ be a set of multipliers. The near optimal solution of $\operatorname{LP}\left(\mu^{*}\right)$ can be found when $\mathrm{Z}_{1}(\mu)=\mathrm{Z}_{2}(\mu)$ and $\sum_{i=1}^{I} x_{i j}-\sum_{k=1}^{K} w_{j k} \leq \varepsilon, \quad \forall j \in J$, where $\mathrm{w}_{\mathrm{jk}}$ and $\mathrm{x}_{\mathrm{ij}}$ are the solutions of $\operatorname{LPl}\left(\mu^{*}\right)$ and $\operatorname{LP2}\left(\mu^{*}\right)$ respectively, and $\varepsilon$ is a small value.

Alternatively, the LD heuristic also can be terminated using the maximum number of iterations allowed. However, the solution must be feasible or satisfy Property 3.1.

### 3.5.2.2 Lagrangian Decòmpoosition Heuristic Procedures (LD)

To solve $\mathrm{LP}(\mu)$ relaxation problem, the following heuristic procedure is used
Step 1: Initiate the multiplier values ( $\mu$ )
Step 2: Solve LP1 $(\mu)$ subproblem

- Obtaining $\mathrm{Z}_{\mathrm{l}}(\mu), \mathrm{w}_{\mathrm{jk}}$, and $\mathrm{Z}_{\mathrm{LPI}}$.

Step 3: Solve LP2( $\mu$ ) subproblem.

- Obtaining $\mathrm{Z}_{2}(\mu), \mathrm{x}_{\mathrm{ij}}, \mathrm{y}_{\mathrm{i}}$, and $\mathrm{Z}_{\mathrm{LP} 2}$.

Step 4: Find $\mathrm{Z}_{\mathrm{LP}(\mu)}$
Step 5: Checking the stopping criteria

- If stopping criteria is satisfied, stop the procedure.


## - Otherwise go to Step 6.

Step 6: Update the multiplier values ( $\mu$ ), then go to Step 2.
The following figure 3.1 shows $L D$ heuristic in each iteration.


Figure 3.1 LD heuristic in each iteration.

### 3.5.2.3 Updating Multipliers, $\mu$

There are many existing methods to update the multipliers, $\mu$. However, among the available approaches, the subgradient algorithm seems to work the best for the problem in
this study. Very simple and easy to implement without using a linear programming system approach, the multipliers values can be found relatively fast. More details about subgradient and other similar methods can be found in Wolsey (1998), Bertsimas and Orlin (1994), Geoffrion and McBride (1978), Crowder (1976), Camerini, Fratta, and Maffioli (1975), Geoffrion (1974), Held, Wolfe, and Crowder (1974), Grinold (1970).

Assume $Z_{P 1}$ is the objective function value of the feasible solution of the original problem, $Z_{L P\left(\mu^{t}\right)}$ is the objective function value of the solution of the relaxation problem in iteration $t$. and, $\theta_{l}$ is a positive scalar between 0 and 2. Then the multipliers, $\mu^{l}$, in iteration $t$ can be updated as given in Step 6 above using the following steps.

Step 6-1: (Initialization) Let $t \leftarrow 0, \mu^{t} \in\left(R^{m}\right)^{+}$and $\mu^{t}>0$

Step 6-2: $\gamma^{t} \leftarrow$ is a solution vector of $x_{i j}^{t}$ and $w_{j k}^{t}$ after solving $\operatorname{LP}\left(\mu^{t}\right)$
Step 6-3: Let $\mu^{t+1} \leftarrow \max \left\{0, \mu^{t}+\beta_{t} \gamma^{t}\right\}$, where $\beta_{t}$ is a positive scalar called the step size.
$\beta_{t}$ can be found by $\beta_{t}=\frac{\theta_{t}\left(Z_{P 1}-Z_{L P\left(\mu^{t}\right)}\right)}{\left\|\gamma^{t}\right\|^{2}}$
Step of-4: $t=t+i$ and go to Step 2 in the LD Heuristics.

### 3.6 Multi-product Capacitated Two-echelon Facility Location Problem (MCTFL)

### 3.6.1 Mixed Integer Linear Programming

MCTFL problem is used to determine facility locations of the whole supply chain when there are several commodities produced at several plants with known production
capacities. There is a known demand for each product by each customer or retailer. This demand is satisfied by shipping via regional distribution centers (DC), with each customer/retailer being assigned to at least one DC. There are upper bounds on the allowable total annual throughput of each product at each DC. The possible locations for the DCs are given, but particular sites are to be used depending on the least total systemwide cost. The problem is to determine which DC sites to use for each product, which customers should be served by each $D C$, which $D C$ should be served by each plant, and what the pattern of transportation flows should be for all products. The following mixed integer programming problem represents MCTFL.

Minimize $\sum_{p=1 i=1}^{P} \sum_{j=1}^{J} A_{i j}^{p} x_{i j}^{p}+\sum_{i=1}^{l} b_{i} y_{i}+\sum_{p=1}^{P} \sum_{j=1}^{J} \sum_{k=1}^{K} C_{j k}^{p} w_{j k}^{p}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k}^{p} \geq D_{k}^{p}, & \forall k \in K, p \in P, \\
\sum_{k=1}^{K} w_{j k}^{p} \leq U_{j}^{p} z_{j}, & \forall j \in J, p \in P, \\
\sum_{i=1}^{I} x_{i j}^{p}=\sum_{k=1}^{K} w_{j k}^{p}, & \forall j \in J, p \in P \\
\sum_{j=1}^{J} x_{i j}^{p} \leq P_{i}^{p} y_{i}, & \forall i \in I, p \in P \\
x_{i j}^{p} \geq 0, & \forall i \in I, j \in J, p \in P \\
w_{j k}^{p} \geq 0, & \forall j \in J, k \in K, p \in P \\
y_{i}, z_{j} \in\{0,1\}, & \forall i \in I, j \in J, \tag{3.33}
\end{array}
$$

As you see, the problem is to find the subset of plants and warehouses that will minimize the total supply chain costs such that the demand of all the customers can be satisfied without violating the capacity constraints of the plants and warehouses. Equation (3.26) is the problem objective function to minimize the total supply chain costs.

Constraints (3.27) require that each product demand by each customer is satisfied and constraints (3.28) and (3.30) prevent upper bound violations of supply of each product for the selected warehouses and plants respectively. Constraints (3.29) balance the in-flow product and out-flow product at warehouses. Notice that constraint (3.28) uses the upper bound for particular products at the DC or warehouse, so the problem can be decomposed into SCTFL. However, additional procedure needs to be developed to find the optimal solution.

### 3.6.2 Solution Procedure for MCTFL

It is obvious that MCTFL problem is NP-hard and much more complex than SCTFL problem. Therefore the use of a heuristic approach is appropriate in this case. As you see, MCTFL can be decomposed into $P$ different SCTFL subproblems with some modification of the second and the last terms of the objective constraint (3.26). Based on MCTFL decomposable nature, instead of solving it directly, individual products are treated as SCTFL and then try to improve the solution. The foltowing is the heuristic procedure for MCTFL.

Step 1: Arrange the products in descending order based on the total sales amount.

- Let $P^{\prime}=$ a set of ranked products.

Step 2: Let $p^{*}$ be the first product of set $P^{\prime}$. Solve SCTFL for product $p^{*}$.
$-O b t a i n Z_{p^{*}}, w_{j k}^{p^{*}}, x_{i j}^{p^{*}}, y_{i}$ and $z_{j}$

- From $y_{i}$ and $z_{j}$, now let $I^{*}=\{i\}$ and $J^{*}=\{j\}$, where $I^{*}$ and $J^{*}$ are sets of plants and DCs respectively that are used

Step 3: Set $b_{i}$ and $d_{j}=0$ for all $i \in I^{*}$ and $j \in J^{*}$ in constraint (3.26).

Step 4: Update set $P^{\prime}=P^{\prime}-\left\{p^{*}\right\}$.

Step 5: Stop when $P^{\prime}=\{\varnothing\}$. Otherwise, Go to Step 2.
The following figure 3.2 show MCTFL heuristic procedure.


Figure 3.2 MCTFL heuristic procedure.

### 3.7 Solution Procedures for LP1 and LP2

After decomposing the SCTFL into LP1 and LP2, LP1 and LP2 are solved iteratively using Bender's decomposition concepts. More details about Bender's decomposition can be found in Magnanti (1981), Geoffrion (1972), and Geoffrion and Graves (1971). It is known that Bender's decomposition generates an acceptable result when compared with other largescale linear integer methods such as Lagrangian relaxation, Dantzig (1960), Dantzig and Wolfe (1961), Geoffrion (1974), Held, Wolfe and Crowder (1974), Christofides and Beasley
(1983), Sridharan (1993), and Branch and Bound, Akinc and Khumawala (1977), Holmberg and Hellstrand (1998), Park, Lim and Lee (1998). However, as mentioned in several literature such as Cornuejols, Sridharan and Thizy (1991), Bender's method has some weaknesses when it deals with complex primal problem, the Bender's master problem. It is quite known that solving the Dual's master problem using Lagrangian multiplier is a lot easier and more efficient than Bender's master problem when using popular solvers or mathematical methods such as Simplex or Karmarkar's interior points, Kamarkar (1984), Vandebei, Meketon, and Freedman (1986), and Todd (1990). Based on this observation, we develop a heuristic to specifically solve Bender's master and subproblem. The developed heuristic generally yields an optimum, or close to optimum for the single echelon location problems. The following are the details of the heuristic procedure.

Bender's decomposition is an iterative procedure that deals with solving two separate problems. One is called Bender's master problem, and the other is called Bender's subproblem. In this study based on LP1, the master and subproblem will be placed in the following generic forms.
$\underset{z \in[0,1]}{\operatorname{Minimize}}\left[\begin{array}{ll}\left.\begin{array}{l}\text { Minimize } \\ w_{j k} \in Z^{+} \\ \text {Subject to } \\ j=1 \\ \sum_{k=1}^{K} \\ C_{j k} w_{j k}\end{array}\right] \sum_{j=1}^{J} d_{j} z_{j} \\ \sum_{j=1}^{J} w_{j k} \geq D_{k}, & \forall k \in K \\ \sum_{k=1}^{K} w_{j k} \leq I_{j} z_{j}, & \forall j \in J\end{array}\right]$

Subject to $\sum_{k=1}^{k} D_{k} \leq \sum_{j=1}^{J} I_{j} z_{j}$
or its linear programming dual form

$$
\begin{equation*}
\underset{z \in[0,1]}{\operatorname{Minimize}}\left[\underset{t \in T}{\operatorname{Maximize}} \sum_{k=1}^{K} D_{k} \lambda_{k}^{t}+\sum_{j=1}^{J}\left(d_{j}-I \mu_{j} \mu_{j}^{t}\right) z_{j}\right] \tag{3.36}
\end{equation*}
$$

Subject to $\sum_{k=1}^{k} D_{k} \leq \sum_{j=1}^{J} I_{j} z_{j}$
or

Minimize $\rho$
$z \in[0,1], \rho$
Subject to $\quad \rho \geq \sum_{k=1}^{K} D_{k} \lambda_{k}^{t}+\sum_{j=1}^{J}\left(d_{j}-I_{j} \mu_{k}^{l}\right) z_{j}, \quad$ all $t \in T$ $\sum_{k=1}^{k} D_{k} \leq \sum_{j=1}^{J} I_{j} z_{j}$

Where T is the index set of all dual feasible basic solutions $\left(\lambda^{\prime}, \mu^{\prime}\right)$ of Bender subproblems and $\lambda$ and $\mu$ correspond to the constraints (3.14) and (3.15) of LP1. The constraints indexed by $t \in T$ are called Benders or primal cuts or Bender subproblems. Benders proposed to solve a relaxation of the original problem by taking only a subset of primal cuts, and to generate cuts when necessary. In each iteration, a primal cut is generated using the dual optimal solution of Bender subproblem and added to Bender master problem. The master is then solved to give a new $z$ and $\rho$.

For LP2, the master and subproblem will be defined in the following generic forms.
$\underset{\substack{y \in[0.1] \\ z \in[0,1]}}{\substack{\text { Minimize } \\ x_{i j} \in Z^{+}}}\left[\begin{array}{ll}\text { Mimize } & \sum_{i=1}^{I} \sum_{j=1}^{J} A_{i j} x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=1}^{J} d_{j} z_{j} \\ \text { Subject to } \\ \sum_{i=1}^{I} x_{i j} \leq I_{j} z_{j}, & \\ \sum_{j=1}^{J} x_{i j} \leq P_{i} y_{i}, & \forall j \in J \\ \sum_{i=1}^{I} \sum_{j=1}^{J} x_{i j} \geq D, & \forall D \text { is const. }\end{array}\right]$

Subject to $D \leq \sum_{j=1}^{J} I_{j} z_{j}$ and $D \leq \sum_{i=1}^{I} P_{i} y_{i}$
or
Minimize $y \in[0,1]$, $z \in[0,1], \rho$
Subject to $\quad \rho \geq \sum_{j=1}^{J}\left(d_{j}-I_{j} \mu_{j}^{t}\right) z_{j}+\sum_{i=1}^{I}\left(b_{i}-P_{i} \mu_{i}^{t}\right) y_{i}+D \lambda^{t}, \quad$ all $t \in T$

$$
\begin{equation*}
D \leq \sum_{j=1}^{J} I_{j} z_{j} \text { and } D \leq \sum_{i=1}^{I} P_{i} y_{i} \tag{3.40}
\end{equation*}
$$

Again, T is the index set of all dual feasible basic solutions $\left(\lambda^{\prime}, \mu^{\prime}\right)$ of Bender subproblems, $\mu$ correspond to constraints (3.19) and (3.20), and $\lambda$ correspond to the constraint (3.21). The constraints indexed by $t \in T$ are called Benders or primal cuts or Bender subproblems of LP2.

### 3.7.1. Solving Bender's Subproblem

The following are examples of Bender's subproblems after fixing the binary variables in LP1 and LP2. For LP1, an instance with three warehouses and four customers is used.

Each of the three warehouses can be used to fill all four customers' orders. The maximum inventory of each warehouse is between 50 to 70 units and the demand of each customer is between 30 to 50 units. The following are the subproblems of this problem.

## Bender's Primal subproblem:

$\operatorname{Min} \quad 2.5 w_{11}+1.9 w_{12}+3 w_{13}+2.7 w_{14}+1.5 w_{21}+2 w_{22}+2.3 w_{23}+2.5 w_{24}$

$$
+2.1 w_{31}+3.5 w_{32}+1.1 w_{33}+2.2 w_{34}
$$

Subject to

| $w_{1 /}$ |  | $+w_{31}$ | $\geq 30$ |
| :---: | :---: | :---: | :---: |
| $w_{12}$ | $+w_{22}$ | + $w_{32}$ | $\geq 40$ |
| $w_{13}$ | $+w_{23}$ | $+w_{33}$ | $\geq 35$ |
| $w_{14}$ | $+w_{24}$ | + $w_{34}$ | $\geq 50$ |
| $w_{11}+w_{12}+w_{13}+w_{14}$ |  |  | $\leq 50$ |
|  | $+w_{22}+w_{23}+w_{24}$ |  | $\leq 60$ |
|  |  | $w_{31}+w_{32}+w_{33}+w_{34}$ | $\leq 70$ |

All $w_{j k} \geq 0$

## Bender's Dual subproblem:

$\operatorname{Max} 30 \lambda_{1}+40 \lambda_{2}+35 \lambda_{3}+50 \lambda_{4}-50 \mu_{1}-60 \mu_{2}-70 \mu_{3}$
Subject to


All $\lambda_{k}$ and $\mu_{j} \geq 0$

For LP2, the example of three plants and four warehouses are used. Each of the three plants can be used to fill demands from all warehouses. The maximum production capacity of each plant is between 50 to 70 units and the demand of each warehouse is between 30 to 50 units. The following are the subproblems of this problem.

## Bender's Primal subproblem:

Min $2.5 x_{11}+1.9 x_{12}+3 x_{13}+2.7 x_{14}+1.5 x_{21}+2 x_{22}+2.3 x_{23}+2.5 x_{24}$ $+2.1 x_{31}+3.5 x_{32}+1.1 x_{33}+2.2 x_{34}$

Subject to

| $x_{I I}+$ | $+x_{21} \quad+$ | $+x_{31}$ | $\leq 30$ |
| :---: | :---: | :---: | :---: |
| $x_{12}$ | $+x_{22}$ | $+x_{32}$ | $\leq 40$ |
| $x_{13}$ | $+x_{23}$ | $+x_{33}$ | $\leq 35$ |
| $x_{14}$ | $+x_{24}$ | 24 $+x_{34}$ | $\leq 50$ |
| $x_{11}+x_{12}+x_{13}+x_{14}$ |  |  | $\leq 50$ |
|  | $x_{21}+x_{22}+x_{23}+x_{24}$ |  | $\leq 60$ |
|  |  | $x_{31}+x_{32}+x_{33}+x_{34}$ | $\leq 70$ |
| $x_{11}+x_{12}+x_{13}+x_{14}+$ | $+x_{21}+x_{22}+x_{23}+x_{24}+$ | $+x_{31}+x_{32}+x_{33}+x_{34}$ | $\geq 130$ |
| All $x_{j k} \geq 0$ |  |  |  |

## Bender's Dual subproblem:

Max $\quad-30 \mu_{1}-40 \mu_{2}-35 \mu_{3}-50 \mu_{4}-50 \mu_{5}-60 \mu_{6}-70 \mu_{7}+130 \lambda$
Subject to


All $\lambda_{k}$ and $\mu_{j} \geq 0$

To feasibly and effectively solve Bender's subproblems above, we first determine Bender's primal subproblem, which is in the form of a simple transportation problem and easy to solve. Since the problem deals with the large-scale number of integer variables, the application of Vogel's approximation method (VAM), which is known as a near optimal heuristic with less complexity and computational time, is selected to find the primal solution. Next, the affine-scaling method and Cholesky factorization method are utilized to trace out the dual solution. The following are the details of the method.

### 3.7.1.1. Modified Vogel's Approximation Method for LP1

Step1: Determine the penalty for each row (column) by subtracting the second highest cost element in the row (column) from the highest cost element in the same row (column).

Step2: Determine the row or column with the largest penalty, breaking ties arbitrarily. Allocate as much as possible to the variable with the least cost in the selected row or column. Make adjustment to the supply and demand and then cross out the satisfied row or column. If a row and a column are satisfied simultaneously, just one of them is crossed out and the remaining row (column) is set to zero supply (demand). Any row or column with zero supply or demand should not be used in calculating future penalties (in step 3).

## Step3:

a) If exactly one row or one column remains uncrossed out and there is only one row (column) with positive supply, determine the basic variables in the row (column) by the least-cost method (as described in the next section). Stop.
b) If all uncrossed-out rows and columns have (assigned) zero supply and demand, determine the zero basic variables by the least-cost method. Stop.
c) Otherwise, recalculated the penalties for the uncrossed-out rows and columns, then go to step 2. (Notice that the rows and columns with assigned zero supply and demand should not be used in computing these penalties.)

## The Least-cost Method

The procedure is as follows. Assign as much as possible to the variable with the smallest unit cost in the entire tableau (Ties are broken arbitrarily.) Cross out the satisfied row or column (If both a column and a row are satisfied simultaneously, only one may be crossed out.) After adjusting the supply and demand for all uncrossed-out rows and columns, repeat the process by assigning as much as possible to the variable with the smallest uncrossed-out unit cost. The procedure is complete when exactly one row or one column remains uncrossed out.

To demonstrate the Vogel method for LP1, an instance with three warehouses and four customers is used. Each of the three warehouses can be used to fill all four customers' orders. The maximum inventory of each warehouse is between 50 to 70 units and the demand of each customer is between 30 to 50 units.

Numerical example for LPI Bender's subproblem:

| Iteration 0 | Customer |  |  |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | Dummy |  |  |
| $\begin{gathered} \text { DCs } \\ 1 \end{gathered}$ | 2.5 | 1.9 | 3.0 | 2.7 | M | 50 | 0.3 |
|  |  | 40 |  |  |  |  |  |
| 2 | 1.5 | 2.0 | 2.3 | 2.5 | M | 60 | 0.2 |
|  |  |  |  |  |  |  |  |
| 3 | 2.1 | 3.5 | 1.1 | 2.2 | M | 70 | 1.3 |
|  |  |  |  |  |  |  |  |
| Demand | 30 | 40 | 35 | 50 |  |  |  |
| Penalty | 0.4 | 1.5 | 0.7 | 0.2 |  |  |  |

- The largest penalty is 1.5 at column \#2.
- Number of allocated products is 40 units from DC \#1 to Customer \#2.

| Iteration <br> 1 | Customer |  |  |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | Dummy |  |  |
| $\underset{1}{\mathrm{DCs}}$ | 2.5 | 1.9 | 3.0 | 2.7 | M |  |  |
|  |  | 40 |  |  |  | 10 | 0.3 |
| 2 | 1.5 | 2.0 | 2.3 | 2.5 | M |  |  |
|  |  |  |  |  |  | 60 | 0.2 |
| 3 | 2.1 | 3.5 | 1.1 | 2.2 | M |  |  |
|  |  |  | 35 |  |  | 70 | 0.1 |
| Demand | 30 | 40 | 35 | 50 |  |  |  |
| Penalty | 0.4 |  | 0.7 | 0.2 |  |  |  |

- Number of allocated products is 35 units from DC \#3 to Customer \#3.

- Column \#3 is crossed out and updated supply of DC \#3 is 35 units.
- The largest penalty is 1.0 at row \#2.
- Number of allocated products is 30 units from DC \#2 to Customer \#1.

- Column \#1 is crossed out and updated supply of DC \#2 is 30 units.
- Since there is only one remaining column, the least-cost method is used.
- Number of allocated product is 35 and 15 units from DC \#3 to Customer \#4 and from DC \#2 to Customer \#4, respectively.

| Iteration Final | Customer |  |  |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | Dummv |  |  |
| $\begin{gathered} \text { DCs } \\ 1 \end{gathered}$ | 2.5 | 1.9 | 3.0 | 2.7 | M |  |  |
|  |  | 40 |  |  |  | 10 |  |
| 2 | 1.5 | 2.0 | 2.3 | 2.5 | M |  |  |
|  | 30 |  |  | 15 |  | 15 |  |
| 3 | 2.1 | 3.5 | 1.1 | 2.2 | M |  |  |
|  |  |  | 35 | 35 |  | 0 |  |
| Demand | 30 | 40 | 35 | 50 |  |  |  |
| Penalty |  |  |  |  |  |  |  |

- Updated supply of DC \#2 is 15 units and DC \#3 is zero.


### 3.7.1.2. Modified Vogel's Approximation Method for LP2

Step 1: Set $D=$ total needed product (total demands at DCs level).

Step 2: Determine a penalty for each row (column) by subtracting the second highest cost element in the row (column) from the highest cost element in the same row (column)

Step 3: Determine the row or column with the largest penalty, breaking ties arbitrarily. Allocate N product units to the variable with the least cost in the selected row or column, where $\mathrm{N}=$ minimize (demand, supply, D ). Make adjustment to the supply and demand and then cross out the satisfied row or column. If a row and a column are satisfied simultaneously, just one of them is crossed out and the remaining row (column) is set to zero
supply (demand). Any row or column with zero supply or demand should not be used in calculating future penalties (in step 4).

## Step 4:

a) If exactly one row or one column remains uncrossed out and there is only one row (column) with positive supply (demand), determine the basic variables in the row (column) by the least-cost method to allocate the remaining D. Then update D value. Stop.
b) If all uncrossed-out rows and column have (assigned) zero supply and demand, determine the zero basic variables by the least-cost method to allocate the remaining D. Stop.
c) Otherwise, recalculate the penalties for the uncrossed-out rows and columns and update D value, then go to step 3. (Notice that the rows and columns with assigned zero supply and demand should not be used in computing these penalties.)

To demonstrate the Modified Vogel's Approximation method for LP2, an example of three plants and four warehouses are used. Each of the three plants can be used to fill demands from all warehouses. The maximum production capacity of each plant is between 50 to 70 units and the demand of each warehouse is between 30 to 50 units.

## Numerical example for LP2 Bender's subproblem:

| Iteration 0 | Warehouse |  |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |  |  |
| Plant | 2.5 | 1.9 | 3.0 | 2.7 | 50 | 0.3 |
|  |  | 40 |  |  |  |  |
| 2 | 1.5 | 2.0 | 2.3 | 2.5 | 60 | 0.2 |
|  |  |  |  |  |  |  |
| 3 | 2.1 | 3.5 | 1.1 | 2.2 | 70 | 1.3 |
|  |  |  |  |  |  |  |
| Demand | 30 | 40 | 35 | 25 |  |  |
| Penalty | 0.4 | 1.5 | 0.7 | 0.2 |  |  |

- Total needed product $=130$ units
- Number of allocated products $=\min \{40,50,130\}=40$ units

| Iteration 1 | Warehouse |  |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 |  |  |  |
| $\begin{gathered} \text { Plant } \\ 1 \end{gathered}$ | 2.5 | $\frac{19}{40}$ | 3.0 | 2.7 | 10 | 0.3 |
| 2 | 1.5 | 20 | 2.3 | 2.5 | 60 | 0.2 |
| 3 | 2.1 |  | 1.1 <br> 35 | 2.2 | 70 | 0.1 |
| Demand | 30 | 40 | 35 | 25 |  |  |
| Penalty | 0.4 |  | 0.7 | 0.2 |  |  |

- Total needed product $=\{130-40\}=90$ units.
- Number of allocated products $=\min \{35,70,90\}=35$ units

| $\begin{gathered} \text { Iteration } \\ 2 \end{gathered}$ | Warehouse |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 23 | 4 |  |  |
| Plant <br> 1 | 2.5 | R.92, $530{ }^{2}$ | 2.7 | 10 | 0.2 |
| 2 | 1.5 |  | 2.5 | 60 | 1.0 |
| 3 | 2.1 |  | 2.2 | 35 | 0.1 |
| Demand | 30 |  | 25 |  |  |
| Penalty | 0.4 |  | 0.2 |  |  |

- Total needed products $=\{90-35\}=55$ units.
- Number of allocated products $=\min \{30,60,55\}=30$ units.

| Iteration 2 | Warehouse |  |  |  | Supply | Penalty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |  |  |
| Plant 1 |  |  |  | 2.7 | 10 |  |
| 2 | $\frac{1 S^{2}}{3}$ |  |  | 2.5 | 30 |  |
| 3 | $21$ |  | $\frac{5+1}{5+35}$ | 2.2 <br> 25 | 35 |  |
| Demand | 30 | Y80家 | - 35 | 25 |  |  |
| Penalty |  |  |  |  |  |  |

- Total needed products $=\{55-30\}=25$ units.
- Number of allocated product $=\min \{50,35,25\}=25$ units.


### 3.7.1.3. Finding Dual Subproblem Solution from the Primal Subproblem Solution

In order to quickly estimate the dual solution from the primal outcome, the knowledge of the affine-scaling method and the Numeric Cholesky factorization are utilized. The following standard optimization problems are used to demonstrate the method.

Primal: Minimize $\quad c^{T} W$
Subject to $A w=b \quad w \geq 0$
Dual: Maximum $b^{T} \lambda$
Subject to $A^{T} \lambda \leq c \quad \lambda$ is free

## How to apply the affine-scaling method

To find the dual solution, the original problem is scaled using an affine transformation. The following are the scaled problem and its scaling relationship.

| Primal $:$ | Minimize $\quad c{ }_{1}^{T} W_{1}$ |
| ---: | :--- |
|  | Subject to $\quad A_{1} W_{1}=b \quad W_{1} \geq 0$ |

Where
$w_{1}=D^{-1} x \quad A_{1}=A D \quad c_{1}=D c$,
and
$w_{1}=\left[\begin{array}{c}1 \\ 1 \\ : \\ \vdots \\ 1\end{array}\right], \quad D=\left[\begin{array}{lllll}w_{1} & & & & \\ & w_{2} & & & \\ & & \ldots & & \\ & & & \ldots & \\ & & & & w_{n}\end{array}\right]$

According to the affine-scaling method, the dual solution can be estimated when there is an available primal solution. For
more information about the affine-scaling method, the reader is referred to Arbel (1993). The equation below is used to estimate the solution vector for the dual problem when the original problem is in the scaling form using affine transformation.

$$
\begin{equation*}
\lambda=\left(A D^{2} A^{T}\right)^{-1} A D^{2} c \quad \text { or } \quad\left(A D^{2} A^{T}\right) \lambda=A D^{2} c \tag{3.41}
\end{equation*}
$$

## How to apply Chelosky Factorization

As you see, to find the inverse matrix, $\left(A D^{2} A^{T}\right)^{-1}$, is an expensive operation and in most cases is not needed for obtaining the solution to the system of equation. To avoid this costly operation, Chelosky factorization method is applied. Chelosky factorization method is a solution approach for general linear system of equations, which has a symmetry. It is also known as one of the best methods for a computer based solution. Since, the matrix, $\left(A D^{2} A^{T}\right)$ in equation (3.41) is symmetric, the Cholesky factorization of $\left(A D^{2} A^{T}\right)$ can be written as

$$
\begin{equation*}
A D^{2} A^{T}=L L^{T} \tag{3.42}
\end{equation*}
$$

The $\mathrm{m} \times \mathrm{m}$ lower triangular matrix $L$ is referred to as the Cholesky factor. To derive the Cholesky factor, the product form of $\left(A D^{2} A^{T}\right)$ can be written out in an explicit manner as following.

$$
A D^{2} A^{T}=\left[\begin{array}{ccccc}
a_{11} & a_{12} & \ldots & \ldots & a_{1 m} \\
a_{21} & a_{22} & \ldots & \ldots & a_{2 m} \\
\ldots & \ldots & \ldots & \ldots & \ldots \\
\ldots & \ldots & \ldots & \ldots & \ldots \\
a_{m 1} & a_{m 2} & \ldots & \ldots & a_{m m}
\end{array}\right]=L L^{T}=\left[\begin{array}{ccccc}
l_{11} & 0 & \ldots & \ldots & 0 \\
l_{21} & l_{22} & \ldots & \ldots & 0 \\
& \ldots & \ldots & \ldots & \ldots \\
& \ldots & \ldots & \ldots & \ldots \\
l_{m 1} & l_{m 2} & \ldots & \ldots & l_{m m}
\end{array} \begin{array}{cccccc}
l_{11} & l_{21} & \ldots & \ldots & l_{m 1} \\
0 & l_{22} & \ldots & \ldots & l_{m 2} \\
\ldots & \ldots & \ldots & \ldots & \\
0 & 0 & \ldots & 0 & l_{m m}
\end{array}\right]
$$

To come up with the factor in this study, the column-wise Cholesky factorization algorithm Arbel (1993) is performed. The row-wise Cholesky factorization algorithm can be found in Martin (1999). The column-wise algorithm is described below.

```
For \(q=1,2, \ldots, m:\) (column indexes)
    \(l_{q q}=\sqrt{a_{q q}-\sum_{j=1}^{q-1} l_{q j}^{2}} \quad\) (diagonal element)
    For \(i=q+1, \ldots . . ., m:(\) row indixes \()\)
        \(l_{i q}=\frac{a_{i q}-\sum_{p=1}^{q-1} l_{i p} l_{q p}}{l_{q q}} \quad\) (elements below the diagonal)
    End
End
```

Now, suppose a matrix $\left(A D^{2} A^{T}\right)$ is factored through a Cholesky factorization scheme, the solution to the symmetric system of equations, now, can be easily obtained using a forward and backward solve cycles. Based on the equation (3.41) and (3.42), the original problem now becomes

$$
\begin{equation*}
L L^{r_{\lambda}}=A D^{\dot{2}} c \tag{3.43}
\end{equation*}
$$

Next, by defining $v=L^{T} \lambda$ equation (3.43) is rewritten as

$$
\begin{equation*}
L v=A D^{2} c \tag{3.44}
\end{equation*}
$$

and because $L$ is a lower triangular matrix, finding this system solution is easily accomplished. Suppose the vector $b=A D^{2} c$. Writing (3.44) explicitly becomes

$$
\left[\begin{array}{ccccc}
l_{11} & 0 & \ldots & \ldots & 0  \tag{3.45}\\
l_{21} & l_{22} & \ldots & \ldots & 0 \\
& \ldots & \ldots & \ldots & \ldots \\
& \ldots & \ldots & \ldots & \ldots \\
l_{m 1} & l_{m 2} & \ldots & \ldots & l_{m m}
\end{array}\right]\left[\begin{array}{c}
v_{1} \\
v_{2} \\
\ldots \\
v_{m}
\end{array}\right]=\left[\begin{array}{c}
b_{1} \\
b_{2} \\
\ldots \\
\ldots \\
b_{m}
\end{array}\right]
$$

Finding the system solution shown above can be accomplished in a forward manner by starting to solve for $v_{1}$ from the first equation, followed by solving for $v_{2}$ from the second equation, and so on. This process is called a forward solve cycle. Once the solution for $v$ is available, the process of solving the vector $\lambda$ can begin using the following system.

$$
\begin{equation*}
L^{\top} \lambda=v \tag{3.46}
\end{equation*}
$$

Since $L^{T}$ is an upper triangular matrix, the solution process, first, starts by solving for $\lambda_{m}$. and going backward toward obtaining the solution for $\lambda_{1}$. This solution process is known as a backward solve cycle.

The affine-scaling and Chelosky factorization methods are demonstrated next through the same numerical example used earlier in demonstrating the VAM method in section
3.7.1.1.

Affine-scaling \& Chelosky factorization numerical Example

$$
\begin{aligned}
\text { Min } & 2.5 w_{11}+1.9 w_{12}+3 w_{13}+2.7 w_{14}+1.5 w_{2 l}+2 w_{22}+2.3 w_{23}+2.5 w_{24} \\
& +2.1 w_{31}+3.5 w_{32}+1.1 w_{33}+2.2 w_{34}
\end{aligned}
$$

Subject to

| $w_{H}+$ | $+w_{2 l}$ | $+w_{31}$ | $\geq 30$ |
| :---: | :---: | :---: | :---: |
| $w_{12}$ | $+w_{22}$ | + $w_{32}$ | $\geq 40$ |
| $w_{13}$ | $+w_{23}$ | $+w_{33}$ | $\geq 35$ |
| $w_{14}$ | $+w_{24}$ | $+w_{34}$ | $\geq 50$ |
| $w_{11}+w_{l 2}+w_{l 3}+w_{l 4}$ |  |  | $\leq 50$ |
|  | $w_{21}+w_{22}+w_{23}+w_{24}$ |  | $\leq 60$ |
|  |  | $w_{31}+w_{32}+w_{33}+w_{34}$ | $\leq 70$ |
| All $w_{j k} \geq 0$ |  |  |  |

Suppose the primal solution of the problem is $w_{12}=40, w_{21}=30, w_{24}=15, w_{33}=35$, and $w_{34}=35$. The following vectors can be formed.

$A=\left[\begin{array}{rrrrrrrrrrrrrrrrrrr}1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & -1 & 0 & 0 & 0 \\ -1 & -1 & -1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & -1 & -1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & -1 & -1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 1\end{array}\right]$
Step 1: Given the primal solution from VAM, the scaling matrix, $D, A D^{2} A^{T}$ and the vector $A D^{2} c$ are formed. These are as given below.


$$
A D^{2} A^{T}=\left[\begin{array}{rrrrrrr}
900 & 0 & 0 & 0 & 0 & -900 & 0 \\
0 & 1600 & 0 & 0 & -1600 & 0 & 0 \\
0 & 0 & 1225 & 0 & 0 & 0 & -1225 \\
0 & 0 & 0 & 1450 & 0 & -225 & -1225 \\
0 & -1600 & 0 & 0 & 1700 & 0 & 0 \\
-900 & 0 & 0 & -225 & 0 & 1350 & 0 \\
0 & 0 & -1225 & -1225 & 0 & 0 & 2450
\end{array}\right], \quad A D^{2} c=\left[\begin{array}{r}
1350.0 \\
3040.0 \\
1347.5 \\
3257.5 \\
-3040.0 \\
-1912.5 \\
-4042.5
\end{array}\right]
$$

Step 2: Solve for the estimate of the dual vector, $\lambda$, from equation (3.41). Begin by applying Cholesky factorization algorithm to find the lower triangular matrix, Cholesky factor from the matrix $A D^{2} A^{T}$. The result of this method is given below.

$$
L=\left[\begin{array}{rrrrrrr}
30.00 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 40.00 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 35.00 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 38.08 & 0 & 0 & 0 \\
0 & -40.00 & 0 & 10.00 & 0 & 0 & 0 \\
-30.00 & 0 & 0 & -5.91 & 0 & 20.37 & 0 \\
0 & 0 & -35.00 & -32.17 & 0 & -9.33 & 10.15
\end{array}\right]
$$

Step 3: Applying a forward solve cycle, namely, solving for $v$ from equation (3.44)

$$
\left[\begin{array}{rrrrrrr}
30.00 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 40.00 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 35.00 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 38.08 & 0 & 0 & 0 \\
0 & -40.00 & 0 & 10.00 & 0 & 0 & 0 \\
-30.00 & 0 & 0 & -5.91 & 0 & 20.37 & 0 \\
0 & 0 & -35.00 & -32.17 & 0 & -9.33 & 10.15
\end{array}\right]\left[\begin{array}{l}
v_{1} \\
\nu_{2} \\
v_{3} \\
\nu_{4} \\
v_{5} \\
v_{6} \\
\nu_{7}
\end{array}\right]=\left[\begin{array}{r}
1350.0 \\
3040.0 \\
1347.5 \\
3257.5 \\
-3040.0 \\
-1912.5 \\
-4042.5
\end{array}\right]
$$

The result of this process is given below.

$$
\nu=\left[\begin{array}{r}
45.00 \\
76.00 \\
38.50 \\
85.55 \\
0.00 \\
-2.80 \\
3.05
\end{array}\right]
$$

Step 4: Apply a backward solve cycle, namely, solve for $\lambda$ from the equation (3.44).

$$
\left[\begin{array}{rrrrrrr}
30.00 & 0 & 0 & 0 & 0 & -30.00 & 0 \\
0 & 40.00 & 0 & 0 & -40.00 & 0 & 0 \\
0 & 0 & 35.00 & 0 & 0 & 0 & -35.00 \\
0 & 0 & 0 & 38.08 & 10.00 & -5.91 & -32.17 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 20.37 & -9.33 \\
0 & 0 & 0 & 0 & 0 & 0 & 10.15
\end{array}\right]\left[\begin{array}{l}
\lambda_{1} \\
\lambda_{2} \\
\lambda_{3} \\
\lambda_{4} \\
\mu_{1} \\
\mu_{2} \\
\mu_{3}
\end{array}\right]=\left[\begin{array}{r}
45.00 \\
76.00 \\
38.50 \\
85.55 \\
0.00 \\
-2.80 \\
3.05
\end{array}\right]
$$

The result of this process, which is the dual subproblem solution, is given beiow.
$\lambda=\left[\begin{array}{l}1.50 \\ 1.90 \\ 1.40 \\ 2.50 \\ 0.00 \\ 0.00 \\ 0.30\end{array}\right]$

### 3.7.2. Solving Bender's Master Optimal Problem, BMO

The following is an example of Bender's Master Problem in a supply chain system that includes the single echelon system in both LP1 and LP2 decomposition problem.

Min $\rho$
Subject to $\quad \rho \geq 21+2 Y_{1}-4 Y_{2}-7 Y_{3}$
$\rho \geq 12+0 Y_{1}+3 Y_{2}+3 Y_{3}$
$\rho \geq 15-2 Y_{1}+0 Y_{2}+3 Y_{3}$
$10 Y_{1}+20 Y_{2}+30 Y_{3} \geq 30$

$$
\begin{equation*}
Y_{l}, Y_{2}, Y_{3} \in\{0,1\} \tag{3.48}
\end{equation*}
$$

As mentioned in the earlier chapters, the objective of this study is to develop a heuristic to deal with large-scale problem with an acceptable computational time. Therefore, the problem is solved using an iterative heuristic procedure. BMO is established based on a penalty concept similar to Vogel's approximation and Dynamic Programming methods. In all experimental problems, BMO method could yield an optimum with a short computational time. Details of the method are explained below.

## BMO's heuristic procedures

First, let I be the set of binary variables in the master problem, and let J be the set of constraints that have the variable (Y), except constraint (3.48). Then, let $\mathrm{I}_{0}$ be the set of binary variables, $Y_{i}$, that has a zero value, and let $I_{1}$ be the set of binary variables, $Y_{i}$, that has the value of one, $\left(I=I_{0} \cup I_{1}\right)$. Now, let $Z^{B}$ be the best objective value so far, $Z^{k}$ be the objective value at iteration k , and $\mathrm{S}_{\mathrm{j}}{ }^{\mathrm{k}}$ be the constraint value when considering only constraint j in iteration k (the rest of the constraints are temporarily ignored). Also, let $\mathrm{S}_{\mathrm{ij}}$ be another constraint value when considering only constraint $j$ while letting $Y_{i}$ in $I_{l}$ equal to zero, and $a_{i j}$ be the coefficient of $Y_{i}$ variables in constraint $j$. Finally, let $b_{i j}$ be the coefficient of $Y_{i}$ variable and D be the constant value on the right hand side of constraint (3.48). The detailed steps of the procedure and an example of BMO table are as follows:

## BMO heuristic procedures:

Step 0: Set $\mathrm{I}_{0}=\{\varnothing\}, \mathrm{I}_{\mathrm{I}}=\{\mathrm{I}\}$, and $\mathrm{k}=0$,
Step 1: Evaluate $S_{j}^{k}$ value for $\forall j \in J$ by letting $Y_{i}=1$ for $i \in I_{1}$, and $Y i=0$ for $I \in I_{0}$.
Step 2: Evaluate $\mathrm{Z}_{\text {max }}$ value where $Z_{\max }=\operatorname{Max}_{\forall j \in J}\left(S_{j}^{k}\right)$, and let $\mathrm{Z}^{\mathrm{k}}=\mathrm{Z}_{\text {max }}$ and $Z^{B}=Z^{k}$.

Step 3: Increase k value by one.
Step 4: Evaluate $\mathrm{S}_{\mathrm{ij}}$ value where $\mathrm{S}_{\mathrm{ij}}=\left\{\mathrm{S}_{\mathrm{j}}^{\mathrm{k} \cdot \mathrm{I}}-\mathrm{a}_{\mathrm{ij}}\right\}$, for $\mathrm{i} \in \mathrm{I}_{\mathrm{I}}$, and $\mathrm{j} \in \mathrm{J}$.
Step 5: Find $S_{i}$ value where $S_{i}=\operatorname{Max}\left\{S_{i j}: j \in J\right\}$, for $i \in I_{1}$.
Step 6: Evaluate $Z^{k}$ value where $Z^{k}=\operatorname{Min}\left\{S_{i}: i \in I_{1}\right\}$, and let $i^{*}=i$ which has the minimum value of $\mathrm{S}_{\mathrm{i}}$.

## Step 7:

a) If $Z^{\mathrm{k}} \leq \mathrm{Z}^{\mathrm{B}}$ and $\sum_{i=1}^{I_{i}^{\prime}} b_{i} Y_{i} \geq D, \forall I^{\prime}=\left\{I_{1}-i^{*}\right\}$, let $\mathrm{Z}^{\mathrm{B}}=\mathrm{Z}^{\mathrm{k}}$ and move $\mathrm{i}^{*}$ from $\mathrm{I}_{1}$ to $\mathrm{I}_{0}$, then go to Step 8.
b) If $\mathrm{Z}^{\mathrm{k}} \leq \mathrm{Z}^{\mathrm{B}}$ but $\sum_{i=1}^{I^{\prime}} b_{i} Y_{i} \leq D, \forall I^{\prime}=\left\{I_{1}-i^{*}\right\}$, remove $\mathrm{S}_{\mathrm{i}^{*}}$ from the consideration, then go back to Step 6.
c) Otherwise, Stop.

Step 8: a) If $\left|I_{\|}\right|=1$, Stop.
b) Set $S_{j}^{k}$ value where $S_{j}{ }^{k}=S_{i}{ }^{*} j$ for $j \in J$, and $i{ }^{*}$ is the result from Step 6. Then go to Step 3.

Figure 3.3 shows an example of BMO table used to store all variables generated by the heuristic in each iteration. The example table represents a problem involving three 0-1 variables and three constraints.

| $\mathbf{a}_{11}$ | $\mathrm{a}_{12}$ | $\mathrm{a}_{13}$ |  |
| :---: | :---: | :---: | :---: |
| $S_{11}$ |  |  | S ${ }^{\text {, }}$ |
|  | $\mathbf{S}_{12}$ | $S_{13}$ |  |
| $\mathrm{a}_{21}$ | $\mathbf{a}_{22}$ | $\mathrm{a}_{23}$ | $S_{2}{ }^{\text {k }}$ |
| $\mathrm{S}_{21}$ | $\mathrm{S}_{22}$ | S 3 |  |
| $a_{31}$ | $\mathrm{a}_{32}$ | $a_{33}$ | S, ${ }^{\text {k }}$ |
| $\mathrm{S}_{31}$ | $\mathbf{S}_{32}$ | $\mathrm{S}_{3}$ |  |
| $S_{1}$ | $S_{2}$ | S | $\mathrm{Z}^{\mathbf{4}}$ |

Figure 3.3 Shows all variables in BMO table.

## BMO numerical example, referred to (3.47):

Min $\rho$
Subject to $\quad \rho \geq 21+2 Y_{1}-4 Y_{2}-7 Y_{3}$

$$
\begin{aligned}
& \rho \geq 12+0 Y_{1}+3 Y_{2}+3 Y_{3} \\
& \rho \geq 15-2 Y_{1}+0 Y_{2}+3 Y_{3} \\
& 10 Y_{1}+20 Y_{2}+30 Y_{3} \geq 30 \\
& Y_{l}, Y_{2}, Y_{3} \in\{0,1\}
\end{aligned}
$$

$$
k=0
$$

$$
\mathrm{I}_{0}=\{\varnothing\}, \text { and } \mathrm{I}_{1}=\{1,2,3\} . \quad \mathrm{D}=30
$$

$$
Z^{B}=18
$$

| 2 | 4 |  | 12 |
| :---: | :---: | :---: | :---: |
| $S_{4}$ | $\mathrm{S}_{12}$ | $\mathrm{S}_{13}$ |  |
| 0 | 3 | 3 | 18 |
| $\mathrm{S}_{21}$ | $\mathrm{S}_{22}$ | $\mathrm{S}_{3}$ |  |
| -2 | 0 | 3 | 16 |
| $\mathrm{S}_{31}$ | $\mathrm{S}_{32}$ | $\mathrm{S}_{33}$ |  |
|  |  |  | 18 |

$k=1$

| 2 | $-4$ | -7 | 16 |
| :---: | :---: | :---: | :---: |
| 10 | 16 | 19 |  |
| 0 | 3 | 3 | 15 |
| 18 | 15 | 15 |  |
| -2 | 0 | 3 | 16 |
| 18 | 16 | 19 |  |
| 18 | 16 | 19 | 16 |

Based on step 6: $\mathbf{i}^{*}=2$
Based on step 7(c): $16 \leq Z^{B}$ and $\{10+30\} \geq D$, new $Z^{B}=16$.

$$
\mathrm{I}_{0}=\{2\}, \text { and } \mathrm{I}_{1}=\{1,3\}
$$

Based on step 8(b): $S_{1}^{1}=16, S_{2}^{1}=15$, and $S_{3}^{1}=16$.

$$
k=2
$$



Based on step 6: $\mathrm{i}^{*}=1$
Based on step 7(c): $18 \geq Z^{B}$, Stop.
The optimal objective value is 16 , and the optimal solution is $\left\{\mathrm{Y}_{1}=1, \mathrm{Y}_{2}=0\right.$, and $\left.\mathrm{Y}_{3}=1\right\}$. The heuristic stops in the second iteration since $\mathrm{Z}^{2}>\mathrm{Z}^{\mathrm{B}}$.

### 3.8. Chapter Summary

In this chapter, the framework for the supply chain management system for a singleproduct and multi-product supply chain management problems at the strategic and tactical planning levels were addressed. The problems are focused on selecting a set of operating
facilities within the supply chain. At first, all required data for model development, model characteristic, and the total systemwide costs within a supply chain network were defined. Next, two mixed integer linear programming problems, SCTFL and MCTFL, were developed and described.

To solve these two problems, heuristic methods based on decomposition technique were introduced. MCTFL problem was decomposed to SCTFL problem. SCTFL problem was decomposed to LP1 and LP2. To feasibly and effectively solve LP1 and LP2, Bender's decomposition concepts were used. A set of new heuristic methods to specifically solve Bender's master and sub problems was developed. The application of Vogel's Approximation Method (VAM), the affine-scaling method, and Cholesky factorization were utilized or modified to trace out the solution of Bender's subproblem.

Finally, a new method called BMO was introduced to find Bender's master solution. The method was established based on a penalty concept similar to VAM and Dynamic Programming methods. In all experimental problems, BMO method could yield an optimum solution within a short computational time.

## CHAPTER 4

## MODEL DEVELOPMENT FOR A PULL-BASED

## SUPPLY CHAIN SYSTEM

### 4.1. General Introduction

As mention in the previous chapters, in order to minimize a company's systemwide costs, all decisions along the supply chain need to be considered together at the same time. In this chapter SCTFL method from chapter 3 is applied to the pull-based supply chain system at a company operational level. Two heuristic procedures, one for a single-product and the other for multi-product aspects are then developed to determine the optimal customers' order filling, production plan, and inventory replenishment decisions. The studied supply chain system consists of two echelons, customers vs. distribution centers and distribution centers vs. manufacturing plants.

### 4.2. Generic Supply Chain Model

In this section, two generic supply chain models are first created. One deals with two-echelon case, which consists of plants, DCs, and customer locations. The other deals with a single echelon, which consists of either plants and DCs, or DCs and customers. The difference between these two models and their uses depends on how a company fulfills its customers' orders and the way the company replenishes its inventory. The first model represents the situation when there are not enough available stocks at the $D C$ level to respond to customers' orders. In this case the company needs to retrieve the ordered products from the plant level via DCs, to fulfill its customers' orders. Another situation is when the
company needs to replenish inventory when inventory drops below the safety stock level after filling customers' orders at the DC level. The second model represents a single echelon case between plants vs. DCs, and DCs vs. customers. This ideal single echelon model is used to represent a situation when there are enough on-hand inventories to fill customers' orders without retrieving products from the plant level. In this situation, products are allocated from DCs to each customer location, referred to here as Model 2.1. Another single echelon case deals with the situation when each DC needs to replenish its inventory from plants, referred to here as Model 2.2.

Model 1: Generic model for two echelon distribution system consisting of plants, DCs, and customer sites.


Figure 4.1 Two echelon distribution network

Model 2: Generic model for one echelon distribution system consisting.


Figure 4.2 One echelon distribution network.

## Model Assumptions:

1) The model deals with only one product at a time.
2) The model mainly focuses on integrating advanced production planning, inventory control, and distribution planning.
3) All plants can supply goods to all DCs.
4) All DCs can supply goods to all customers.
5) No plants are allowed to directly supply goods to customers.
6) The model focuses on Make to Order business.
7) Actual demands come from Sales and Marketing.
8) No transshipment between distribution centers.
9) No transshipment between plants.
10) All transshipments have a short lead-time.

The mathematical formulation of the problem throughout this chapter uses the following notation.
p index for commodities,
$i$ index for plants,
$j$ index for possible distribution center (DC) sites, or warehouse locations,
$k \quad$ index for customers or retailers,
P a set of commodities,
I a set of plants,
$J$ a set of warehouses or DC,
$K$ a set of customers,
$a_{i j}^{p} \quad$ the unit transportation cost of product p from plant i to warehouse j ,
$b_{i}^{p} \quad$ fixed setup costs for product $p$ at plant i,
$c_{j k}^{p} \quad$ the unit transportation cost of product $p$ from warehouse $j$ to customer/retailer k ,
$d_{j} \quad$ fixed processing costs at warehouse $\mathrm{j} / \mathrm{DC} \mathrm{j}$
$e_{j}^{p} \quad$ the unit throughput/processing cost of product $p$ at warehouse/DC $j$,
$f_{i}^{p}$ the unit procurement cost of product $p$ at plant $i$,
$D_{k}^{p} \quad$ demand of customer/retailer k of product p,
$U_{j}^{p}$ maximum inventory capacity of commudity $p$ at warehouse $j$,
$P_{i}^{p} \quad$ maximum production capacity of product p at plant i, quantity of product $p$ from plant $i$ to warehouse/DC $j$, quantity of product $p$ from warehouse/DC $j$ to customer/retailer k,
$y_{i}^{p} \quad$ a $0-1$ variable that becomes 1 if product $p$ is produced at plant $i$, and 0 otherwise.
$z_{j}^{P} \quad$ a $0-1$ variable that will be 1 if warehouse/DC j is used to fill customer orders, and 0 otherwise.

### 4.3. General Solution Concept and Techniques

In pull-base supply chain system, execution is initiated in response to customer order. At the time of execution of the system, demand is known with certainty. This means that production and distribution of products must accurately reflect the real demand. All processes in the customer order cycle, replenishment cycle, and manufacturing cycle are triggered by the arrival of a customer order. In this study, order fulfillment takes places from finish-product inventory if they are available. But in a situation where not enough stock may be on hand to fill customer requests, all processes in the replenishment and manufacturing cycle are started. Both replenishment and manufacturing cycles are thus parts of the customer order fulfillment process in the customer order cycle.

To effectively solve this complex problem, we first study all product movements within the system. There are four possible product movements or cases that may happen when sales orders are received from end customers within a specific time window. With the
superscript $p$ dropped from the parameters for the single product case, the following is the mixed integer linear programming model for all four cases.

## Case 1: To fill customer orders, product shipments from plants via DCs need to be

 performed, using Model 1.This deals with the case where there is not enough inventory at the right or optimal DC locations to directly satisfy customer orders.

$$
\begin{equation*}
\text { Minimize } \sum_{i=1}^{I} \sum_{j=1}^{J}\left(a_{i j}+f_{i}\right) x_{i j}+\sum_{i=1}^{I} b_{i} y_{i}+\sum_{j=1}^{J} \sum_{k=1}^{K}\left(c_{j k}+e_{j}\right) w_{j k}+\sum_{j=1}^{J} d_{j} z_{j} \tag{4.1}
\end{equation*}
$$

## Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k} \geq D_{k}, & \forall k \in K, \\
\sum_{k=1}^{K} w_{j k} \leq U_{j} z_{j}, & \forall j \in J, \\
\sum_{i=1}^{l} x_{i j}=\sum_{k=1}^{K} w_{j k}, & \forall j \in J, \\
\sum_{j=1}^{J} x_{y} \leq P_{i} y_{i}, & \forall i \in I, \\
x_{y} \geq 0, & \forall i \in I, j \in J, \\
w_{j k} \geq 0, & \forall j \in J, k \in K, \\
y_{i}, z, \in\{0,1\}, & \forall i \in I, j \in J, \tag{4.8}
\end{array}
$$

In this case, a company has a set of supply plants and distribution centers with fixed costs and capacities. The finished goods, for a set of customers with known demands, are to be supplied from plants via DCs/warehouses. The total transportation cost incurred include the cost of the products supplied from plants to DCs and from DCs to customers, along with fixed production and fixed DCs operation costs. The problem is to determine the policies on
distribution, inventory control, and production planning both at the plants and DCs levels that will minimize the total supply chain costs while satisfying all customer demands without violating the production and storage capacity constraints of the plants and DCs. Equation (4.1) is the problem objective function, to minimize the total supply chain cost. Constraint (4.2) requires that demand be satisfied and constraints (4.3) and (4.4) prevent upper bound violations of supplies for the warehouses and plants respectively. Constraints (4.5) balances in-flow products and out-flow products at warehouses. Constraints (4.3) and (4.5) also ensure that supplies can only be generated from a facility if and only if the facility exists.

## Case 2: Shipments from DCs to customers, using Model 2.1

In this case, it is assumed there are maximum stock levels at the time to fill the customers' orders at the DC level. The total maximum inventory is also greater than total customers' demands and all customers' order can be filled without generating production orders at the manufacturing plants.

Minimize $\sum_{j=1}^{J} \sum_{k=1}^{K}\left(c_{j k}+e_{j}\right) w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k} \geq D_{k}, & \forall k \in K, \\
\sum_{k=1}^{N} w_{j k} \leq I_{j} z_{j}, & \forall j \in J \\
w_{j k} \geq 0, & \forall j \in J, k \in K, \\
z_{j} \in\{0,1\}, & \forall j \in J, \tag{4.13}
\end{array}
$$

(Where $I_{j}$ is the maximum product inventory at $D C j$.)

## Case 3: Shipment from DCs to customers with consideration of on hand inventory level.

## at DCs using Model 2.1

In this case, there is enough on-hand inventories at the DC level to fill customer orders, again, without generating any production orders at the plant level. The on-hand stocks of all DCs are greater than all customers' orders.

Minimize $\sum_{j=1}^{J} \sum_{k=1}^{K}\left(c_{j k}+e_{j}\right) w_{j k}+\sum_{j=1}^{J} d_{j} z_{j}$
Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k} \geq D_{k}, & \forall k \in K, \\
\sum_{k=1}^{K} w_{j k} \leq\left(H_{j}-R_{j}\right) z_{j}, & \forall j \in J \\
w_{j k} \geq 0, & \forall j \in J, k \in K, \\
z_{j} \in\{0,1\}, & \forall j \in J, \tag{4.18}
\end{array}
$$

## Remark:

$$
\begin{equation*}
\sum_{j=1}^{J}\left(H_{j}-R_{j}\right) \geq \sum_{k=1}^{K} D_{k} \tag{4.19}
\end{equation*}
$$

Where $\quad H_{j}=$ On hand inventory of $\mathrm{DC}_{\mathrm{j}}$

$$
R_{j}=\text { Reorder point of } \mathrm{DC}_{\mathrm{j}}
$$

## Model 2.2

Minimize $\sum_{i=1}^{l} \sum_{j=1}^{J}\left(a_{i j}+f_{i}\right) x_{i j}+\sum_{i=1}^{l} b_{i} y_{i}$

Subject to
$\sum_{i=1}^{1} x_{i j} \geq D_{j}, \quad \forall j$,
$\sum_{j=1}^{J} x_{i j} \leq P_{i} y_{i}, \quad \forall i$,
$x_{i j} \geq 0, \quad \forall i \in I, j \in J$,
$y_{i} \in\{0,1\} \quad \forall i \in I$,

Replenishment takes place when demands at the $D C$ level, $D_{j}$ are known. $D_{j}$ can be found by the following conditions:

$$
\begin{align*}
& E_{j}=H_{j}-R_{j}-\sum_{k=1}^{K} w_{j k} \\
& D_{j}=\left\{\begin{array}{lll}
0 & \text { when } \quad E_{j} \geq 1 \\
I_{j}-E_{j} & \text { otherwise }
\end{array}\right. \tag{4.26}
\end{align*}
$$

Where $\quad E_{j}=$ decision variable

$$
\begin{aligned}
& H_{j}=\text { On hand inventory of } \mathrm{DC} \mathrm{C}_{\mathrm{j}} \\
& R_{j}=\text { Reorder point of } \mathrm{DC} C_{\mathrm{j}} \\
& I_{j}=\text { Maximum allowed inventory at } \mathrm{DC}_{\mathrm{j}}
\end{aligned}
$$

In this case, there are not enough on-hand inventories at the DC level, and production orders have to be generated at the plant level to satisfy customers' demand. It is worth to note that this case will be used only when the demands at DC level are known. According to the pull-based concept, the demand at DC level will be tied to the safety stock level or reorder point of each DC . Therefore, the model will not only fulfill the customers' orders but will at the same time replenish inventories at the DC level at the same time as well.

### 4.4. Solution Methodology for a Pull-based Supply Chain in a Single-product Problem (PSCSP)

It is obvious that execution in the customer order cycle, replenishment cycle, and manufacturing cycle depends on on-hand inventories and reorder points at the DC levels. If there are enough on-hand inventories and inventory replenishments are not required, only the solutions of case 3 may be necessary. However, if there are not enough on-hand inventories or inventory replenishments are required, the solutions of case 1 may be needed. Base on the mathematical models in previous section, it is intuitive that solving a single-echelon allocation problem like case 3 is much easier than a two-echelon allocation problem in case 1.

To effectively solve the problem, heuristic procedures are designed to investigate the outcome of a single-echelon problem first prior to dealing with a two-echelon problem. If the outcome of a single-echelon problem requires inventory replenishment or logistics cost is too expensive, the outcome of a two-echelon problem may be needed. The following is a heuristic procedure to determine the optimal customer order filling, inventory replenishment, and production decisions when a pull-based supply chain is applied for a single-product case. Notation:

Let $\quad S^{i} \quad=$ Optimal objective value for case $i, i=1,2,3$, and 4 .
$S^{*} \quad=$ Overall optimal objective value.
$W_{i}, Z_{i}=A$ set of solutions for case $i, i=1,2$, and 3.
$\mathrm{Xi}, \mathrm{Yi}=\mathrm{A}$ set of solutions for case $\mathrm{i}, \mathrm{i}=1$ and 4.
$\mathrm{W}^{*}, \mathrm{Z}^{*}, \mathrm{X}^{*}, \mathrm{Y}^{*}=$ Overall optimal solution.
$\mathrm{Cl}=$ Total distribution cost from DCs to customers.

## C2 = Total distribution cost from Plants to DCs.

## A Heuristic Procedure for PSCSP

Step 1: Solve case 2 for $S^{\mathbf{2}}$ and $\left(W_{2}, Z_{2}\right)$
Step 2: Solve case 3 for $S^{3}$ and $\left(W_{3}, Z_{3}\right)$
Step 3: Compare $S^{2}$ and $S^{3}$. If $S^{3}=S^{2}$, set $S^{*}=S^{3}, X^{*}$ and $Y^{*}=0, W^{*}=W_{3}$, and $Z^{*}=Z_{3}$, then stop. Otherwise go to next step.

Step 4: Solve case 1 for $S^{1}$ and $\left(X_{1}, Y_{1}, W_{1}\right.$, and $\left.Z_{1}\right)$.
Step 5: Compare $S^{1}$ and $S^{3}$. If $S^{3} \leq S^{1}$, set $S^{*}=S^{3}, X^{*}$ and $Y^{*}=0, W^{*}=W_{3}$, and $Z^{*}=Z_{3}$, then stop. Otherwise go to next step.

Step 6: Let $W_{4}=W_{1}$ and $Z_{4}=Z_{1}$, and Find $C 1$.
Step 7: Find all demands at Plant - DCs level, $\mathrm{D}_{\mathrm{j}}$, by using condition (4.26). Then solve case 4 for C 2 and $\left(\mathrm{X}_{4}, \mathrm{Y}_{4}\right)$.

Step 8: Find $S^{4}$, which is the total operation cost of $C 1$ and $C 2$. Then set $S^{*}=S^{4}$, $X^{*}=X_{4}$ and $Y^{*}=Y_{4}, W^{*}=W_{1}$, and $Z^{*}=Z_{1}$. The following figure 4.3 shows a pull-based heuristic procedure.


Figure 4.3 A pull-based heuristic procedure

### 4.5. Solution Methodology for a Pull-based Supply Chain in Multi-product Problem (PSCMP)

A pull-based supply chain in multi-product problem is used in making decisions involving multiple products. It is used in finding the best decision in fulfilling customers' orders, replenishing inventory, and establishing production orders and plans for the whole supply chain for all products. Like the single-product problem, there are known customers' demands for each product during each decision instance. There are also known throughput capacity or upper bounds for each product at each DC and plant. The possible candidate locations for the DCs and plants are also given. The problem is to determine which facility sites should be used in order to minimize the total supply chain costs when considering all product movements at the same time. A key element of this aggregate model is to determine
the candidates sites for the plants and DCs that should be selected. The following mixed integer programming problem represents the pull-based supply chain in multi-product. Remark: this model represents a day-by-day decision or operational decision level.

$$
\begin{align*}
\text { Minimize } & \sum_{p=1}^{P} \sum_{i=1}^{I} \sum_{j=1}^{J}\left(a_{i j}^{p}+f_{i}^{p}\right) x_{i j}^{p}+\sum_{p=1}^{P} \sum_{i=1}^{I} b_{i}^{p} y_{i}^{p}+\sum_{p=1}^{P} \sum_{j=1}^{J} \sum_{k=1}^{K}\left(c_{j k}^{p}+e_{j}^{p}\right) w_{j k}^{p} \\
& +\sum_{j=1}^{J} \sum_{k=1}^{K} d_{j} z_{j} \tag{4.25}
\end{align*}
$$

Subject to

$$
\begin{array}{rr}
\sum_{j=1}^{J} w_{j k}^{p} \geq D_{k}^{p}, & \forall k \in K, p \in P \\
\sum_{k=1}^{K} w_{j k}^{p} \leq U_{j}^{p} z_{j}, & \forall j \in J, p \in P \\
\sum_{i=1}^{I} x_{i j}^{p}=\sum_{k=1}^{K} w_{j k}^{p}, & \forall j \in J, p \in P, \\
\sum_{j=1}^{J} x_{i j}^{p} \leq P_{i}^{p} y_{i}^{p}, & \forall i \in I, p \in P, \\
x_{i j}^{p} \geq 0, & \forall i \in I, j \in J, p \in P \\
w_{j k}^{p} \geq 0, & \forall j \in J, k \in K, p \in P \\
y_{i}^{p}, z_{j} \in\{0,1\}, & \forall i \in I, j \in J, p \in P \tag{4.32}
\end{array}
$$

It is clear that the model is very much the same as MCTFL in section 3.6.1 of chapter 3, except that the fixed costs at plant level, $b_{i}^{p}$, is now defined based on each product. The fixed cost mainly deals with the manufacturing cost of each product at different plants. Notices that the establishment cost at plant level, which is defined in MCTFL, is not part of $b_{i}^{p}$, since the problem, now, deals with a decision in operational level or day-by-day decision level. Normally, the establishment cost at plant level happens in the strategic and
tactical level. This assumption is also true for the warehouse fixed cost, $d_{j}$. The warehouse fixed cost in operational level normally deals with the operating costs related to hiring/paying shipping and handling personnel and fee. This also is true at the plant level where hiring and paying for general labor takes place. So, this cost is not product specific like $b_{i}^{p}$ at plant level but one time charge whenever a particular warehouse is used to fill customer orders in a particular time period. For example, suppose the time period is weekly. This means that the warehouse fixed cost will represent a weekly fixed operating cost. This cost may include other costs such as material handling and shipping equipment costs if applicable.

As you see, PSCMP can be decomposed as PSCSP into P different problems with some modification to the last term of the objective function (4.25). Furthermore, in some situations, the transportation costs associated with the first and the third terms of the same objective function may also need to be modified if it happens that an incentive transportation rate is used to ship in large quantities. This kind of rate is widely used, especially in Less-Than-Truckload (LTL), and Truckload (TL) motor carrier business. It is used to encourage shippers to increase shipment size and allow carriers to better utilize the capacity of their equipment. With the consideration of incentive rates, the unit transportation cost $a_{i j}^{p}$ in the first term and $c_{j k}^{p}$ in the third term must be modified. Based on the nature of the problem and the complication of the transportation rate structure, instead of solving the problem directly, the problem is attacked as a PSCSP problem, solved one product at a time. Then in each iteration, all associated costs, previously mentioned, are updated. Figure 4.4 shows a heuristic for a pull-based supply chain of multi-product case.


Figure 4.4 A heuristic for a pull-based supply chain of multi-product case

The following is the heuristic procedure for PSCMP.
Step 1: Arrange the products in descending order based on the total sales amount.

- Let $P^{\prime}=$ a set of ranked products

Step 2: Let $p^{*}$ be the first product of set $P!$ Solve PSCSP.
$-\quad$ Obtain $Z_{p^{*}, w_{j k}^{p^{*}}, x_{i j}^{p^{*}}, y_{i}^{p^{*}} \text { and } z_{j}, ~(1)}$

- From $y_{i}^{p^{*}}, z_{j}$, and $w_{j k}^{p_{k}^{*}}$, now let $I^{*}=\{i\}, J^{*}=\{j\}$, and $K^{*}=\{k\}$, where $I^{*}, J^{*}$, and $K^{*}$ are sets of used plants, used DCs, and customer/retailer locations, respectively.

Step 3: Set $d_{j}=0$ for all $j \in J^{*}$ in equation (4.25).
Step 4: Update set $P^{\prime}=P^{\prime}-\left\{p^{*}\right\}$.

Step 5: Update $a_{i j}^{p}$ and $c_{j k}^{p}$, where $i \in I^{*}, j \in J^{*}, k \in K^{*}$, and $p \in P^{\prime}$.

- Subtract $\Delta$ from $a_{i j}^{p}$ or $c_{j k}^{p}$ where $\Delta$ is an incentive transportation rate. Remark: this step can be omitted if an incentive transportation rate is not applicable)

Step 6: Stop when $P^{\prime}=\{\varnothing\}$. Otherwise, Go to Step 2.

### 4.6 Chapter Summary

In this chapter, the framework for the pull-base supply chain management system for a single-product and multi-product supply chain management problems at the day-by-day or operational level was addressed. The problems are focused on determining the optimal customers' order filling, production plan, and inventory replenishment decisions. At first, two generic supply chain networks were defined. One represented a single echelon case and another represented a two-echelon case. Next, all possible product movements within the pull-based supply chain were described based on these two generic networks. Four mixed integer linear programming problems were used to represent all four possible product movements in a single product supply chain management problem.

To solve the single product problem, PSCSP, a heuristic method based on the idea of investigating the outcome of a single-echelon problem first prior to dealing with a twoechelon problem was introduced. The developed decomposition methods in the previous chapter were then used to find solutions. To solve the pull-based supply chain in a multiproduct problem, PSCMP, the problem was first decomposed as PSCSP into P different
problems. Then PSCSP was soived one problem or product at a time. In each iteration, all associated costs were updated and the heuristic process continued until the last product was considered.

## CHAPTER 5

## COMPUTATIONAL PERFORMANCE

### 5.1 Numerical Examples

In an effort to evaluate the performance of the solution methodology developed in Chapters 3 and 4, the following tasks were undertaken:

- Tested the supply chain network configuration with a single product, SCTFL, (on 10 example problems with a weekly average demand of 500 customers within the supply chain network of ten warehouses and four manufacturing plants) and compared the results with other two heuristic algorithms (Shortest Distance and Lowest Transportation methods).
- Tested the supply chain network configuration with multiple product, MCTFL, (on 10 example problems with a weekly average demand of 15 products from 500 customers within the supply chain network of ten warehouses and four manufacturing plants) and compared the results with other three heuristic algorithms (Shortest Distance, Lowest Transportation Cost, and Single Warehouse Preference methods).
- Tested the Pull-base Supply Chain method for a single product problem, PSCSP, (on 10 example problems with a weekly demand of a single product from 500 customers within the supply chain network of ten warehouses and four manufacturing plants. Each example problem consists of 13 weeks (one quarter)
of sales. In each week, there are 30 to 100 sales order items and compared the results with other two heuristic algorithms (Shortest Distance and Lowest Transportation Cost methods).
- Tested the Pull-base Supply Chain method for the multi product case, PSCMP, (on 10 example problems with a weekly demand of 15 products from 500 customers within the supply chain network of ten warehouses and four manufacturing plants. Each example problem consists of 13 weeks (one quarter) of sales. In each week, there are 550 to 1000 item-sales orders and compared the results with other three heuristic algorithm (Shortest Distance, Lowest Transportation Cost, and Single Warehouse Preference methods).

All testing data were randomly generated. Ten sets of problems were generated for SCTFL and MCTFL. Each set was comprised of an average weekly demand of 500 orders, which can be filled from ten different warehouses and four different plants. There is a single product in SCTFL and a total of 15 products in MCTFL To compare the PSCSP and PSCMP methods, another set of problems was generated that primarily involves week by week operations,. Each set of problems consists of 13 weeks (one quarter) of sales. In each quarter, there are about 700 sales order items in PSCSP and about 10000 sales order items in PSCMP). In each week, there are about 30 to 80 sales order items in PSCSP and about 750 sales order items in PSCMP. Again all customers' orders are filled from a network that involve ten different warehouses and four different plants. An example of customers' orders
is appended in Appendix A. Example results solved using heuristic procedures in this study are appended in Appendix B, and C.

### 5.2 Comparison of Results for SCTFL versus Other Two Heuristic Methods

Recall in chapter 3 that the SCTFL model developed was based on a single product strategy. In an effort to assess the effectiveness of the SCTFL method with the two heuristics, 10 sets of randomly generated problems with 500 customers were solved. In each set of problem, there is a single product involved. The reason for this comparison was to assess the difference in the solution quality and performance between the methods. This type of comparison is helpful in identifying the trade-offs between the methods. These problems were solved via the program developed in this study, on a Pentium III 800 personal computer. Table 5.1 to 5.3 shows the results of each method. Each column contain the following information:

- Cotumn 1 shows the problem number.
- Column 2 shows the total number of customers in the problem.
- Column 3 shows the total number of sales order items.
- Column 4 shows the total costs at warehouses and customers level, denoted as Cost 1.
- Column 5 shows the total costs at plants and warehouses level, denoted as Cost 2.
- Column 6 shows the total supply chain costs (Cost 1 plus Cost 2 ).
- Column 7 shows the number of actual warehouses used out of some possible number of warehouses.
- Column 8 shows the number of actual plants used out of some possible number of plants.
- Column 9 shows the total CPU time to arrive at the solution.

The main thing to note in looking at these results is that SCTFL heuristic method will always generate equal or less total number of used warehouses and plants than the other two methods. SCTFL heuristic method will also generate less total costs at both warehouses vs. customers and plants vs. warehouses level.

Table 5.1 Results of SCTFL problems using the shortest distance method

| Problem <br> $\#$ | \# of <br> Customers | \# of SO <br> items | Cost 1 | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 500 | 500 | 209,249 | 814,084 | $1,023.333$ | 10 | 4 | 5.24 |
| 2 | 500 | 500 | 224,974 | 553,514 | 778.488 | 10 | 4 | 4.09 |
| 3 | 500 | 500 | 281,095 | 919,264 | $1,200,359$ | 10 | 4 | 4.25 |
| 4 | 500 | 500 | 246,179 | 556,653 | 802,832 | 10 | 4 | 4.36 |
| 5 | 500 | 500 | 470,619 | $2,387,762$ | $2,858,381$ | 10 | 4 | 4.23 |
| 6 | 500 | 500 | 156,852 | 546,109 | 702,961 | 10 | 4 | 4.07 |
| 7 | 500 | 500 | 159,350 | 604,636 | 763,986 | 10 | 4 | 4.10 |
| 8 | 500 | 500 | 372,973 | 933,279 | $1,306,252$ | 10 | 4 | 4.25 |
| 9 | 500 | 500 | 239,200 | 570,328 | 809,528 | 10 | 4 | 5.29 |
| 10 | 500 | 500 | 269,179 | 512,698 | 781,877 | 10 | 4 | 4.21 |

Table 5.2 Results of SCTFL problems using the lowest transportation cost method

| Problem <br> $\#$ | \# of <br> Customers | \# of SO <br> items | Cost 1 | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 500 | 500 | 195,869 | 829,411 | $1,025,280$ | 10 | 4 | 5.30 |
| 2 | 500 | 500 | 211,681 | 558,196 | 769,877 | 10 | 4 | 4.07 |
| 3 | 500 | 500 | 261,497 | 974,511 | $1,236,008$ | 10 | 4 | 4.26 |
| 4 | 500 | 500 | 230,223 | 571,047 | 801,270 | 10 | 4 | $4.37 \mid$ |
| 5 | 500 | 500 | 436,439 | $2,392,518$ | $2,828,957$ | 10 | 4 | 4.20 |
| 6 | 500 | 500 | 148.119 | 552,121 | 700,240 | 10 | 4 | 4.06 |
| 7 | 500 | 500 | 151,881 | 611,941 | 763,822 | 10 | 4 | 4.10 |
| 8 | 500 | 500 | 349,045 | 962,532 | $1,311,577$ | 10 | 4 | 4.24 |
| 9 | 500 | 500 | 225,037 | 586,340 | 811,377 | 10 | 4 | 5.29 |
| 10 | 500 | 500 | 253,481 | 518.630 | 772,111 | 10 | 4 | 4.21 |

Table 5.3 Results of SCTFL problems using SCTFL heuristic method

| Problem <br> $\#$ | \# of <br> Customers | \# of SO <br> items | Cost 1 | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> time <br> (minutes) |
| :---: | :---: | :---: | :---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 500 | 500 | 192,591 | 734,502 | 927,093 | 6 | 3 | 63.23 |
| 2 | 500 | 500 | 215,793 | 330,805 | 546,598 | 4 | 3 | 45.05 |
| 3 | 500 | 500 | 287,026 | 652,137 | 939,163 | 6 | 4 | 61.21 |
| 4 | 500 | 500 | 232,911 | 433,971 | 666,882 | 6 | 3 | 75.35 |
| 5 | 500 | 500 | 466,027 | $1,626,888$ | $2,092,915$ | 5 | 2 | 55.15 |
| 6 | 500 | 500 | 131,377 | 448,323 | 579,700 | 4 | 3 | 49.09 |
| 7 | 500 | 500 | 140,337 | 342,568 | 482,905 | 6 | 3 | 49.19 |
| 8 | 500 | 500 | 381,618 | 653,749 | $1,035,367$ | 7 | 4 | 88.58 |
| 9 | 500 | 500 | 226,673 | 469,266 | 695,939 | 7 | 4 | 44.04 |
| 10 | 500 | 500 | 244,714 | 405,885 | 650,599 | 6 | 4 | 45.50 |

Table 5.4 shows a comparison of the results for SCTFL problems that were solved using the shortest distance, the lowest transportation cost, and the heuristic methods. The performance measurement employed in this comparison was quality of solutions. As indicated by this table, SCTFL heuristic solutions for all 10 tests outperformed that of the shortest distance and the lowest transportation cost methods. The shortest distance in the worst case came within $58.21 \%$ and in the best case came within $10.38 \%$ of the solution obtained by SCTFL heuristic. The lowest transportation cost in the worst case came within $\mathbf{5 8 . 1 7 \%}$ and in the best case came within $10.59 \%$ of solution obtained by SCTFL heuristic. However, in all cases the shortest distance and the lowest transportation cost methods outperformed SCTFL heuristic in the CPU time it took to find the best solution. $\overline{\mathrm{S} C T F L}$ heuristic in the worst case took 88.58 minutes and in the best case took 44.04 minutes to find the solution. While comparing between the shortest distance and the lowest transportation cost methods, there was not much difference in both the quality of solutions and the CPU time. Note that the percentage difference in solution equals ((Method II - Method I) $\div$ Method I) * $100 \%$.

Table 5.4 Comparison of SCTFL problems using shortest distance, lowest transportation cost, and the SCTFL heuristic methods

| Problem <br> $\#$ | Shortest <br> Distance | Lowest <br> Trans. Cost | SCTFL <br> Heuristic | \% Diff. in <br> Sol. <br> Shortest vs. <br> Lowest | \% Diff in Sol. <br> Shortest vs. <br> SCTFL | \% Diff <br> in Sol. <br> Lowest vs. <br> SCTFL |
| :---: | ---: | ---: | ---: | :---: | :---: | :---: |
| 1 | $1,023,333$ | $1,025,280$ | 927,093 | 0.10 | 10.38 | 10.59 |
| 2 | 778,488 | 769,877 | 546,598 | -1.10 | 42.42 | 40.85 |
| 3 | $1,200,359$ | $1,236,008$ | 939,163 | 2.88 | 27.81 | 31.61 |
| 4 | 802,832 | 801,270 | 666,882 | -0.19 | 20.39 | 20.15 |
| 5 | $2,858,381$ | $2,828,957$ | $2,092,915$ | -1.04 | 36.57 | 35.17 |
| 6 | 702,961 | 700,240 | 579,700 | -0.39 | 21.26 | 20.79 |
| 7 | 763,986 | 763,822 | 482,905 | -0.02 | 58.21 | 58.17 |
| 8 | $1,306,252$ | $1,311.577$ | $1,035,367$ | 0.41 | 26.16 | 26.68 |
| 9 | 809,528 | 811,377 | 695,939 | 0.23 | 16.32 | 16.59 |
| 10 | 781,877 | 772,111 | 650,599 | -1.26 | 20.18 | 18.68 |

Overall, the SCTFL heuristic outperformed the two other heuristics in the quality of solutions obtained while the two other heuristics dominated the SCTFL heuristic in the amount of CPU time required to solve the problems. From a practical standpoint, given the low cost availability of computers in our time, it is obvious that the cost savings obtained from using the SCTFL heuristics will more than pay for the cost of the computer time required in solving the problems. Therefore, in spite of the poor performance of the SCTFL heuristic in CPU time requirement relative to the other heuristics, it is still more beneficial to adopt the SCTFL heuristic under real life applications than to adopt any of the other two solution approaches presented in this study

### 5.3 Comparison of Results for MCTFL Versus Other Three Heuristic Methods

In an effort to see how well the MCTFL performed against other three heuristic methods, 10 sets of problems with 500 customers were solved. In each set of randomly generated problems, there were 15 products involved. The average weekly sales order items were randomly generated and ranged from one to fifteen products for each customer. In
each problem, on average there were 3,750 sales items ordered. The results of the 10 problems that were solved using the shortest distance, the lowest transportation cost, the single warehouse preference, and MCTFL heuristic methods are given in Tables 5.5, 5.6, 5.7, and 5.8. These tables contain the following information:

- Column 1 shows the problem number.
- Column 2 shows the total number of customers in the problem.
- Column 3 shows the total number of sales items ordered.
- Column 4 shows the total cost at the warehouse and customer interface level, denoted as Cost 1.
- Column 5 shows the total costs at the plant and warehouse interface level, denoted as Cost 2.
- Column 6 shows the total supply chain costs (Cost 1 plus Cost 2).
- Column 7 shows the number of actual warehouses used out of some possible number of warehouses.
- Column 8 shows the number of actual plants used out of some possible number of plants.
- Column 9 shows the total CPU time to arrive at the solution.

Table 5.5 Results of MCTFL problems using the shortest distance method

| Problem <br> $\#$ | \# of <br> Customers | \# of <br> SO <br> items | Cost l | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> (ime <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 500 | 3610 | $1,780,740$ | $6,286,225$ | $8,066,965$ | 10 | 4 | 40.17 |
| 2 | 500 | 3802 | $1,987,264$ | $6,889,144$ | $8,876,408$ | 10 | 4 | 42.47 |
| 3 | 500 | 3789 | $1,920,961$ | $6,726,362$ | $8,647,323$ | 10 | 4 | 42.27 |
| 4 | 500 | 3794 | $2,011,373$ | $7,021,158$ | $9,032,531$ | 10 | 4 | 41.30 |
| 5 | 500 | 3765 | $1,850,833$ | $6,449,736$ | $8,300,569$ | 10 | 4 | 42.33 |
| 6 | 500 | 3713 | $1,850,833$ | $6,576,087$ | $8,426,920$ | 10 | 4 | 41.50 |
| 7 | 500 | 3704 | $1,827,389$ | $6,497,490$ | $8,324,879$ | 10 | 4 | 41.52 |
| 8 | 500 | 3744 | $1,834,156$ | $6,533,978$ | $8,368,134$ | 10 | 4 | 41.57 |
| 9 | 500 | 3692 | $1,772,311$ | $6,329,314$ | $8,101,625$ | 10 | 4 | 40.43 |
| 10 | 500 | 3701 | $1,831,924$ | $6,477,249$ | $8,309,173$ | 10 | 4 | 41.05 |

The key thing to note is that in all of the problems, Cost 2 , which is the total cost at plants vs. warehouses level, is always greater than Cost 1 , which is the total cost at warehouses vs. customers level. This is because Cost 2 was not only included transportation costs as in Cost 1 but also included the product standard costs as defined in section 3.3 and

## 3.4 in Chapter 3.

Table 5.6 Results of MCTFL problems using the towest transportation cost method

| Problem <br> $\#$ | \# of <br> Customers | \# of <br> So <br> items | Cost 1 | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 500 | 3610 | 1.522 .454 | 6.026 .685 | $7.549,139$ | 10 | 4 | 39.12 |
| 2 | 500 | 3802 | $1,630,966$ | $6,451,210$ | $8,082.176$ | 10 | 4 | 40.27 |
| 3 | 500 | 3789 | $1.630,448$ | $6.463,799$ | 8.094 .247 | 10 | 4 | 39.27 |
| 4 | 500 | 3794 | $1,665,393$ | $6.570,241$ | $8.235,634$ | 10 | 4 | 39.22 |
| 5 | 500 | 3765 | $1,564,018$ | 6.185 .958 | $7.749,976$ | 10 | 4 | 39.48 |
| 6 | 500 | 3713 | $1,524,798$ | $6,229,876$ | $7.754,674$ | 10 | 4 | 38.48 |
| 7 | 500 | 3704 | $1,584.251$ | $6,337,849$ | 7.922 .100 | 10 | 4 | 39.17 |
| 8 | 500 | 3744 | $1,593,343$ | 6.312 .252 | $7.905,595$ | 10 | 4 | 39.44 |
| 9 | 500 | 3692 | $1,524.499$ | $6,072,466$ | $7.596,965$ | 10 | 4 | 38.33 |
| 10 | 500 | 3701 | $1,560.359$ | $6,180,429$ | $7.740,788$ | 10 | 4 | 38.50 |

Table 5.7 Results of MCTFL problems using the single warehouse preference method

| Problem <br> $\#$ | \# of <br> Customers | \# of <br> SO <br> items | Cost 1 | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 500 | 3610 | $1,617,755$ | $6,223,428$ | $7,841,183$ | 10 | 4 | 40.16 |
| 2 | 500 | 3802 | $1,788,158$ | $6,748,562$ | $8,536,720$ | 10 | 4 | 41.39 |
| 3 | 500 | 3789 | $1,739,169$ | $6,659,266$ | $8,398,435$ | 10 | 4 | 40.26 |
| 4 | 500 | 3794 | $1,798,202$ | $6,842,822$ | $8,641,024$ | 10 | 4 | 40.28 |
| 5 | 500 | 3765 | $1,677,567$ | $6,422,624$ | $8,100,191$ | 10 | 4 | 41.40 |
| 6 | 500 | 3713 | $1,662,846$ | $6,499,809$ | $8,162,655$ | 10 | 4 | 40.50 |
| 7 | 500 | 3704 | $1,640,484$ | $6,444,602$ | $8,085,086$ | 10 | 4 | 40.36 |
| 8 | 500 | 3744 | $1,659,982$ | $6,429,611$ | $8,089,593$ | 10 | 4 | 41.07 |
| 9 | 500 | 3692 | $1,615,331$ | $6,275,562$ | $7,890,893$ | 10 | 4 | 39.53 |
| 10 | 500 | 3701 | $1,668,252$ | $6,406,288$ | $8,074,540$ | 10 | 4 | 40.27 |

Table 5.8 Results of MCTFL problems using MCTFL heuristic method

| Problem <br> $\#$ | \# of <br> Customers | \# of <br> SO <br> items | Cost 1 | Cost 2 | Total Costs | \# of <br> WHs | \# of <br> Plants | CPU <br> time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 500 | 3610 | $1,451.419$ | $5,252,128$ | $6,703.547$ | 10 | 4 | 116.56 |
| 2 | 500 | 3802 | $1,523,395$ | $5,849,263$ | $7,372.658$ | 10 | 4 | 149.29 |
| 3 | 500 | 3789 | $1,513,672$ | $5,744,561$ | $7,258,233$ | 10 | 4 | 128.08 |
| 4 | 500 | 3794 | $1,581,236$ | $5,334,156$ | $6,915,392$ | 10 | 4 | 141.21 |
| 5 | 500 | 3765 | $1,510,999$ | $5,372,491$ | $6,883,490$ | 10 | 4 | 178.58 |
| 6 | 500 | 3713 | $1,479.166$ | 5.637 .848 | $7,117.014$ | 10 | 4 | 120.00 |
| 7 | 500 | 3704 | 1.481 .601 | $5,321,553$ | 6.803 .154 | 10 | 4 | 167.47 |
| 8 | 500 | 3744 | $1,520,652$ | $5,243,388$ | $6,764,040$ | 10 | 4 | 120.02 |
| 9 | 500 | 3692 | $1,478.400$ | 5.440 .108 | 6.918 .508 | 10 | 4 | 117.57 |
| 10 | 500 | 3701 | $1,511,526$ | $5,511,449$ | 7.022 .975 | 10 | 4 | 129.09 |

Table 5.9 and 5.10 shows a comparison of the results for MCTFL problems that were solved using the shortest distance, the lowest transportation cost, the single warehouse preference, and the heuristic methods. The performance measure employed in this comparison was quality of solutions. As indicated by these two tables and Figure 5.1, MCTFL heuristic solutions for all 10 tests problems outperformed that of the other three methods. The shortest distance in the worst case came within $30.61 \%$ and in the best case came within $17.10 \%$ of the solution obtained by MCTFL heuristic. The lowest
transportation cost in the worst case came within $19.09 \%$ and in the best case came within $8.96 \%$ of the solution obtained by MCTFL heuristic. The single warehouse preference in the worst case came within $24.95 \%$ and in the best case came within $14.69 \%$ of the solution obtained by MCTFL heuristic. However, in all cases the other three methods outperformed MCTFL heuristic in the CPU time it took to find the best solution. MCTFL heuristic in worst case took 178.58 minutes and in the best case took 116.56 minutes to find the solution. While comparing among the three methods, the shortest distance in the worst case came within $9.83 \%$ and in the best case came within $5.08 \%$ of solution obtained by the lowest transportation cost. The shortest distance in the worst case came within $4.53 \%$ and in the best case came within $2.47 \%$ of solution obtained by the single warehouse preference. The single warehouse preference in the worst case came within $5.62 \%$ and in the best case came within $2.06 \%$ of solution obtained by the lowest transportation cost. However, all the three methods solved the problems within 38 to 42 minutes. Note that the percentage difference in solution equals ((Method II - Method I) $\div$ Method I) * $100 \%$.

Table 5.9 Comparison of MCTFL problems using shortest distance, lowest transportation cost, single warehouse preference and MCTFL heuristic methods

| Problem <br> $\#$ | Shortest <br> Distance | Lowest <br> Trans. Cost | Single Wh. <br> Preference | MCTFL <br> Heuristic | \% Diff in <br> Sol. <br> Shortest <br> vs. <br> MCTFL | \% Diff in <br> Sol. <br> Lowest vs. <br> MCTFL | \%Diffin <br> Sol. Single <br> Wh. Pref <br> vs. <br> MCTFL |
| :---: | :---: | :---: | ---: | ---: | ---: | ---: | ---: |
| 1 | $8,066,965$ | $7,549,139$ | $7,841,183$ | $6,703,547$ | 20.34 | 12.61 | 16.97 |
| 2 | $8,876,408$ | $8,082,176$ | $8,536,720$ | $7,372,658$ | 20,40 | 9.62 | 15.79 |
| 3 | $8,647,323$ | $8,094,247$ | $8,398,435$ | $7,258,233$ | 19.14 | 11.52 | 15.71 |
| 4 | $9,032,531$ | $8,235,634$ | $8,641,024$ | $6,915,392$ | 30.61 | 19.09 | 24.95 |
| 5 | $8,300,569$ | $7,749,976$ | $8,100,191$ | $6,883,490$ | 20.59 | 12.59 | 17.68 |
| 6 | $8,426,920$ | $7,754,674$ | $8,162,655$ | $7,117,014$ | 18.41 | 8.96 | 14.69 |
| 7 | $8,324,879$ | $7,922,100$ | $8.085,086$ | $6,803,154$ | 22.37 | 16.45 | 18.84 |
| 8 | $8,368,134$ | $7,905,595$ | $8,089,593$ | $6.764,040$ | 23.72 | 16.88 | 19.60 |
| 9 | $8,101,625$ | $7,596,965$ | $7,890,893$ | $6,918,508$ | 17.10 | 9.81 | 14.05 |
| 10 | $8,309,173$ | $7,740,788$ | $8,074,540$ | $7,022,975$ | 18.31 | 10.22 | 14.97 |

Table 5.10 Comparison of MCTFL problems among shortest distance, lowest transportation cost, and single warehouse preference methods

| Problem <br> $\#$ | Shortest <br> Distance | Lowest <br> Trans. Cost | Single Wh. <br> Preference | \% Diff in <br> Sol. Shortest <br> vs. Lowest | \% Diff in <br> Sol. Shortest <br> vs. Single <br> Wh. Pref | \%Diff in <br> Sol. Single <br> Wh. Pref vs. <br> Lowest |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | $8,066,965$ | $7,549,139$ | $7,841,183$ | 6.86 | 2.88 | 3.87 |
| 2 | $8,876,408$ | $8,082,176$ | $8,536,720$ | 9.83 | 3.98 | 5.62 |
| 3 | $8,647,323$ | $8,094,247$ | $8,398,435$ | 6.83 | 2.96 | 3.76 |
| 4 | $9,032,531$ | $8,235,634$ | $8,641,024$ | 9.68 | 4.53 | 4.92 |
| 5 | $8,300,569$ | $7,749,976$ | $8,100,191$ | 7.10 | 2.47 | 4.52 |
| 6 | $8,426,920$ | $7,754,674$ | $8,162,655$ | 8.67 | 3.24 | 5.26 |
| 7 | $8,324,879$ | $7,922,100$ | $8,085,086$ | 5.08 | 2.97 | 2.06 |
| 8 | $8,368,134$ | $7,905,595$ | $8,089,593$ | 5.85 | 3.44 | 2.33 |
| 9 | $8,101,625$ | $7,596,965$ | $7,890,893$ | 6,64 | 2.67 | 3.87 |
| 10 | $8,309,173$ | $7,740,788$ | $8,074,540$ | 7.34 | 2.91 | 4.31 |



Figure 5.1 MCTFL total costs of 10 testing problems

Like in the previous comparisons, the quality of solution among the techniques was dominated by the MCTFL heuristic method while the solution time for the other three heuristics dominated the MCTFL heuristic. In other words, the three heuristics produced their best solutions in less time than the MCTFL heuristic. Again, as in the SCTFL case, if the quality of solution is the primary emphasis for decision making and computational time can be acquired at a reasonable cost, obviously, the MCTFL heuristic will be a preferred solution method. In today's industrial environment where computers are ubiquitous, the benefits of using the MCTFL heuristic over the three other heuristics will more than pay for the cost of computer time required to solve the problem.

### 5.4 Comparison of Results for PSCSP versus Other Two Heuristic Methods

So far, all tests performed were done based on facility location problem with either a single (SCTFL) or multiple products (MCTFL) on a long-term basis. In this section, the focus was shifted to weekly operations for a single product in what is known as the PSCSP problem. The operations mostly involved filling customers' orders, replenishing company's inventory, and manufacturing the products if needed. These decisions have huge impact on a company's total supply chain cost and ultimately affect later decisions over time. So, to determine how well this study's PSCSP heuristic would perform against other existing heuristic methodologies, 10 sets of simulated problems were used to perform the test. In each set of the problems, there were 13 weeks (quarter year) of customers' sales orders. In each week there were 30 to 100 sales orders. All sales orders were randomly generated from a pool of 500 customers. In order to reflect real life operation, all product inventory activities/movements were updated after each week. The results of the 10 problems that
were solved using the shortest distance method are as given in Tables 5.11 to 5.20. The results of the same 10 problems using the lowest transportation cost heuristic are as given in Tables 5.21 to 5.30 . The results of the same 10 problems using the PSCSP heuristic are as given in Table 5.31 to 5.40. These tables contain the following information:

- Column 1 shows the week identification number.
- Column 2 shows the total number of sales orders.
- Column 3 shows the total cost at warehouse and customer level, denoted as Cost 1.
- Column 4 shows the total cost at plant and warehouse level, denoted as Cost 2 .
- Column 5 shows the total supply chain cost (Cost 1 plus Cost 2).
- Column 6 shows the number of actual warehouses used out of some possible number of warehouses.
- Column 7 shows the number of actual plants used out of some possible number of plants.
- Column 8 shows the total CPU time taken to arrive at the solution.

The main thing to note is that in all of the problems, PSCSP heuristic method generated the results with less number of warehouses and plants.

Table 5.11 PSCSP resuits of test no. I using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 61 | 47.594 | 37,852 | 85,446 | 9 | 1 | 0.41 |
| 2 | 30 | 38,116 | 26.380 | 64,496 | 9 | 1 | 0.17 |
| 3 | 51 | 48.554 | 95.919 | 144.473 | 10 | 2 | 0.23 |
| 4 | 55 | 49,666 | 47,890 | 97,556 | 10 | 1 | 0.33 |
| 5 | 47 | 43,179 | 91,363 | 134,542 | 9 | 2 | 0.50 |
| 6 | 56 | 48,072 | 87,320 | 135,392 | 9 | 1 | 0.35 |
| 7 | 50 | 44,044 | 119,119 | 163,163 | 9 | 2 | 0.29 |
| 8 | 54 | 48,259 | 68,747 | 117,006 | 10 | 2 | 0.28 |
| 9 | 47 | 45.939 | 92.888 | 138,827 | 10 | 2 | 0.46 |
| 10 | 55 | 43.967 | 105.584 | 149,551 | 8 | 1 | 0.33 |
| 11 | 61 | 57.418 | 129,972 | 187,390 | 10 | 3 | 0.51 |
| 12 | 44 | 46.497 | 84.985 | 131.482 | 10 | 2 | 0.42 |
| 13 | 54 | 47,904 | 93,001 | 140,905 | 10 | 2 | 0.31 |

Table 5.12 PSCSP results of test no. 2 using the shortest distance method

| Week No.\# of <br> SO | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |  |
| :---: | :---: | ---: | ---: | ---: | :---: | :---: | :---: |
| 1 | 51 | 53,992 | 27.137 | 81,129 | 10 | 1 | 0.24 |
| 2 | 55 | 57,353 | 56,654 | 114,007 | 10 | 2 | 0.26 |
| 3 | 39 | 41,933 | 76,581 | 118,514 | 8 | 2 | 0.30 |
| 4 | 61 | 55,786 | 70,081 | 125,867 | 10 | 2 | 0.40 |
| 5 | 43 | 69,169 | 102,944 | 172.113 | 10 | 3 | 0.59 |
| 6 | 71 | 65,984 | 158,669 | 224,653 | 10 | 3 | 0.13 |
| 7 | 60 | 58,240 | 44,305 | 102.545 | 10 | 1 | 0.40 |
| 8 | 40 | 50.240 | 86,611 | 136,851 | 10 | 3 | 0.34 |
| 9 | 45 | 48.169 | 71,447 | 119,616 | 9 | 2 | 0.40 |
| 10 | 45 | 50,894 | 25,637 | 76.531 | 10 | 1 | 0.49 |
| 11 | 59 | 55,705 | 74,355 | 130,060 | 10 | 2 | 0.37 |
| 12 | 51 | 61,800 | 172.805 | 234,605 | 10 | 4 | 0.39 |
| 13 | 45 | 52.538 | 75,507 | 128.045 | 10 | 2 | 0.42 |

Table 5.13 PSCSP resuits of test no. 3 using the shortest distance method

| Week No. | \# of <br> SO | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 70 | 72.501 | 89.968 | 162.469 | 10 | 1 | 0.15 |
| 2 | 50 | 50.683 | 98.976 | 149,659 | 8 | 2 | 0.23 |
| 3 | 34 | 46,060 | 58,165 | 104,225 | 10 | 3 | 0.21 |
| 4 | 56 | 60,210 | 92,359 | 152,569 | 10 | 2 | 0.34 |
| 5 | 56 | 58,262 | 80,485 | 138,747 | 10 | 3 | 0.35 |
| 6 | 60 | 60,935 | 190,504 | 251,439 | 9 | 3 | 0.39 |
| 7 | 56 | 56.951 | 41,040 | 97,991 | 10 | 1 | 0.35 |
| 8 | 38 | 46,848 | 85,973 | 132,821 | 9 | 2 | 0.28 |
| 9 | 47 | 50,396 | 85.806 | 136,202 | 9 | 3 | 0.45 |
| 10 | 60 | 62,017 | 109,957 | 171.974 | 10 | 2 | 0.39 |
| 11 | 58 | 57.277 | 87,491 | 144,768 | 10 | 2 | 0.35 |
| 12 | 55 | 56,906 | 121.562 | 178.468 | 10 | 2 | 0.32 |
| 13 | 49 | 48.016 | 123,816 | 171,832 | 8 | 3 | 0.26 |

Table 5.14 PSCSP results of test no. 4 using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 66 | 70.849 | 48.611 | 119.460 | 10 | 1 | 0.15 |
| 2 | 36 | 49.229 | 60,169 | 109.398 | 10 | 2 | 0.25 |
| 3 | 40 | 59.935 | 77,969 | 137,904 | 10 | 2 | 0.47 |
| 4 | 63 | 55.460 | 79.470 | 134.930 | 9 | 1 | 0.43 |
| 5 | 54 | 53.205 | 84.807 | 138,012 | 10 | 3 | 0.32 |
| 6 | 63 | 71.828 | 188,894 | 260,722 | 10 | 3 | 0.53 |
| 7 | 66 | 60.439 | 67,038 | 127,477 | 10 | 2 | 0.12 |
| 8 | 54 | 57.800 | 44.431 | 102,231 | 10 | 1 | 0.27 |
| 9 | 47 | 50,884 | 114,514 | 165,398 | 9 | 3 | 0.43 |
| 10 | 73 | 60,652 | 96.061 | 156,713 | 9 | 2 | 0.14 |
| 11 | 52 | 53.53 i | 79.988 | 133.519 | 10 | 2 | 0.28 |
| 12 | 47 | 50,031 | 53,101 | 103.132 | 9 | 1 | 0.51 |
| 13 | 51 | 51,664 | 61,890 | 113.554 | 9 | 1 | 0.27 |

Table 5.15 PSCSP results of test no. 5 using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 58 | 71.675 | 107,785 | 179,460 | 10 | 1 | 0.36 |
| 2 | 36 | 55,254 | 106,237 | 161,491 | 10 | 3 | 0.22 |
| 3 | 51 | 67,756 | 169.818 | 237,574 | 10 | 2 | 0.24 |
| 4 | 57 | 67,332 | 161,227 | 228,559 | 9 | 3 | 0.36 |
| 5 | 61 | 75.230 | 170,038 | 245,268 | 10 | 3 | 0.39 |
| 6 | 52 | 84.765 | 196,605 | 281,370 | 10 | 2 | 0.41 |
| 7 | 60 | 72.422 | 180.129 | 252,551 | 10 | 4 | 0.39 |
| 8 | 46 | 62,408 | 87.798 | 150,206 | 10 | 2 | 0.44 |
| 9 | 41 | 60.628 | 97.166 | 157,794 | 10 | 3 | 0.33 |
| 10 | 56 | 69.738 | 220,652 | 290,390 | 10 | 3 | 0.33 |
| 11 | 54 | 81,288 | 165,388 | 246,676 | 10 | 2 | 0.44 |
| 12 | 54 | 66,237 | 167,473 | 233,710 | 9 | 3 | 0.32 |
| 13 | 63 | 90,486 | 218,139 | 308,625 | 10 | 2 | 0.52 |

Table 5.16 PSCSP results of test no. 6 using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | $\begin{aligned} & \hline \text { CPU Time } \\ & \text { (minutes) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 60 | 51.678 | 68.937 | 120.615 | 10 | 3 | 0.40 |
| 2 | 37 | 44.615 | 49.136 | 93,751 | 10 | 3 | 0.23 |
| 3 | 37 | 43.513 | 43.991 | 87,504 | 10 | 2 | 0.26 |
| 4 | 63 | 49.900 | 102.562 | 152.462 | 10 | 4 | 0.45 |
| 5 | 57 | 48.697 | 72.567 | 121.264 | 10 | 4 | 0.35 |
| 6 | 51 | 45,285 | 60,195 | 105,480 | 10 | 3 | 0.28 |
| 7 | 57 | 51.551 | 75.923 | 127,474 | 10 | 4 | 0.37 |
| 8 | 46 | 45,809 | 49.993 | 95,802 | 10 | 2 | 0.43 |
| 9 | 52 | 48,161 | 74.418 | 122.579 | 10 | 4 | 0.26 |
| 10 | 63 | 51.972 | 88,453 | 140,425 | 10 | 4 | 0.44 |
| 11 | 52 | 49.099 | 78.242 | 127.341 | 10 | 4 | 0.30 |
| 12 | 53 | 47,415 | 52.711 | 100.126 | 10 | 2 | 0.32 |
| 13 | 52 | 49,886 | 75.401 | 125,287 | 10 | 4 | 0.30 |

Table 5.17 PSCSP results of test no. 7 using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 55 | 49,730 | 69.168 | 118,898 | 10 | 3 | 0.45 |
| 2 | 44 | 45.964 | 61.535 | 107.499 | 10 | 4 | 0.35 |
| 3 | 40 | 50.501 | 88.385 | 138.886 | 10 | 4 | 0.45 |
| 4 | 59 | 45,998 | 90,877 | 136,875 | 9 | 3 | 0.39 |
| 5 | 54 | 48,769 | 86,681 | 135,450 | 10 | 3 | 0.31 |
| 6 | 74 | 51,963 | 105,964 | 157.927 | 10 | 4 | 0.16 |
| 7 | 60 | 51,051 | 85,051 | 136,102 | 10 | 4 | 0.42 |
| 8 | 43 | 47.234 | 70,618 | 117,852 | 10 | 3 | 0.38 |
| 9 | 36 | 42,234 | 38,711 | 80,945 | 10 | 2 | 0.26 |
| 10 | 50 | 48,510 | 82,755 | 131,265 | 10 | 4 | 0.29 |
| 11 | 52 | 46,577 | 53.501 | 100,078 | 10 | 2 | 0.30 |
| 12 | 64 | 48.897 | 91.513 | 140,410 | 10 | 4 | 0.13 |
| 13 | 50 | 47,963 | 84,885 | 132,848 | 10 | 3 | 0.27 |

Table 5.18 PSCSP results of test no. 8 using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 70 | 77.139 | 84.576 | 161,715 | 9 | 2 | 0.13 |
| 2 | 30 | 41.607 | 46.502 | 88,109 | 8 | 2 | 0.15 |
| 3 | 39 | 61,845 | 102.622 | 164,467 | 10 | 4 | 0.28 |
| 4 | 46 | 64.914 | 78.720 | 143,634 | 10 | 2 | 0.48 |
| 5 | 45 | 87,864 | 129,087 | 216,951 | 10 | 3 | 1.04 |
| 6 | 60 | 76,768 | 126,115 | 202.883 | 10 | 3 | 0.38 |
| 7 | 52 | 69,210 | 104.168 | 173,378 | 10 | 3 | 0.30 |
| 8 | 52 | 64.632 | 98.570 | 163.202 | 9 | 2 | 0.27 |
| 9 | 47 | 63.830 | 66.336 | 130,166 | 9 | 2 | 0.46 |
| 10 | 53 | 69.090 | 107.185 | 176,275 | 10 | 3 | 0.30 |
| 11 | 55 | 95.586 | 145.071 | 240.657 | 10 | 3 | 0.41 |
| 12 | 42 | 60.792 | 73.867 | 134.659 | 9 | 3 | 0.39 |
| 13 | 53 | 67.538 | 94.593 | 162,131 | 10 | 3 | 0.29 |

Table 5.19 PSCSP results of test no. 9 using the shortest distance method

| Week No. | \# of <br> SO | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minules) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 60 | 58.420 | 48,106 | 106,526 | 10 | 1 | 0.39 |
| 2 | 37 | 51.477 | 16.337 | 67,814 | 10 | 1 | 0.24 |
| 3 | 55 | 60,208 | 177,775 | 237,983 | 10 | 3 | 0.27 |
| 4 | 55 | 58,241 | 61,353 | 119,594 | 10 | 2 | 0.33 |
| 5 | 38 | 47.161 | 29,719 | 76,880 | 10 | 2 | 0.35 |
| 6 | 50 | 55,306 | 89,546 | 144,852 | 10 | 2 | 0.28 |
| 7 | 65 | 60,348 | 167,036 | 227,384 | 10 | 4 | 0.11 |
| 8 | 50 | 53,513 | 43,944 | 97,457 | 10 | 1 | 0.25 |
| 9 | 56 | 56,437 | 79.958 | 136,395 | 10 | 2 | 0.29 |
| 10 | 61 | 55.505 | 84.439 | 139.944 | 9 | 2 | 0.40 |
| 11 | 47 | 62.347 | 116,446 | 178,793 | 10 | 3 | 1.05 |
| 12 | 49 | 55.606 | 94.317 | 149,923 | 10 | 1 | 0.27 |
| 13 | 49 | 51.760 | 49.982 | 101,742 | 10 | 2 | 0.25 |

Table 5.20 PSCSP results of test no. 10 using the shortest distance method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 55 | 62.744 | 38.951 | 101.695 | 10 | 1 | 0.33 |
| 2 | 41 | 53.533 | 36.181 | 89,7.14 | 10 | 1 | 0.30 |
| 3 | 52 | 53.325 | 95.097 | 148.422 | 9 | 2 | 0.24 |
| 4 | 44 | 55.734 | 77,004 | 132.738 | 10 | 3 | 0.43 |
| 5 | 48 | 53.752 | 62.139 | 115.891 | 9 | 2 | 0.26 |
| 6 | 65 | 82.169 | 211,942 | 294,111 | 10 | 4 | 0.16 |
| 7 | 58 | 61.224 | 54.736 | 115,960 | 10 | 2 | 0.37 |
| 8 | 44 | 58.918 | 80.598 | 139,516 | 10 | 1 | 0.40 |
| 9 | 41 | 53.424 | 41.447 | 94,871 | 10 | 2 | 0.34 |
| 10 | 63 | 59.408 | 113.300 | 172,708 | 9 | 3 | 0.40 |
| 11 | 44 | 49,270 | 56.148 | 105.418 | 9 | 1 | 0.45 |
| 12 | 56 | 61,298 | 130.981 | 192.279 | 9 | 3 | 0.33 |
| 13 | 41 | 52,656 | 40,417 | 93.073 | 10 | 2 | 0.37 |

Table 5.21 PSCSP results of test no. 1 using the lowest transportation cost method

| Week No. | \# of <br> SO | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 61 | 50.715 | 30,030 | 80,745 | 10 | 1 | 0.40 |
| 2 | 30 | 41.942 | 31,722 | 73,664 | 10 | 1 | 0.17 |
| 3 | 51 | 47.235 | 48.631 | 95,866 | 10 | 1 | 0.24 |
| 4 | 55 | 48.668 | 90,839 | 139,507 | 10 | 2 | 0.33 |
| 5 | 47 | 46.227 | 111,663 | 157,890 | 10 | 2 | 0.50 |
| 6 | 56 | 48,796 | 94,928 | 143,724 | 10 | 2 | 0.34 |
| 7 | 50 | 46.959 | 71,917 | 118.876 | 10 | 2 | 0.28 |
| 8 | 54 | 47.057 | 66,399 | 113,456 | 10 | 2 | 0.29 |
| 9 | 47 | 45,214 | 114.432 | 159,646 | 10 | 2 | 0.46 |
| 10 | 55 | 46.785 | 137.750 | 184,535 | 9 | 3 | 0.33 |
| 11 | 61 | 56,389 | 86,955 | 143,344 | 10 | 2 | 0.51 |
| 12 | 44 | 41,608 | 93.553 | 135,161 | 9 | 1 | 0.42 |
| 13 | 54 | 43.167 | 52,062 | 95,229 | 9 | 1 | 0.31 |

Table 5.22 PSCSP results of test no. 2 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 51 | 50,360 | 21.422 | 71.782 | 9 | 1 | 0.29 |
| 2 | 55 | 55,612 | 79,382 | 134.994 | 10 | 2 | 0.26 |
| 3 | 39 | 44,977 | 52.523 | 97,500 | 9 | 1 | 0.30 |
| 4 | 61 | 53,931 | 72.227 | 126,158 | 10 | 2 | 0.40 |
| 5 | 43 | 63,405 | 98,433 | 161.838 | 10 | 3 | 0.55 |
| 6 | 71 | 63,583 | 114,189 | 177.772 | 10 | 2 | 0.14 |
| 7 | 60 | 56.690 | 93.902 | 150.592 | 10 | 3 | 0.39 |
| 8 | 40 | 49.242 | 71.571 | 120.813 | 10 | 2 | 0.35 |
| 9 | 45 | 51.208 | 63,456 | 114.664 | 10 | 2 | 0.40 |
| 10 | 45 | 50.239 | 106.492 | 156,731 | 10 | 2 | 0.49 |
| 11 | 59 | 54.258 | 46.766 | 101,024 | 10 | 1 | 0.37 |
| 12 | 51 | 61,152 | 88.262 | 149,414 | 10 | 3 | 0.40 |
| 13 | 45 | 47,798 | 62,059 | 109,857 | ) | 1 | 0.43 |

Table 5.23 PSCSP results of test no. 3 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 70 | 62.629 | 80,842 | 143,471 | 10 | 2 | 0.13 |
| 2 | 50 | 52.791 | 103.522 | 156,313 | 9 | 2 | 0.23 |
| 3 | 34 | 45.084 | 40.778 | 85,862 | 10 | 2 | 0.22 |
| 4 | 56 | 57.397 | 114,559 | 171,956 | 10 | 2 | 0.34 |
| 5 | 56 | 58,052 | 82,518 | 140,570 | 10 | 3 | 0.34 |
| 6 | 60 | 59.387 | 152,132 | 211,519 | 10 | 2 | 0.39 |
| 7 | 56 | 55,179 | 49,918 | 105,097 | 10 | 2 | 0.34 |
| 8 | 38 | 49,639 | 108,157 | 157,796 | 10 | 3 | 0.29 |
| 9 | 47 | 52,869 | 77,076 | 129,945 | 10 | 3 | 0.46 |
| 10 | 60 | 59,628 | 133.925 | 193,553 | 10 | 2 | 0.39 |
| 11 | 58 | 54,204 | 84,639 | 138,843 | 10 | 2 | 0.34 |
| 12 | 55 | 55,182 | 101,488 | 156,670 | 10 | 3 | 0.32 |
| 13 | 49 | 54,550 | 89,302 | 143,852 | 10 | 2 | 0.25 |

Table 5.24 PSCSP results of test no. 4 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 66 | 58.483 | 45.754 | 104.237 | 10 | I | 0.12 |
| 2 | 36 | 47.807 | 34,685 | 82.492 | 10 | 2 | 0.25 |
| 3 | 40 | 51,737 | 71,329 | 123.066 | 10 | 2 | 0.37 |
| 4 | 63 | 52,042 | 67.936 | 119.978 | 3 | 1 | 0.42 |
| 5 | 54 | 52,131 | 58,636 | 110.767 | 10 | 2 | 0.32 |
| 6 | 63 | 60,696 | 167,014 | 227,710 | 10 | 4 | 0.44 |
| 7 | 66 | 58,370 | 102,502 | 160.872 | 10 | 2 | 0.12 |
| 8 | 54 | 55,429 | 22,639 | 78.068 | 10 | 1 | 0.28 |
| 9 | 47 | 49.266 | 89,358 | 138,624 | 9 | 3 | 0.43 |
| 10 | 73 | 62.416 | 168,910 | 231,326 | 10 | 2 | 0.14 |
| 11 | 52 | 49,630 | 36.655 | 86,285 | 9 | 1 | 0.29 |
| 12 | 47 | 48,813 | 44,835 | 93,648 | 9 | 2 | 0.50 |
| 13 | 51 | 46,354 | 62,701 | 109,055 | 8 | 1 | 0.27 |

Table 5.25 PSCSP resuits of test no. 5 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { SO } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 58 | 68,874 | 98.629 | 167.503 | 10 | 2 | 0.36 |
| 2 | 36 | 49,578 | 149,003 | 198.581 | 9 | 3 | 0.23 |
| 3 | 51 | 61.864 | 136,337 | 198,201 | 9 | 2 | 0.24 |
| 4 | 57 | 69,700 | 146,804 | 216,504 | 10 | 2 | 0.35 |
| 5 | 61 | 71,948 | 192.842 | 264.790 | 10 | 4 | 0.40 |
| 6 | 52 | 83,907 | 187,702 | 271,609 | 10 | 2 | 0.41 |
| 7 | 60 | 68,276 | 167,728 | 236,004 | 10 | 4 | 0.39 |
| 8 | 46 | 60,714 | 109.283 | 169,997 | 10 | 2 | 0.43 |
| 9 | 41 | 57,361 | 113,196 | 170,557 | 10 | 3 | 0.33 |
| 10 | 56 | 66,482 | 212.046 | 278,528 | 10 | 3 | 0.33 |
| 11 | 54 | 78,658 | 185,032 | 263,690 | 10 | 3 | 0.43 |
| 12 | 54 | 63,706 | 125,117 | 188,823 | 9 | 2 | 0.31 |
| 13 | 63 | 88.619 | 270,235 | 358,854 | 10 | 4 | 0.51 |

Table 5.26 PSCSP results of test no. 6 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 60 | 50.061 | 75.742 | 125.803 | 10 | 4 | 0.39 |
| 2 | 37 | 40.140 | 44.399 | 84,539 | 9 | 3 | 0.23 |
| 3 | 37 | 38.938 | 53.818 | 92,756 | 9 | 4 | 0.26 |
| 4 | 63 | 49.092 | 90.102 | 139,194 | 10 | 3 | 0.45 |
| 5 | 57 | 47.871 | 76,085 | 123,956 | 10 | 4 | 0.35 |
| 6 | 51 | 44.924 | 59,477 | 104,401 | 10 | 3 | 0.29 |
| 7 | 57 | 49.791 | 76.319 | 126.110 | 10 | 4 | 0.37 |
| 8 | 46 | 45.142 | 45.174 | 90,316 | 10 | 2 | 0.43 |
| 9 | 52 | 47,860 | 79.719 | 127,579 | 10 | 4 | 0.26 |
| 10 | 63 | 50,062 | 90.364 | 140,426 | 10 | 4 | 0.43 |
| 11 | 52 | 48,174 | 69,290 | 117.464 | 10 | 3 | 0.3 |
| 12 | 53 | 46,330 | 67.142 | 113.472 | 10 | 4 | 0.32 |
| 13 | 52 | 48,493 | 64,768 | 113.261 | 10 | 3 | 0.29 |

Table 5.27 PSCSP results of test no. 7 using the lowest transportation cost method

| Week No. | \# of <br> SO | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 55 | 47,345 | 68,214 | 115.559 | 10 | 3 | 0.37 |
| 2 | 44 | 45.062 | 56,599 | 101,661 | 10 | 3 | 0.35 |
| 3 | 40 | 47.887 | 83,380 | 131,267 | 10 | 4 | 0.35 |
| 4 | 59 | 48,561 | 87,569 | 136,130 | 10 | 3 | 0.39 |
| 5 | 54 | 47.534 | 85,964 | 133.498 | 10 | 3 | 0.32 |
| 6 | 74 | 50,901 | 113,201 | 164,102 | 10 | 4 | 0.15 |
| 7 | 60 | 49,523 | 81,885 | 131,408 | 10 | 4 | 0.41 |
| 8 | 43 | 47,091 | 68,134 | 115,225 | 10 | 3 | 0.38 |
| 9 | 36 | 41,698 | 38,356 | 80,054 | 10 | 2 | 0.26 |
| 10 | 50 | 47,430 | 85,579 | 133,009 | 10 | 4 | 0.30 |
| 11 | 52 | 46,044 | 58,659 | 104,703 | 10 | 2 | 0.30 |
| 12 | 64 | 48,211 | 83,133 | 131,344 | 10 | 3 | 0.13 |
| 13 | 50 | 47,143 | 91,639 | 138,782 | 10 | 4 | 0.27 |

Table 5.28 PSCSP results of test no. 8 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 70 | 79,081 | 87.305 | 166.386 | 10 | 2 | 0.13 |
| 2 | 30 | 45,142 | 23.602 | 68,744 | 9 | 2 | 0.15 |
| 3 | 39 | 59,562 | 116.419 | 175.981 | 9 | 3 | 0.28 |
| 4 | 46 | 59,689 | 84.619 | 144.308 | 9 | 2 | 0.48 |
| 5 | 45 | 87,738 | 147,127 | 234,865 | 10 | 3 | 1.04 |
| 6 | 60 | 72.040 | 112,950 | 184,990 | 10 | 3 | 0.38 |
| 7 | 52 | 67.307 | 107,834 | 175,141 | 10 | 2 | 0.30 |
| 8 | 52 | 61.284 | 88.683 | 149.967 | 9 | 2 | 0.26 |
| 9 | 47 | 62,401 | 92,080 | 154.481 | 9 | 3 | 0.45 |
| 10 | 53 | 66,266 | 94,855 | 161,121 | 10 | 3 | 0.31 |
| 11 | 55 | 69,331 | 99.071 | 168.402 | 10 | 2 | 0.31 |
| 12 | 42 | 62,138 | 91.654 | 153,792 | 10 | 4 | 0.40 |
| 13 | 53 | 60,656 | 98,014 | 158.670 | 9 | 2 | 0.30 |

Table 5.29 PSCSP results of test no. 9 using the lowest transportation cost method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 60 | 56.868 | 40.911 | 97,779 | 10 | 1 | 0.39 |
| 2 | 37 | 50.449 | 48.579 | 99.028 | 10 | 2 | 0.25 |
| 3 | 55 | 58.864 | 129,953 | 188,817 | 10 | 2 | 0.27 |
| 4 | 55 | 56,048 | 93,048 | 149,096 | 10 | 2 | 0.33 |
| 5 | 38 | 46,648 | 19,306 | 65,954 | 10 | 1 | 0.35 |
| 6 | 50 | 54,307 | 93.521 | 147,828 | 10 | 1 | 0.28 |
| 7 | 65 | 58,634 | 113,825 | 172,459 | 10 | 4 | 0.12 |
| 8 | 50 | 51,900 | 85,997 | 137,897 | 10 | 2 | 0.25 |
| 9 | 56 | 55,732 | 103,169 | 158,901 | 10 | 1 | 0.29 |
| 10 | 61 | 55,556 | 40,138 | 95.694 | 10 | 2 | 0.40 |
| 11 | 47 | 55,191 | 136,755 | 191.946 | 10 | 3 | 0.55 |
| 12 | 49 | 49,723 | 56,671 | 106,394 | 9 | 2 | 0.27 |
| 13 | 49 | 50,122 | 65,620 | 115,742 | 10 | 2 | 0.25 |

Table 5.30 PSCSP results of test no. 10 using the lowest transportation cost method

| Week No. | \# of <br> So | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | ---: | ---: | ---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |
| 2 | 45 | 60,237 | 39,013 | 99,250 | 10 | 1 | 0.32 |
| 3 | 52 | 49,567 | 54,650 | 107,540 | 91,107 | 9 | 2 |
| 4 | 44 | 54,346 | 66,114 | 161,741 | 10 | 2 | 0.30 |
| 5 | 48 | 56,825 | 72,504 | 129,360 | 10 | 3 | 0.24 |
| 6 | 65 | 72,517 | 128,516 | 201,033 | 10 | 10 | 3 |
| 7 | 58 | 59,248 | 93,598 | 152,846 | 10 | 2 | 0.26 |
| 8 | 44 | 57,424 | 92,814 | 150,238 | 10 | 2 | 0.13 |
| 9 | 41 | 48,435 | 62,325 | 110,760 | 9 | 2 | 0.40 |
| 10 | 63 | 60,962 | 82,606 | 143,568 | 10 | 1 | 0.34 |
| 11 | 44 | 50,908 | 61,731 | 112,699 | 10 | 3 | 0.40 |
| 12 | 56 | 61,341 | 136,947 | 198,288 | 10 | 3 | 0.45 |
| 13 | 41 | 48,324 | 54,367 | 102,691 | 9 | 2 | 0.34 |

Table 5.31 PSCSP resuits of test no. 1 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 61 | 26,959 | 59.709 | 86,668 | 3 | 1 | 2.21 |
| 2 | 30 | 15,848 | 39.448 | 55,296 | 3 | 1 | 1.05 |
| 3 | 51 | 23,011 | 68,314 | 91,325 | 3 | 1 | 2.02 |
| 4 | 55 | 26,298 | 71,756 | 98,054 | 2 | 1 | 2.19 |
| 5 | 47 | 27.135 | 89,621 | 116,756 | 4 | 1 | 2.00 |
| 6 | 56 | 26.603 | 106,667 | 133,270 | 3 | 2 | 2.27 |
| 7 | 50 | 25,279 | 89,039 | 114,318 | 4 | 2 | 2.12 |
| 8 | 54 | 22.977 | 84,741 | 107.718 | 3 | 1 | 2.30 |
| 9 | 47 | 20,748 | 84,460 | 105,208 | 3 | 1 | 2.00 |
| 10 | 55 | 26,819 | 91,259 | 118.078 | 4 | 1 | 2.30 |
| 11 | 61 | 36,089 | 133,227 | 169,316 | 4 | 1 | 3.03 |
| 12 | 44 | 22,360 | 105,884 | 128,244 | 3 | 1 | 2.32 |
| 13 | 54 | 25,036 | 100,267 | 125,303 | 3 | 2 | 3.21 |

Table 5.32 PSCSP results of test no. 2 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { so } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | $\begin{aligned} & \hline \text { CPU Time } \\ & \text { (minutes) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 51 | 28.484 | 41,650 | 70.134 | 3 | 1 | 3.22 |
| 2 | 55 | 33,475 | 81.716 | 115.191 | 4 | 1 | 3.38 |
| 3 | 39 | 27.465 | 47,112 | 74.577 | 4 | 2 | 2.37 |
| 4 | 61 | 34,221 | 69.493 | 103.714 | 4 | 1 | 4.15 |
| 5 | 43 | 27,798 | 53.275 | 81.073 | 3 | 1 | 2.55 |
| 6 | 71 | 46.769 | 116.347 | 163.116 | 5 | 3 | 5.25 |
| 7 | 60 | 32,820 | 76,991 | 109.811 | 3 |  | 4.24 |
| 8 | 40 | 24,400 | 66,150 | 90.550 | 3 | 1 | 1.49 |
| 9 | 45 | 27.523 | 31.250 | 58.773 | 3 | 1 | 1.31 |
| 10 | 45 | 26.712 | 77.368 | 104.080 | 3 | 1 | 1.31 |
| 11 | 59 | 30.671 | 48.373 | 79.044 | 3 | I | 2.13 |
| 12 | 51 | 30.087 | 93.976 | 124,063 | 4 | 3 | 1.52 |
| 13 | 45 | 28.450 | 69.673 | 98.123 |  | 2 | 1.40 |

Table 5.33 PSCSP results of test no. 3 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 70 | 44.651 | 95.269 | 139.920 | 5 | 2 | 3.15 |
| 2 | 50 | 33,641 | 123,858 | 157,499 | 3 | 1 | 2.58 |
| 3 | 34 | 22,058 | 31,458 | 53,516 | 3 | 1 | 2.29 |
| 4 | 56 | 39,804 | 82,099 | 121,903 | 5 | 2 | 3.00 |
| 5 | 56 | 33,045 | 124,777 | 157.822 | 3 | 1 | 2.12 |
| 6 | 60 | 37,440 | 106,299 | 143.739 | 3 | 3 | 3.09 |
| 7 | 56 | 33.494 | 54,735 | 88,229 | 4 | 1 | 3.26 |
| 8 | 38 | 31,072 | 67,148 | 98.220 | 5 | 2 | 2.25 |
| 9 | 47 | 39,706 | 90,740 | 130,446 | 6 | 3 | 3.16 |
| 10 | 60 | 37,961 | 121,354 | 159,315 | 3 | 3 | 4.18 |
| 11 | 58 | 37.704 | 94,984 | 132,688 | 4 | 3 | 4.03 |
| 12 | 55 | 33,338 | 95,131 | 128,469 | 4 | 1 | 4.08 |
| 13 | 49 | 38.682 | 73,072 | 111,754 | 5 | 2 | 3.32 |

Table 5.34 PSCSP results of test no. 4 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 66 | 32.392 | 58,887 | 91.279 | 3 | 1 | 2.38 |
| 2 | 36 | 22.617 | 40.243 | 62.860 | 3 | 1 | 1.48 |
| 3 | 40 | 22.871 | 55,162 | 78,033 | 3 | 1 | 2.27 |
| 4 | 63 | 37,629 | 78,904 | 116,533 | 3 | 2 | 4.06 |
| 5 | 54 | 28,660 | 56,047 | 84,707 | 2 | 1 | 3.50 |
| 6 | 63 | 35,386 | 80,858 | 116,244 | 4 | 1 | 4.04 |
| 7 | 66 | 36,152 | 81.144 | 117,296 | 4 | 2 | 4.00 |
| 8 | 54 | 34.091 | 70,989 | 105.080 | 3 | 1 | 3.40 |
| 9 | 47 | 31,074 | 47.732 | 78,806 | 4 | 1 | 3.09 |
| 10 | 73 | 47,677 | 132.792 | 180.469 | 5 | 3 | 5.02 |
| 11 | 52 | 29,217 | 88.556 | 117.773 | 2 | 1 | 3.45 |
| 12 | 47 | 33,951 | 34,071 | 68,022 | 5 | 1 | 1.39 |
| 13 | 51 | 33,338 | 45,462 | 78,800 | 3 | 1 | 1.52 |

Table 5.35 PSCSP results of test no. 5 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 58 | 55.593 | 98.123 | 153,716 | 7 | 2 | 2.39 |
| 2 | 36 | 37.431 | 131.418 | 168,849 | 4 | 2 | 2.15 |
| 3 | 51 | 46,219 | 125,074 | 171,293 | 5 | 2 | 3.22 |
| 4 | 57 | 58,434 | 145,860 | 204,294 | 7 | 3 | 4.39 |
| 5 | 61 | 54,354 | 176,700 | 231.054 | 6 | 3 | 5.25 |
| 6 | 52 | 52.621 | 119,611 | 172,232 | 7 | 2 | 3.30 |
| 7 | 60 | 59,973 | 127,890 | 187,863 | 7 | 2 | 4.22 |
| 8 | 46 | 40,657 | 158,969 | 199,626 | 4 | 3 | 3.38 |
| 9 | 41 | 43,176 | 87,820 | 130,996 | 4 | 1 | 3.06 |
| 10 | 56 | 51,416 | 188,948 | 240,364 | 6 | 3 | 4.50 |
| 11 | 54 | 51,194 | 134,042 | 185,236 | 6 | 2 | 4.48 |
| 12 | 54 | 47,448 | 164,313 | 211,761 | 4 | 3 | 5.00 |
| 13 | 63 | 54,538 | 133,339 | 187,877 | 6 | 1 | 5.39 |

Table 5.36 PSCSP results of test no. 6 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 60 | 25.422 | 68.568 | 93.990 | 4 | 1 | 1.24 |
| 2 | 37 | 20.542 | 51.863 | 72.405 | 4 | 1 | 1.08 |
| 3 | 37 | 25.252 | 43,682 | 68,934 | 5 | 1 | 1.19 |
| 4 | 63 | 22,825 | 94,876 | 117,701 | 3 | 1 | 2.51 |
| 5 | 57 | 21,135 | 79.478 | 100,613 | 3 | 1 | 1.40 |
| 6 | 51 | 22,287 | 56,580 | 78,867 | 4 | 1 | 1.59 |
| 7 | 57 | 25.717 | 71.558 | 97.275 | 4 | 1 | 1.05 |
| 8 | 46 | 28.112 | 52.111 | 80.223 | 6 | 1 | 1.58 |
| 9 | 52 | 23,650 | 71,121 | 94.771 | 4 | 1 | 2.14 |
| 10 | 63 | 23,826 | 99,620 | 123,446 | 3 | 1 | 3.21 |
| 11 | 52 | 20,746 | 78.451 | 99.207 | 3 | 1 | 2.39 |
| 12 | 53 | 24,730 | 50.869 | 75,599 | 4 | 1 | 2.46 |
| 13 | 52 | 24.562 | 68,493 | 93,055 | 4 | 1 | 2.36 |

Table 5.37 PSCSP results of test no. 7 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 55 | 23.512 | 57.733 | 81,245 | 4 | 1 | 2.12 |
| 2 | 44 | 18.107 | 71,375 | 89,482 | 3 | 1 | 1.00 |
| 3 | 40 | 25,497 | 57.946 | 83,443 | 5 | 2 | 1.56 |
| 4 | 59 | 22,559 | 90,924 | 121,583 | 3 | 1 | 3.26 |
| 5 | 54 | 23.436 | 72,452 | 95,888 | 4 | 1 | 2.08 |
| 6 | 74 | 25,401 | 116,189 | 141,590 | 3 | 1 | 4.42 |
| 7 | 60 | 30,387 | 70,571 | 100,958 | 5 | 1 | 4.07 |
| 8 | 43 | 23,366 | 73,099 | 96,465 | 4 | 2 | 1.00 |
| 9 | 36 | 21,230 | 36,933 | 58,163 | 5 | 1 | 1.46 |
| 10 | 50 | 23,767 | 70.590 | 94,357 | 4 | 2 | 3.05 |
| 11 | 52 | 18.830 | 53,864 | 72,694 | 3 | 1 | 2.49 |
| 12 | 64 | 22,315 | 96,019 | 118,334 | 3 | 1 | 4.13 |
| 13 | 50 | 24.912 | 80,208 | 105,120 | 4 | 1 | 3.04 |

Table 5.38 PSCSP results of test no. 8 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { SO } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 70 | 62,115 | 98,758 | 160.873 | 6 | 2 | 4.02 |
| 2 | 30 | 27.516 | 29.289 | 56.805 | 4 | 1 | 1.29 |
| 3 | 39 | 45,124 | 76.608 | 121,732 | 5 | 2 | 2.21 |
| 4 | 46 | 42.337 | 67.615 | 109.952 | 4 | 1 | 3.04 |
| 5 | 45 | 44,704 | 101,168 | 145.872 | 5 | 2 | 2.45 |
| 6 | 60 | 55,460 | 115.011 | 170,471 | 6 | 3 | 5.01 |
| 7 | 52 | 59.459 | 111,228 | 170,687 | 6 | 3 | 4.05 |
| 8 | 52 | 49.054 | 87.254 | 136.308 | 5 | 3 | 4.13 |
| 9 | 47 | 47,670 | 77.390 | 125,060 | 5 | 2 | 3.24 |
| 10 | 53 | 47,171 | 93.124 | 140.295 | 3 | 2 | 3.59 |
| 11 | 55 | 51.571 | 92.744 | 144,315 | 5 | 2 | 3.51 |
| 12 | 42 | 46,257 | 95.122 | 141,379 | 5 | 3 | 3.14 |
| 13 | 53 | 45,174 | 76,826 | 122.000 | 4 | 3 | 3.59 |

Table 5.39 PSCSP results of test no. 9 using PSCSP heuristic method

| Week No. | $\begin{aligned} & \text { \# of } \\ & \text { So } \end{aligned}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 60 | 33.724 | 79,604 | 113.328 | 3 | 1 | 4.37 |
| 2 | 37 | 25,297 | 32.555 | 57,852 | 3 | 1 | 2.24 |
| 3 | 55 | 37,704 | 82,096 | 119,800 | 4 | 2 | 4.18 |
| 4 | 55 | 35,732 | 106,003 | 141.735 | 4 | 3 | 4.41 |
| 5 | 38 | 21,707 | 60,993 | 82,700 | 2 | 2 | 2.44 |
| 6 | 50 | 28,944 | 41,102 | 70,046 | 3 | 1 | 3.51 |
| 7 | 65 | 36,499 | 88,596 | 125,095 | 4 | 1 | 5.38 |
| 8 | 50 | 30,448 | 71,497 | 101,945 | 4 | 2 | 3.40 |
| 9 | 56 | 33,944 | 99,059 | 133,003 | 4 | 3 | 4.47 |
| 10 | 61 | 33,603 | 65,994 | 99,597 | 3 | 1 | 5.30 |
| 11 | 47 | 26,938 | 32,555 | 59,493 | 3 | 1 | 3.24 |
| 12 | 49 | 36,076 | 83,889 | 119.965 | 5 | 1 | 3.58 |
| 13 | 49 | 27,931 | 57,308 | 85,239 | 4 | 2 | 4.04 |

Table 5.40 results of test no. 10 using PSCSP heuristic method

| Week No. | \# of <br> SO | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 55 | 38,469 | 39,763 | 78,232 | 4 | 1 | 5.01 |
| 2 | 41 | 29,623 | 56,177 | 85.800 | 3 | 1 | 3.12 |
| 3 | 52 | 33,666 | 65,307 | 98,973 | 2 | 1 | 4.25 |
| 4 | 44 | 31,332 | 80.236 | 111.568 | 4 | 1 | 3.39 |
| 5 | 48 | 36,718 | 67.193 | 103.911 | 4 | 3 | 4.34 |
| 6 | 65 | 51,319 | 78.754 | 130.073 | 5 | 2 | 6.04 |
| 7 | 58 | 45,654 | 96.052 | 141.706 | 4 | 2 | 5.32 |
| 8 | 44 | 34.849 | 83.263 | 118,112 | 4 | 1 | 3.41 |
| 9 | 41 | 29,915 | 61.425 | 91,340 | 4 | 2 | 3.45 |
| 10 | 63 | 45,480 | 70,084 | 115.564 | 4 | 2 | 6.10 |
| 11 | 44 | 32,926 | 112.914 | 145.840 | 4 | 1 | 3.48 |
| 12 | 56 | 39,727 | 62,948 | 102.675 | 3 | 1 | 5.04 |
| 13 | 41 | 31,820 | 39,476 | 71.296 | 4 | 2 | 3.52 |

Table 5.41 shows a comparison of the results for PSCSP total supply chain costs over
13 weeks that were solved using all three methods. The performance measure employed in this comparison was quality of solutions measured in cumulative supply chain cost over a 13 week period. As indicated in the table, the PSCSP heuristic solutions for all 10 tests
problems outperformed the shortest distance and the lowest transportation cost methods.
The shortest distance method in the worst case came within $39.09 \%$ and in the best case came within $16.60 \%$ of the solution obtained by PSCSP heuristic. The lowest transportation cost method in the worst case came within $31.89 \%$ and in the best case came within $13.25 \%$ of solution obtained by PSCSP heuristic. However, in all cases the shortest distance method and the lowest transportation cost method outperformed PSCSP heuristic in terms of the CPU time required to find the best solution in each week. The PSCSP heuristic in the worst case took 6.10 minutes and in the best case took 3.12 minutes to find the solution (refer to Table 5.40). A comparison between the shortest distance method and the lowest transportation cost method shows that latter outperformed the former in nine out of the ten problems when the measure of performance is cost. There was not much difference in term of CPU time between these two methods. Note that the percentage difference in solution is computed according to the relationship ((Method II - Method I) $\div$ Method I) * $100 \%$.

Table 5.41 Comparison of the PSCSP weekly cumulative costs over 13 weeks using shortest distance, lowest transportation cost, and PSCSP heuristic methods

| Problem <br> $\#$ | Shortest <br> Distance | Lowest <br> Trans. Cost | PSCSP <br> Heuristic | \% Diff. in <br> Sol. <br> Shortest vs. <br> Lowest | \% Diff in Sol. <br> Shortest vs. <br> PSCSP | \% Diff in Sol. <br> Lowest vs. <br> PSCSP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $1,690,229$ | $1,641,643$ | $1,449,554$ | 2.96 | 16.60 | 13.25 |
| 2 | $1.764,536$ | $1,673,139$ | $1.272,249$ | 5.46 | 38.69 | 31.51 |
| 3 | $1,993,164$ | $1.935,447$ | $1,623,520$ | 2.98 | 22.77 | 19.21 |
| 4 | $1,802.450$ | $1,666,128$ | $1,295,902$ | 8.18 | 39.09 | 28.57 |
| 5 | $2,973,674$ | $2,983,641$ | $2.445,161$ | -0.33 | 21.61 | 22.02 |
| 6 | $1,520,110$ | $1.499,277$ | $1,196,086$ | 1.39 | 27.09 | 25.35 |
| 7 | $1,635,035$ | $1,616,742$ | $1,259,322$ | 1.13 | 29.83 | 28.38 |
| 8 | $2,158,227$ | $2,096,848$ | $1.745,749$ | 2.93 | 23.63 | 20.11 |
| 9 | $1,785,287$ | $1,727,535$ | $1,309,798$ | 3.34 | 36.30 | 31.89 |
| 10 | $1,796,396$ | $1,773,950$ | $1,395,090$ | 1.27 | 28.77 | 27.16 |

Table 5.42 shows the weekly cumulative cost of all three methods based on the results of test problem number 10 presented in Table $5.20,5.30$, and 5.40. This table is also representative of the other test results shown in Tables 5.21 - 5.39. From the results, there is a trend.

Table 5.42 The weekly cumulative cost of all three methods based on test no. 10

| Week No. | Shortest Distance | Lowest Trans. Cost | PSCSP Heuristic |
| :---: | ---: | ---: | ---: |
| 1 | 101,695 | 99,250 | 78,232 |
| 2 | 191,409 | 190,357 | 164,032 |
| 3 | 339,831 | 352,098 | 263,005 |
| 4 | 472,569 | 472.558 | 374,573 |
| 5 | 588,460 | 601,887 | 478,484 |
| 6 | 882,571 | 802.920 | 608,557 |
| 7 | 998,531 | 955,766 | 750,263 |
| 8 | $1,138,047$ | $1,106,004$ | 868,375 |
| 9 | $1,232,918$ | $1,216,764$ | 959,715 |
| 10 | $1,405,626$ | $1,360,332$ | $1,075,279$ |
| 11 | $1,703,323$ | $1,472,971$ | $1,221,119$ |
| 12 | $1,796,396$ | $1,671,259$ | $1,323,794$ |
| 13 |  | $1,773,950$ | $1,395,090$ |

Figure 5.2 provides a perspective on how the cumulative total costs for the pull-based supply chain system may vary over time based on the results presented in Table 5.42. The three curves shown on the figure represent the results of the three algorithms presented.

From Figure 5.2, it can be seen that the trend of the cumulative cost over the thirteen weeks are all similar except that the curve for the lowest transportation cost method and the shortest distance method are more closely aligned. In general, the lowest transportation cost method slightly produced better results than the shortest distance method. In fact, the two curves are almost parallel with a little gap between them starting from the first week. This means that as the number of weeks increases, the difference between the cumulative total cost between the two approaches also increased as one would expect. The percent difference in cumulative
cost between the two methods remained almost the same over time. On the other hand, when the cumulative cost trends of the three solution approaches are compared, the PSCSP curve has the smallest slope. The dominance of the PSCSP heuristic over its two rivals was evident by the second week. The gap in the quality of performance between the PSCSP heuristic and the shortest distance and the lowest transportation techniques grew over time. For an operational director or decision maker, the results mean that adopting PSCSP heuristic method to perform a pull-based supply chain system would improve the minimization of company supply chain cost and consequently, the overall system inventories. This result is intuitive.


Figure 5.2 Graph of result from table 5.42

### 5.5 Comparison of Results for PSCMP versus Other Two Heuristic Methods

Like in the previous section, the focus was on a week-by-week operation except that this time multiple product system known as PSCMP problem was investigated. These operations again mostly involved filling customers' orders, replenishing company's inventories, and manufacturing the products as needed. These decisions make a huge impact on the company's total supply chain cost and ultimately affect later decisions over time as well. So, to determine how well this study's PSCMP heuristic would perform against other existing heuristic methodologies, 10 sets of simulated problems were used to perform the test. For each set of problems, there were 13 weeks or one quarter of a year of customers' sales orders that were considered. Each week consists of 300 sales orders and each sale order was made up of 1 to 5 sales order items. On the average there were 750 sales order items in each week. Sales order items were randomly generated from a pool of 15 product lines. All sales orders in each problem were randomly generated from the pool of 500 customers. The total number of sales order items for 13 weeks in each problem ranged from 9,000 to 10,500 sales order items. Again, to reflect the real life operation as closely as possible, all product inventory activities/movements were updated after each week. The results of the 10 problems that were solved using the shortest distance method are as given in Tables 5.43 to 5.52 . The results of the same 10 problems using the lowest transportation cost method are as given in Tables 5.53 to 5.62. The results of the same 10 problems using the single warehouse preference method are as given in Tables 5.63 to 5.72 . Finally, the results of the same 10 problems using PSCMP heuristic are as given in Table 5.73 to 5.82. These tables contain the following information:

- Column 1 shows the week identification number.
- Column 2 shows the total number of sales orders.
- Column 3 shows the total cost at warehouse and customer interface level, denoted as Cost 1 .
- Column 4 shows the total cost at plant and warehouse interface level, denoted as Cost 2.
- Column 5 shows the total supply chain cost (Cost 1 plus Cost 2 ).
- Column 6 shows the number of actual warehouses used out of some possibie number of warehouses. .
- Column 7 shows the number of actual plants used out of some possible number of plants.
- Column 8 shows the total CPU time to arrive at the solution.

An interesting feature to note is that in all of the problems, PSCMP heuristic method satisfied the orders with less number of warehouses and plants compared to the of PSCSP model

Table 5.43 PSCMP results of test no. 1 using the shortest distance method

| Week | \# of | Cost l | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  | (minutes) |
| 1 | 738 | 384.304 | 727.396 | $1,111,700$ | 10 | 4 | 11.07 |
| 2 | 598 | 303,575 | 852,212 | $1,155,787$ | 10 | 4 | 6.30 |
| 3 | 639 | 339,541 | $1,108.610$ | $1,448,151$ | 10 | 4 | 8.06 |
| 4 | 899 | 480,431 | $1,725,543$ | $2,205,974$ | 10 | 4 | 23.53 |
| 5 | 678 | 350,541 | $1,104,040$ | $1,454,581$ | 10 | 4 | 9.07 |
| 6 | 786 | 404,155 | $1,577,603$ | $1,981,758$ | 10 | 4 | 14.32 |
| 7 | 849 | 462,192 | $1,310,412$ | $1,772,604$ | 10 | 4 | 21.01 |
| 8 | 847 | 490,925 | $1,511,590$ | $2,002,515$ | 10 | 4 | 20.59 |
| 9 | 694 | 388,654 | $1,458,634$ | $1,847,288$ | 10 | 4 | 9.46 |
| 10 | 799 | 402,826 | $1,498,800$ | $1,901,626$ | 10 | 4 | 17.03 |
| 11 | 681 | 325,795 | $1,175,941$ | $1,501,736$ | 10 | 4 | 9.05 |
| 12 | 784 | 405.385 | $1,446,763$ | $1,852.148$ | 10 | 4 | 14.47 |
| 13 | 810 | 394,974 | $1,246,174$ | $1,641,148$ | 10 | 4 | 16.12 |

Table 5.44 PSCMP results of test no. 2 using the shortest distance method

| Week <br> No. | \# of <br> SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 657 | 309,988 | 548.297 | 858,285 | 10 | 4 | 11.25 |
| 2 | 579 | 307,377 | 788,073 | 1,095,450 | 10 | 3 | 8.29 |
| 3 | 909 | 435,387 | 1,552,070 | 1,987,457 | 10 | 4 | 34.34 |
| 4 | 746 | 373,336 | 1,192.068 | 1,565,404 | 10 | 4 | 19.18 |
| 5 | 698 | 364,603 | 1,245,871 | 1,610,474 | 10 | 4 | 15.23 |
| 6 | 592 | 304.775 | 1,081.818 | 1,386,593 | 10 | 4 | 6.11 |
| 7 | 604 | 308,177 | 1,241,307 | 1,549.484 | 10 | 4 | 6.50 |
| 8 | 840 | 449.222 | 1.541.365 | 1,990,587 | 10 | 4 | 22.28 |
| 9 | 602 | 285.675 | 930.418 | 1.216 .093 | 10 | 4 | 6.06 |
| 10 | 733 | 377,595 | 1,485.844 | 1,863.439 | 10 | 4 | 11.52 |
| 11 | 854 | 432,459 | 1,520,110 | 1,952,569 | 10 | 4 | 21.48 |
| 12 | 657 | 353,621 | 922.946 | 1.276.567 | 10 | 4 | 8.40 |
| 13 | 634 | 370.794 | 1,362,158 | 1,732.952 | 10 | 4 | 8.01 |

Table 5.45 PSCMP results of test no. 3 using the shortest distance method

| Week | \# of |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
|  |  |  |  |  |  |  |  |
| Time |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| (minutes) |  |  |  |  |  |  |  |
| 1 | 817 | 394,444 | 756,061 | $1,150,505$ | 10 | 3 | 24.11 |
| 2 | 768 | 411,782 | $1,294,327$ | $1,706,109$ | 10 | 4 | 19.57 |
| 3 | 818 | 397,806 | $1,195,353$ | $1,593,159$ | 10 | 4 | 25.03 |
| 4 | 740 | 385,892 | $1,287,216$ | $1,673,108$ | 10 | 4 | 18.21 |
| 5 | 665 | 343,697 | $1,017,880$ | $1,361,577$ | 10 | 4 | 13.02 |
| 6 | 879 | 444,207 | $1,660,669$ | $2,104,876$ | 10 | 4 | 33.00 |
| 7 | 734 | 371,751 | $1,473,785$ | $1,845,536$ | 10 | 4 | 18.00 |
| 8 | 662 | 339,882 | 871,445 | $1,211,327$ | 10 | 4 | 13.34 |
| 9 | 701 | 406,081 | $1,248,314$ | $1,654,395$ | 10 | 4 | 17.26 |
| 10 | 603 | 309,837 | $1,225,503$ | $1,535,340$ | 10 | 4 | 12,41 |
| 11 | 879 | 309,392 | $1,091,574$ | $1,400,966$ | 10 | 4 | 9.16 |
| 12 | 648 | 321,287 | $1,127,248$ | $1,448,535$ | 10 | 4 | 9.30 |
| 13 | 702 | 366,261 | $1,230,204$ | $1,596,465$ | 10 | 4 | 13.57 |

Table 5.46 PSCMP results of test no. 4 using the shortest distance method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 857 | 414,760 | 825,877 | $1,240,637$ | 10 | 4 | 38.51 |
| 2 | 738 | 363,565 | $1,135,048$ | $1,498,613$ | 10 | 4 | 20.24 |
| 3 | 759 | 365,085 | $1,202,801$ | $1,567,886$ | 10 | 4 | 22.05 |
| 4 | 878 | 499,993 | $1,693,247$ | $2,193,240$ | 10 | 4 | 56.26 |
| 5 | 688 | 336,544 | $1,049,390$ | $1,385,934$ | 10 | 4 | 16.56 |
| 6 | 715 | 345,367 | $1,278,714$ | $1,624,081$ | 10 | 4 | 17.10 |
| 7 | 656 | 368,044 | $1,276,849$ | $1,644,893$ | 10 | 4 | 12.07 |
| 8 | 743 | 346,169 | $1,136,987$ | $1,483,156$ | 10 | 4 | 21.11 |
| 9 | 585 | 321,005 | $1,219,230$ | $1,540,235$ | 10 | 4 | 9.02 |
| 10 | 761 | 346,482 | $1,449,428$ | $1,795,910$ | 10 | 4 | 21.55 |
| 11 | 638 | 319,896 | $1,032,888$ | $1,352,784$ | 10 | 4 | 10.38 |
| 12 | 680 | 347,950 | 980,124 | $1,328,074$ | 10 | 4 | 15.43 |
| 13 | 715 | 343,274 | $1,346,295$ | $1,689,569$ | 10 | 4 | 19.01 |

Table 5.47 PSCMP results of test no. 5 using the shortest distance method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 617 | 320.058 | 488,925 | 808,983 | 10 | 3 | 11.17 |
| 2 | 706 | 388,707 | 1,185,046 | 1,573,753 | 10 | 4 | 21.52 |
| 3 | 720 | 408.318 | 1,183,354 | 1,591,672 | 10 | 4 | 23.33 |
| 4 | 872 | 438.909 | 1,638,428 | 2,077,337 | 10 | 4 | 4.41 |
| 5 | 613 | 318.872 | 988,519 | 1,307,391 | 10 | 4 | 11.10 |
| 6 | 763 | 404,714 | 1,469,066 | 1,873,780 | 10 | 4 | 26.14 |
| 7 | 704 | 363,399 | 1,229,451 | 1,592,850 | 10 | 4 | 20.05 |
| 8 | 744 | 369.611 | 1,136,939 | 1,506,550 | 10 | 4 | 25.48 |
| 9 | 735 | 372,263 | 1,343,600 | 1,715,863 | 10 | 4 | 24.21 |
| 10 | 617 | 335.978 | 1,263,592 | 1,599,570 | 10 | 4 | 12.44 |
| 11 | 848 | 394.540 | 1,224,974 | 1,619,514 | 10 | 4 | 4.14 |
| 12 | 777 | 423.845 | 1,532,188 | 1,956,033 | 10 | 4 | 29.24 |
| 13 | 722 | 372,956 | 1,310,686 | 1,683,642 | 10 | 4 | 20.09 |

Table 5.48 PSCMP results of test no. 6 using the shortest distance method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | $\begin{aligned} & \text { \# of Plants } \\ & 1 \end{aligned}$ | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 761 | 415,256 | 833,533 | 1.248.789 | 10 | 4 | 27.09 |
| 2 | 757 | 376,657 | 1,232,987 | 1.609,644 | 10 | 4 | 26.15 |
| 3 | 809 | 422,153 | 1,222.363 | 1.644.516 | 10 | 4 | 38.25 |
| 4 | 809 | 382,686 | 1,423,042 | 1,805,728 | 10 | 4 | 30.28 |
| 5 | 764 | 371,948 | 1,408,292 | 1.780 .240 | 10 | 4 | 27.36 |
| 6 | 739 | 395,164 | 1,341,290 | 1,736.454 | 10 | 4 | 23.43 |
| 7 | 880 | 481.642 | 1.513 .246 | 1.994,888 | 10 | 4 | 5.01 |
| 8 | 834 | 411,055 | 1,345,652 | 1,756.707 | 10 | 4 | 4.32 |
| 9 | 877 | 454.860 | 1,624.986 | 2.079.846 | 10 | 4 | 5.04 |
| 10 | 723 | 388,422 | 1.415 .883 | 1.804.305 | 10 | 4 | 21.19 |
| 11 | 665 | 320,368 | 971,967 | 1.292.335 | 10 | 4 | 15.51 |
| 12 | 892 | 530,664 | 1,812,240 | 2,342,904 | 10 | 4 | 5.38 |
| 13 | 804 | 390,408 | 1,248,950 | 1,639,358 | 10 | 4 | 32.25 |

Table 5.49 PSCMP results of test no. 7 using the shortest distance method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| (mine |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 827 | 443,485 | 761,439 | $1,204,924$ | 10 | 4 | 19.01 |
| 2 | 794 | 448,050 | $1,309,939$ | $1,757,989$ | 10 | 4 | 16.23 |
| 3 | 800 | 431,988 | $1,641,371$ | $2,073,359$ | 10 | 4 | 17.02 |
| 4 | 597 | 356,063 | $1,094,332$ | $1,450,395$ | 10 | 4 | 6.45 |
| 5 | 772 | 412,639 | $1,314,381$ | $1,727,020$ | 10 | 4 | 14.50 |
| 6 | 892 | 494,094 | $1,606,655$ | $2.100,749$ | 10 | 4 | 25.02 |
| 7 | 770 | 389,289 | $1,354,564$ | $1,743,853$ | 10 | 4 | 14.00 |
| 8 | 717 | 410,246 | $1,503,549$ | $1,913,795$ | 10 | 4 | 11.5 |
| 9 | 762 | 410,909 | $1,206,582$ | $1,617,491$ | 10 | 4 | 14.00 |
| 10 | 588 | 300,890 | 909,142 | $1,210,032$ | 10 | 4 | 6.03 |
| 11 | 710 | 359,965 | $1,361,100$ | $1,721,065$ | 10 | 4 | 11.01 |
| 12 | 741 | 384,358 | $1,385,620$ | $1,769,978$ | 10 | 4 | 12.30 |
| 13 | 681 | 349,570 | $1,040,240$ | $1,389,810$ | 10 | 4 | 9.16 |

Table 5.50 PSCMP results of test no. 8 using the shortest distance method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| (mine |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 700 | 378,381 | 546,410 | 924,791 | 10 | 3 | 15.45 |
| 2 | 775 | 400,163 | $1,354,690$ | $1,754,853$ | 10 | 4 | 20.37 |
| 3 | 795 | 463,319 | $1,365,765$ | $1,829,084$ | 10 | 4 | 25.20 |
| 4 | 850 | 405,286 | $1,388,712$ | $1,793,998$ | 10 | 4 | 29.25 |
| 5 | 652 | 328,791 | $1,085,240$ | $1,414,031$ | 10 | 4 | 11.32 |
| 6 | 848 | 471,687 | $1,708,107$ | $2,179,794$ | 10 | 4 | 29.37 |
| 7 | 770 | 411,219 | $1,401,870$ | $1,813,089$ | 10 | 4 | 20.26 |
| 8 | 771 | 399,827 | $1,322,627$ | $1,722,454$ | 10 | 4 | 21.06 |
| 9 | 723 | 381,346 | $1,378.517$ | $1,759.863$ | 10 | 4 | 16.32 |
| 10 | 868 | 422,764 | $1,662.321$ | $2,085,085$ | 10 | 4 | 33.16 |
| 11 | 837 | 463,422 | $1,500,592$ | $1,964,014$ | 10 | 4 | 29.36 |
| 12 | 698 | 399,789 | $1,141.053$ | $1,540,842$ | 10 | 4 | 15.35 |
| 13 | 734 | 365,507 | $1,164,067$ | $1,529,574$ | 10 | 4 | 15.57 |

Table 5.51 PSCMP results of test no. 9 using the shortest distance method

| Week No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 755 | 414,363 | 747,668 | 1,162,031 | 10 | 3 | 18.43 |
| 2 | 695 | 341.459 | 960,378 | 1,301,837 | 10 | 4 | 14.44 |
| 3 | 801 | 431,238 | 1,429,335 | 1.860.573 | 10 | 4 | 25.26 |
| 4 | 755 | 415,782 | 1.569,963 | 1.985,745 | 10 | 4 | 22.25 |
| 5 | 593 | 322,899 | 962,858 | 1,285,757 | 10 | 4 | 8.31 |
| 6 | 671 | 306,103 | 1,078,950 | 1,385,053 | 10 | 4 | 12.31 |
| 7 | 705 | 371,041 | 1,161,990 | 1,533,031 | 10 | 4 | 15.35 |
| 8 | 903 | 487,426 | 1,977,026 | 2,464,452 | 10 | 4 | 36.57 |
| 9 | 798 | 400.522 | 1,201,156 | 1,601,678 | 10 | 4 | 22.34 |
| 10 | 653 | 375,291 | 1.263,425 | 1,638,716 | 10 | 4 | 11.38 |
| 11 | 674 | 400,955 | 1,355,520 | 1,756,475 | 10 | 4 | 13.38 |
| 12 | 753 | 409.835 | 1.298,482 | 1,708,317 | 10 | 4 | 17.48 |
| 13 | 788 | 462,688 | 1,717.888 | 2,180,576 | 10 | 4 | 23.18 |

Table 5.52 PSCMP results of test no. 10 using the shortest distance method

| Week <br> No. | $\begin{gathered} \text { \# of } \\ \text { SO items } \end{gathered}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 628 | 327,529 | 528.889 | 856,418 | 10 | 4 | 15.24 |
| 2 | 767 | 426.154 | 1,241.692 | 1.667,846 | 10 | 3 | 23.29 |
| 3 | 656 | 347,461 | 980.115 | 1.327 .576 | 10 | 4 | 17.07 |
| 4 | 676 | 383.960 | 1,437,108 | 1.821.068 | 10 | 4 | 19.24 |
| 5 | 656 | 352.177 | 1,197.141 | 1.549 .318 | 10 | 4 | 16.21 |
| 6 | 733 | 371,774 | 1,211,338 | 1,583.112 | 10 | 4 | 20.34 |
| 7 | 680 | 362.457 | 1,108,192 | 1,470,649 | 10 | 4 | 18.06 |
| 8 | 784 | 395,577 | 1,481.264 | 1,876.841 | 10 | 4 | 24.08 |
| 9 | 698 | 349,741 | 1.169.717 | 1.519.458 | 10 | 4 | 18.49 |
| 10 | 791 | 447,707 | 1,582.142 | 2,029,849 | 10 | 4 | 26.46 |
| 11 | 621 | 343.002 | 1,089.820 | 1.432,822 | 10 | 4 | 15.18 |
| 12 | 604 | 329,895 | 1.049.839 | 1.379,734 | 10 | 3 | 14.57 |
| 13 | 716 | 369.772 | 1.373.794 | 1.743 .566 | 10 | 4 | 19.51 |

Tabie 5.53 PSCMP results of test no. I using the lowest transportation cost method

| Week No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 738 | 340,837 | 727,658 | 1,068,495 | 10 | 4 | 11.12 |
| 2 | 598 | 269,380 | 777,603 | 1.046,983 | 10 | 4 | 6.16 |
| 3 | 639 | 303,816 | 1,047,989 | 1,351.805 | 10 | 4 | 7.27 |
| 4 | 899 | 429.629 | 1,728,408 | 2,158,037 | 10 | 4 | 22.18 |
| 5 | 678 | 313,191 | 1,041,390 | 1,354,581 | 10 | 4 | 8.46 |
| 6 | 786 | 363,258 | 1,424,833 | 1,788.091 | 10 | 4 | 14.06 |
| 7 | 849 | 386,512 | 1,315,001 | 1,701,513 | 10 | 4 | 19.49 |
| 8 | 847 | 406.913 | 1,498,199 | 1,905.112 | 10 | 4 | 19.16 |
| 9 | 694 | 336.229 | 1,299,594 | 1,635,823 | 10 | 4 | 9.16 |
| 10 | 799 | 356,785 | 1,426,115 | 1,782,900 | 10 | 4 | 16.09 |
| 11 | 681 | 306,373 | 1,074,908 | 1,381,281 | 10 | 4 | 9.01 |
| 12 | 784 | 359,449 | 1,411,303 | 1,770,752 | 10 | 4 | 14.13 |
| 13 | 810 | 355,866 | 1,439,401 | 1,795,267 | 10 | 4 | 15.45 |

Table 5.54 PSCMP results of test no. 2 using the lowest transportation cost method

| Week <br> No. | \# of <br> SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 657 | 285,554 | 973,903 | 1,259.457 | 10 | 4 | 10.01 |
| 2 | 579 | 269,016 | 854,034 | 1,123,050 | 10 | 4 | 7.47 |
| 3 | 909 | 392,481 | 1.728.930 | 2,121,411 | 10 | 4 | 33.27 |
| 4 | 746 | 341.471 | 1,392.894 | 1,734,365 | 10 | 4 | 18.17 |
| 5 | 698 | 332.487 | 1.182.348 | 1,514,835 | 10 | 4 | 14.53 |
| 6 | 592 | 266.283 | 1,145.004 | 1.411 .287 | 10 | 4 | 8.16 |
| 7 | 604 | 282.408 | 959.540 | 1.241.948 | 10 | 4 | 9.06 |
| 8 | 840 | 370,808 | 1.436.477 | 1,807,285 | 10 | 4 | 29.18 |
| 9 | 602 | 262,379 | 899.613 | 1.161.992 | 10 | 4 | 8.23 |
| 10 | 733 | 333.128 | 1,480,353 | 1,813,481 | 10 | 4 | 16.26 |
| 11 | 854 | 379,325 | 1.185.393 | 1.564,718 | 10 | 4 | 28.30 |
| 12 | 657 | 305.894 | 1,113,893 | 1,419.787 | 10 | 4 | 12.05 |
| 13 | 634 | 312.618 | 1,106.016 | 1,418,634 | 10 | 4 | 10.04 |

Table 5.55 PSCMP results of test no. 3 using the lowest transportation cost method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | ---: | ---: | ---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  | (minutes) |
| 1 | 817 | 361,119 | 738,925 | $1,100,044$ | 10 | 3 | 23.36 |
| 2 | 768 | 346.515 | $1,160,099$ | $1,506,614$ | 10 | 4 | 18.16 |
| 3 | 818 | 346.893 | $1,315,348$ | $1,662,241$ | 10 | 4 | 24.15 |
| 4 | 740 | 333.288 | $1,190,869$ | $1,524,157$ | 10 | 4 | 17.31 |
| 5 | 665 | 310,978 | 932,454 | $1,243,432$ | 10 | 4 | 11.55 |
| 6 | 879 | 389.606 | $1,726,930$ | $2,116,536$ | 10 | 4 | 31.32 |
| 7 | 734 | 318,444 | $1,073,701$ | $1,392,145$ | 10 | 4 | 16.06 |
| 8 | 662 | 304,764 | $1,072,547$ | $1,377,311$ | 10 | 4 | 12.29 |
| 9 | 701 | 338.831 | $1,304,309$ | $1,643,140$ | 10 | 4 | 15.15 |
| 10 | 603 | 285,673 | 978,144 | $1,263,817$ | 10 | 4 | 9.04 |
| 11 | 879 | 394,455 | $1,648,393$ | $2,042,848$ | 10 | 4 | 29.32 |
| 12 | 648 | 290,310 | 928.219 | $1,218.529$ | 10 | 4 | 9.51 |
| 13 | 702 | 322,980 | $1,272,067$ | $1,595,047$ | 10 | 4 | 14.05 |

Table 5.56 PSCMP results of test no. 4 using the lowest transportation cost method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 857 | 385,062 | 819,975 | 1,205,037 | 10 | 4 | 38.24 |
| 2 | 738 | 310,689 | 969,259 | 1,279,948 | 10 | 3 | 18.27 |
| 3 | 759 | 336,464 | 1,380.447 | 1,716.911 | 10 | 4 | 21.45 |
| 4 | 878 | 404,403 | 1,412.451 | 1.816,854 | 10 | 4 | 47.27 |
| 5 | 688 | 300,384 | 1.040 .984 | 1.341.368 | 10 | 4 | 15.32 |
| 6 | 715 | 308,711 | 1,208.538 | 1.517.249 | 10 | 4 | 15.55 |
| 7 | 656 | 308,100 | 1.110 .016 | 1,418,116 | 10 | 3 | 10.54 |
| 8 | 743 | 321,027 | 1,341,052 | 1,662,079 | 10 | 4 | 20.59 |
| 9 | 585 | 278.571 | 1.076 .589 | 1.355,160 | 10 | 4 | 8.35 |
| 10 | 761 | 322,035 | 1,359.305 | 1,681,340 | 10 | 4 | 22.14 |
| 11 | 638 | 288,265 | 949,504 | 1,237,769 | 10 | 4 | 10.27 |
| 12 | 680 | 303,225 | 1,047,118 | 1,350,343 | 10 | 4 | 15.01 |
| 13 | 715 | 311,721 | 1.306,078 | 1,617,799 | 10 | 4 | 19.05 |

Table 5.57 PSCMP results of test no. 5 using the lowest transportation cost method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  | (minutes) |
| 1 | 617 | 287,093 | $1,029,199$ | $1,316,292$ | 10 | 4 | 9.01 |
| 2 | 706 | 323,785 | $1,382,677$ | $1,706,462$ | 10 | 4 | 18.24 |
| 3 | 720 | 336,641 | $1,125,705$ | $1,462,346$ | 10 | 4 | 19.00 |
| 4 | 872 | 388,759 | $1,613,103$ | $2,001,862$ | 10 | 4 | 4.30 |
| 5 | 613 | 278,398 | 962,397 | $1,240,795$ | 10 | 4 | 9.20 |
| 6 | 763 | 364,069 | $1,498,913$ | $1,862,982$ | 10 | 4 | 22.43 |
| 7 | 704 | 327,239 | $1,158,168$ | $1,485,407$ | 10 | 4 | 18.34 |
| 8 | 744 | 323,450 | $1,295,801$ | $1,619,251$ | 10 | 4 | 23.54 |
| 9 | 735 | 337,949 | $1,185,510$ | $1,523,459$ | 10 | 4 | 23.05 |
| 10 | 617 | 286,188 | 976,309 | $1,262,497$ | 10 | 4 | 11.21 |
| 11 | 848 | 372,630 | $1,553,227$ | $1,925,857$ | 10 | 4 | 4.13 |
| 12 | 777 | 368,652 | $1,232,624$ | $1,601.276$ | 10 | 4 | 27.49 |
| 13 | 722 | 339,894 | $1,144,243$ | $1,484,137$ | 10 | 4 | 19.40 |

Table 5.58 PSCMP results of test no. 6 using the lowest transportation cost method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 761 | 353,562 | 618,152 | 971,714 | 10 | 3 | 22.35 |
| 2 | 757 | 346,298 | 1,232,707 | 1.579,005 | 10 | 4 | 25.54 |
| 3 | 809 | 378,002 | 1.237 .721 | 1.615 .723 | 10 | 3 | 36.45 |
| 4 | 809 | 351.557 | 1,508.076 | 1,859,633 | 10 | 4 | 30.12 |
| 5 | 764 | 331,588 | 1,167,936 | 1,499,524 | 10 | 4 | 27.14 |
| 6 | 739 | 346,653 | 1,307.439 | 1,654.092 | 10 | 4 | 22.01 |
| 7 | 880 | 401.512 | 1,367.586 | 1.769,098 | 10 | 4 | 4.43 |
| 8 | 834 | 369,050 | 1,567.492 | 1,936,542 | 10 | 4 | 4.20 |
| 9 | 877 | 385,066 | 1,261,281 | 1,646,347 | 10 | 4 | 4.40 |
| 10 | 723 | 341,191 | 1,375.786 | 1,716.977 | 10 | 4 | 20.04 |
| 11 | 665 | 300,331 | 1,072.601 | 1.372.932 | 10 | 4 | 16.03 |
| 12 | 892 | 443,219 | 1.801 .657 | 2,244.876 | 10 | 4 | 5.11 |
| 13 | 804 | 348,478 | 1,140.175 | 1,488,653 | 10 | 4 | 30.38 |

Table 5.59 PSCMP results of test no. 7 using the lowest transportation cost method

| Week | \# of | Cost l | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  |  |
| (minutes) |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 827 | 374,327 | 728,467 | $1,102,794$ | 10 | 4 | 17.16 |
| 2 | 794 | 368,668 | $1,197,260$ | $1,565,928$ | 10 | 4 | 15.11 |
| 3 | 800 | 370,879 | $1,523,842$ | $1,894,721$ | 10 | 4 | 16.48 |
| 4 | 597 | 294,576 | $1,008,051$ | $1,302,627$ | 10 | 4 | 6.41 |
| 5 | 772 | 364,890 | $1,135,684$ | $1,500,574$ | 10 | 4 | 14.55 |
| 6 | 892 | 415,162 | $1,546,421$ | $1,961,583$ | 10 | 4 | 24.54 |
| 7 | 770 | 351,041 | $1,274,976$ | $1,626,017$ | 10 | 4 | 13.24 |
| 8 | 717 | 339,709 | $1,350,009$ | $1,689,718$ | 10 | 4 | 11.14 |
| 9 | 762 | 376,030 | $1,246,836$ | $1,622,866$ | 10 | 4 | 13.52 |
| 10 | 588 | 252,400 | 946,398 | $1,198,798$ | 10 | 4 | 6.01 |
| 11 | 710 | 320,182 | $1,397,649$ | $1,717,831$ | 10 | 4 | 10.38 |
| 12 | 741 | 337,601 | $1,276,726$ | $1,614,327$ | 10 | 4 | 12.52 |
| 13 | 681 | 287,991 | 907,408 | $1,195,399$ | 10 | 4 | 10.42 |

Table 5.60 PSCMP results of test no. 8 using the lowest transportation cost method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
| Time |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| (minutes) |  |  |  |  |  |  |  |

Table 5.61 PSCMP resuits of test no. 9 using the lowest transportation cost method

| Week <br> No. | \# of <br> SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 755 | 342.615 | 737,330 | 1,079,945 | 10 | 4 | 16.23 |
| 2 | 695 | 311.933 | 898,490 | 1,210.423 | 10 | 4 | 13.37 |
| 3 | 801 | 343.183 | 1,344,370 | 1,687,553 | 10 | 4 | 22.03 |
| 4 | 755 | 372.618 | 1,253,537 | 1,626,155 | 10 | 3 | 19.23 |
| 5 | 593 | 281.957 | 954,678 | 1,236,635 | 10 | 4 | 8.12 |
| 6 | 671 | 285,725 | 1,341,866 | 1,627,591 | 10 | 4 | 12.05 |
| 7 | 705 | 309,855 | 1,055,756 | 1,365,611 | 10 | 4 | 13.57 |
| 8 | 903 | 416,886 | 1,564,033 | 1,980,919 | 10 | 3 | 33.55 |
| 9 | 798 | 357,453 | 1,335,804 | 1,693,257 | 10 | 4 | 21.22 |
| 10 | 653 | 325.879 | 1,171,517 | 1,497,396 | 10 | 3 | 10.40 |
| 11 | 674 | 329,592 | 1,168,888 | 1.498,480 | 10 | 4 | 12.28 |
| 12 | 753 | 363.763 | 1,555,726 | 1,919,489 | 10 | 4 | 16.59 |
| 13 | 788 | 366,029 | 1.255,414 | 1,621,443 | 10 | 4 | 12.36 |

Table 5.62 PSCMP results of test no. 10 using the lowest transportation cost method

| Week <br> No. | $\begin{gathered} \text { \# of } \\ \text { SO items } \end{gathered}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | $\begin{gathered} \hline \text { CPU } \\ \text { Time } \\ \text { (minutes) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 628 | 303,837 | 562,043 | 865,880 | 10 | 4 | 15.00 |
| 2 | 767 | 356,894 | 1,181,429 | 1.538.323 | 10 | 4 | 21.49 |
| 3 | 656 | 310,012 | 880.795 | 1.190,807 | 10 | 4 | 16.11 |
| 4 | 676 | 304,244 | 1,139,189 | 1,443,433 | 10 | 4 | 17.29 |
| 5 | 656 | 317,254 | 1,259.141 | 1.576,395 | 10 | 4 | 16.03 |
| 6 | 733 | 323,697 | 1,215,550 | 1.539.247 | 10 | 4 | 19.34 |
| 7 | 680 | 309.182 | 1.040.121 | 1.349.303 | 10 | 4 | 17.04 |
| 8 | 784 | 354,068 | 1,535.099 | 1.889.167 | 10 | 4 | 22.53 |
| 9 | 698 | 308,716 | 972.644 | 1.281,360 | 10 | 4 | 17.58 |
| 10 | 791 | 381,165 | 1.561.669 | 1.942.834 | 10 | 4 | 23.42 |
| 11 | 621 | 302,125 | 831.668 | 1,133,793 | 10 | 4 | 14.12 |
| 12 | 604 | 281,817 | 1.177.978 | 1.459,795 | 10 | 4 | 14.11 |
| 13 | 716 | 311.749 | 1.289.084 | 1.600,833 | 10 | 4 | 18.37 |

Table 5.63 PSCMP results of test no.1 using the single warehouse preference method

| Week No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 738 | 346.903 | 717,726 | 1,064,629 | 10 | 4 | 11.13 |
| 2 | 598 | 284,266 | 865,881 | 1,150,147 | 10 | 4 | 6.41 |
| 3 | 639 | 312.351 | 972,537 | 1.284,888 | 10 | 4 | 8.07 |
| 4 | 899 | 441,705 | 1,832,034 | 2.273,739 | 10 | 4 | 25.51 |
| 5 | 678 | 327.619 | 1,047,402 | 1,375,021 | 10 | 3 | 9.41 |
| 6 | 786 | 367,439 | 1.366.267 | 1.733 .706 | 10 | 4 | 15.24 |
| 7 | 849 | 420,123 | 1,518,020 | 1,938,143 | 10 | 4 | 19.50 |
| 8 | 847 | 452,734 | 1,592,929 | 2,045,663 | 10 | 4 | 20.54 |
| 9 | 694 | 351,317 | 1,195,027 | 1,546,344 | 10 | 3 | 9.44 |
| 10 | 799 | 371.890 | 1,423,585 | 1,795,475 | 10 | 4 | 16.54 |
| 11 | 681 | 303,962 | 1,103,694 | 1,407,656 | 10 | 4 | 8.56 |
| 12 | 784 | 372.683 | 1,429,679 | 1,802,362 | 10 | 4 | 14.41 |
| 13 | 810 | 357,391 | 1,514,802 | 1,872,193 | 10 | 4 | 16.05 |

Table 5.64 PSCMP results of test no. 2 using the single warehouse preference method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 657 | 288,642 | 507.396 | 796,038 | 10 | 4 | 10.31 |
| 2 | 579 | 284,674 | 831,697 | 1,116,371 | 10 | 3 | 8.33 |
| 3 | 909 | 397,883 | 1,450,693 | 1.848.576 | 10 | 4 | 32.46 |
| 4 | 746 | 341,734 | 1,251,549 | 1.593.283 | 10 | 4 | 19.51 |
| 5 | 698 | 339.600 | 1,100,860 | 1,440,460 | 10 | 4 | 15.16 |
| 6 | 592 | 281,935 | 1,222,350 | 1,504,285 | 10 | 4 | 8.05 |
| 7 | 604 | 291,066 | 1,079,957 | 1,371,023 | 10 | 4 | 9.36 |
| 8 | 840 | 405.977 | 1.579.026 | 1,985,003 | 10 | 4 | 28.09 |
| 9 | 602 | 264.924 | 779,889 | 1,044,813 | 10 | 4 | 9.57 |
| 10 | 733 | 345,390 | 1,442,174 | 1.787.564 | 10 | 4 | 17.24 |
| 11 | 854 | 395,451 | 1,455,464 | 1,850,915 | 10 | 4 | 29.38 |
| 12 | 657 | 325,425 | 1,227,773 | 1.553,198 | 10 | 4 | 12.13 |
| 13 | 634 | 332.336 | 1,217.189 | 1.549.525 | 10 | 4 | 10.33 |

Table 5.65 PSCMP results of test no. 3 using the single warehouse preference method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 817 | 365,460 | 751,734 | 1,117,194 | 10 | 3 | 24.46 |
| 2 | 768 | 381.491 | 1,227,419 | 1,608.910 | 10 | 4 | 18.51 |
| 3 | 818 | 369.554 | 1,293,466 | 1,663,020 | 10 | 4 | 27.09 |
| 4 | 740 | 353,535 | 1,221,229 | 1,574,764 | 10 | 4 | 19.32 |
| 5 | 665 | 317.382 | 1,195,432 | 1,512,814 | 10 | 4 | 15.29 |
| 6 | 879 | 405.612 | 1,514,244 | 1,919,856 | 10 | 4 | 31.56 |
| 7 | 734 | 340,980 | 1,198,302 | 1,539,282 | 10 | 4 | 15.09 |
| 8 | 662 | 314,085 | 1,015,877 | 1,329,962 | 10 | 4 | 14.52 |
| 9 | 701 | 364,100 | 1,431,342 | 1,795,442 | 10 | 4 | 16.26 |
| 10 | 603 | 288,870 | 894,356 | 1,183,226 | 10 | 4 | 10.13 |
| 11 | 879 | 396,551 | 1,783,625 | 2,180,176 | 10 | 4 | 20.00 |
| 12 | 648 | 292,946 | 847,343 | 1,140,289 | 10 | 3 | 7.01 |
| 13 | 702 | 343,278 | 1,349,091 | 1,692,369 | 10 | 4 | 10.11 |

Table 5.66 PSCMP results of test no.4 using the single warehouse preference method

| Week No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 857 | 293,589 | 1,266,423 | 1,560,012 | 10 | 4 | 38.33 |
| 2 | 738 | 330.914 | 1,070.632 | 1.401 .546 | 10 | 4 | 21.25 |
| 3 | 759 | 342.905 | 1,347,062 | 1.689,967 | 10 | 4 | 22.45 |
| 4 | 878 | 448,790 | 1,827,411 | 2,276,201 | 10 | 4 | 44.11 |
| 5 | 688 | 317.351 | 1,143,466 | 1.460 .817 | 10 | 4 | 18.41 |
| 6 | 715 | 320.318 | 1.385.152 | 1,705,470 | 10 | 4 | 14.13 |
| 7 | 656 | 330,017 | 1.111.725 | 1.441.742 | 10 | 4 | 7.23 |
| 8 | 743 | 323,064 | 1,168,924 | 1,491,988 | 10 | 4 | 21.59 |
| 9 | 585 | 291.757 | 966.796 | 1,258,553 | 10 | 4 | 5.58 |
| 10 | 761 | 323.081 | 1.329.090 | 1.652.171 | 10 | 3 | 22.50 |
| 11 | 638 | 296,236 | 1,054,123 | 1,350,359 | 10 | 4 | 10.53 |
| 12 | 680 | 316.395 | 1.300.195 | 1,616.590 | 10 | 4 | 19.02 |
| 13 | 715 | 318,630 | 1.324.121 | 1,642.751 | 10 | 4 | 19.06 |

Table 5.67 PSCMP resuits of test no. 5 using the single warehouse preference method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 617 | 302.665 | 548.803 | 851.468 | 10 | 3 | 9.29 |
| 2 | 706 | 352.290 | 1.056,703 | 1,408,993 | 10 | 4 | 19.20 |
| 3 | 720 | 369,237 | 1,096,759 | 1,465,996 | 10 | 4 | 20.05 |
| 4 | 872 | 403,105 | 1,724,727 | 2,127.832 | 10 | 4 | 4.10 |
| 5 | 613 | 291.281 | 952,853 | 1,244,134 | 10 | 4 | 9.39 |
| 6 | 763 | 374.571 | 1,404,249 | 1,778,820 | 10 | 4 | 22.59 |
| 7 | 704 | 336,376 | 1,084,227 | 1,420,603 | 10 | 4 | 19.09 |
| 8 | 744 | 338.061 | 1,452,522 | 1,790,583 | 10 | 4 | 22.52 |
| 9 | 735 | 348.620 | 1,255.789 | 1,604,409 | 10 | 4 | 22.14 |
| 10 | 617 | 309.627 | 1,053,687 | 1,363.314 | 10 | 4 | 11.02 |
| 11 | 848 | 371,370 | 1,360,411 | 1,731,781 | 10 | 4 | 5.36 |
| 12 | 777 | 393,292 | 1,543,225 | 1,936,517 | 10 | 4 | 26.25 |
| 13 | 722 | 343,383 | 1,147,637 | 1,491,020 | 10 | 4 | 18.25 |

Table 5.68 PSCMP results of test no.6 using the single warehouse preference method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| (mime |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 761 | 374,118 | 667,125 | $1,041,243$ | 10 | 3 | 22.42 |
| 2 | 757 | 345,768 | $1,233,450$ | $1,579,218$ | 10 | 4 | 26.06 |
| 3 | 809 | 387,959 | $1,266,634$ | $1,654,593$ | 10 | 3 | 38.01 |
| 4 | 809 | 353,789 | $1,523,201$ | $1,876,990$ | 10 | 4 | 30.57 |
| 5 | 764 | 342,568 | $1,141,419$ | $1,483,987$ | 10 | 4 | 27.01 |
| 6 | 739 | 374,073 | $1,451,645$ | $1,825,718$ | 10 | 4 | 22.11 |
| 7 | 880 | 440,143 | $1,444,298$ | $1,984,441$ | 10 | 4 | 4.45 |
| 8 | 834 | 381,375 | $1,392,686$ | $1,774,061$ | 10 | 4 | 4.24 |
| 9 | 877 | 413,294 | $1,438,396$ | $1,851,690$ | 10 | 4 | 4.48 |
| 10 | 723 | 355,507 | $1,501,238$ | $1,856,745$ | 10 | 4 | 21.28 |
| 11 | 665 | 297,272 | 952,044 | $1,249,316$ | 10 | 4 | 18.39 |
| 12 | 892 | 478,501 | $1,920,991$ | $2,399,492$ | 10 | 4 | 5.10 |
| 13 | 804 | 369,388 | $1,187,303$ | $1,556,691$ | 10 | 4 | 31.26 |

Table 5.69 PSCMP results of test no. 7 using the single warehouse preference method

| Week | \# of | Cost l | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 827 | 402,330 | 751,480 | $1,153,810$ | 10 | 4 | 17.56 |
| 2 | 794 | 403,488 | $1,333,743$ | $1,737,231$ | 10 | 4 | 15.57 |
| 3 | 800 | 391,600 | $1,522,035$ | $1,913,635$ | 10 | 4 | 16.49 |
| 4 | 597 | 319,616 | 956,582 | $1,276,198$ | 10 | 4 | 6.29 |
| 5 | 772 | 380,456 | $1,305,406$ | $1,685,862$ | 10 | 4 | 14.30 |
| 6 | 892 | 441,626 | $1,682,865$ | $2,124,491$ | 10 | 4 | 24.24 |
| 7 | 770 | 364,007 | $1,262,919$ | $1,626,926$ | 10 | 4 | 13.45 |
| 8 | 717 | 373,683 | $1,301,157$ | $1,674,840$ | 10 | 4 | 11.41 |
| 9 | 762 | 377,974 | $1,318,937$ | $1,696,911$ | 10 | 4 | 13.43 |
| 10 | 588 | 275,582 | 995,176 | $1,260,758$ | 10 | 4 | 6.01 |
| 11 | 710 | 331,693 | $1,325,743$ | $1,657,436$ | 10 | 4 | 10.27 |
| 12 | 741 | 353,996 | $1,352,195$ | $1,706,191$ | 10 | 4 | 12.14 |
| 13 | 681 | 319,619 | $1,104,813$ | $1,424,432$ | 10 | 4 | 9.04 |

Table 5.70 PSCMP results of test no.8 using the single warehouse preference method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| 1 | 700 | 346,199 | 558,989 | 905,188 | 10 | 3 | 15.59 |
| 2 | 775 | 367,655 | $1,178,382$ | $1,546,037$ | 10 | 4 | 19.25 |
| 3 | 795 | 424,699 | $1,526,633$ | $1,951,332$ | 10 | 4 | 22.02 |
| 4 | 850 | 378,407 | $1,373,909$ | $1,752,316$ | 10 | 4 | 28.51 |
| 5 | 652 | 307,654 | 953,653 | $1,261,307$ | 10 | 3 | 10.58 |
| 6 | 848 | 415,767 | $1,659,343$ | $2,075,110$ | 10 | 4 | 28.19 |
| 7 | 770 | 376,943 | $1,447,554$ | $1,824,497$ | 10 | 4 | 19.26 |
| 8 | 771 | 375,620 | $1,410,090$ | $1,785,710$ | 10 | 4 | 21.08 |
| 9 | 723 | 353,088 | $1,161,043$ | $1,514,131$ | 10 | 4 | 17.41 |
| 10 | 868 | 430,459 | $1,652,379$ | $2,082,838$ | 10 | 4 | 32.51 |
| 11 | 837 | 423,750 | $1,322,472$ | $1,746,222$ | 10 | 4 | 28.19 |
| 12 | 698 | 361,140 | $1,221,201$ | $1,582,341$ | 10 | 4 | 16.55 |
| 13 | 734 | 329,719 | $1,314,889$ | $1,644,608$ | 10 | 4 | 15.11 |

Table 5.71 PSCMP results of test no. 9 using the single warehouse preference method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | ---: | ---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  |  |
| (minutes) |  |  |  |  |  |  |  |
| 1 | 755 | 378,849 | 743,363 | $1,122,212$ | 10 | 4 | 17.28 |
| 2 | 695 | 320,650 | 933,916 | $1,254,566$ | 10 | 4 | 13.18 |
| 3 | 801 | 394.703 | $1,483,151$ | $1,877,854$ | 10 | 4 | 23.48 |
| 4 | 755 | 372.272 | $1,261,405$ | $1,633,677$ | 10 | 4 | 19.50 |
| 5 | 593 | 296,444 | 907,771 | $1,204,215$ | 10 | 4 | 8.12 |
| 6 | 671 | 287,195 | $1,326,759$ | $1,613,954$ | 10 | 4 | 12.36 |
| 7 | 705 | 336,429 | $1,239,743$ | $1,576,172$ | 10 | 4 | 14.38 |
| 8 | 903 | 445,405 | $1,680,123$ | $2,125,528$ | 10 | 4 | 33.13 |
| 9 | 798 | 374,866 | $1,372,791$ | $1,747,657$ | 10 | 4 | 22.25 |
| 10 | 653 | 339,283 | $1,019,055$ | $1,358,338$ | 10 | 4 | 10.57 |
| 11 | 674 | 361,068 | $1,389,191$ | $1,750,259$ | 10 | 4 | 13.02 |
| 12 | 753 | 381,568 | $1,518,379$ | $1,899,947$ | 10 | 4 | 15.35 |
| 13 | 788 | 420,067 | $1,406,280$ | $1,826,347$ | 10 | 4 | 12.07 |

Table 5.72 PSCMP results of test no. 10 using the single warehouse preference method

| Week <br> No. | \# of <br> SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 628 | 305.635 | 563.627 | 869.262 | 10 | 4 | 16.32 |
| 2 | 767 | 388,403 | 1,217,843 | 1,606,246 | 10 | 4 | 23.34 |
| 3 | 656 | 325,308 | 920,632 | 1,245,940 | 10 | 4 | 17.45 |
| 4 | 676 | 336.798 | 1.331.217 | 1,668,015 | 10 | 4 | 17.41 |
| 5 | 656 | 320,785 | 1,119.825 | 1,440,610 | 10 | 4 | 16.34 |
| 6 | 733 | 342,276 | 1,297,328 | 1.639,604 | 10 | 4 | 19.35 |
| 7 | 680 | 326,780 | 1.120.721 | 1,447,501 | 10 | 4 | 19.11 |
| 8 | 784 | 359.273 | 1.568.006 | 1,927,279 | 10 | 4 | 23.46 |
| 9 | 698 | 317,998 | 1,011.626 | 1.329,624 | 10 | 4 | 17.36 |
| 10 | 791 | 410,915 | 1,564.459 | 1,975,374 | 10 | 4 | 22.41 |
| 11 | 621 | 316.894 | 990.470 | 1.307,364 | 10 | 4 | 14.23 |
| 12 | 604 | 294,531 | 904,219 | 1,198,750 | 10 | 4 | 14.20 |
| 13 | 716 | 337.729 | 1,408,805 | 1,746,534 | 10 | 4 | 18.25 |

Table 5.73 PSCMP results of test no.1 using PSCMP heuristic method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 738 | 308,476 | 604,619 | 913,095 | 9 | 3 | 29.30 |
| 2 | 598 | 268.956 | 650,892 | 919,848 | 10 | 3 | 21.43 |
| 3 | 639 | 279.786 | 1,149,526 | 1,429,312 | 10 | 3 | 32.45 |
| 4 | 899 | 359.859 | 1,378,125 | 1,737,984 | 10 | 4 | 28.21 |
| 5 | 678 | 282.400 | 942,237 | 1,224,637 | 8 | 3 | 17.58 |
| 6 | 786 | 323,269 | 1.383,349 | 1,706,618 | 9 | 4 | 40.16 |
| 7 | 849 | 367,985 | 1.339,989 | 1,707.974 | 10 | 4 | 48.09 |
| 8 | 847 | 362.921 | 1,239,408 | 1,602,329 | 10 | 4 | 38.57 |
| 9 | 694 | 307,983 | 1,070,710 | 1,378,693 | 9 | 4 | 19.20 |
| 10 | 799 | 332,776 | 1,474,094 | 1,806,870 | 9 | 4 | 50.26 |
| 11 | 681 | 294.061 | 1,019,667 | 1,313,728 | 10 | 4 | 39.11 |
| 12 | 784 | 327,430 | 1,388,306 | 1,715.736 | 9 | 4 | 51.04 |
| 13 | 810 | 329.887 | 1,159,184 | 1,489,071 | 10 | 4 | 47.44 |

Table 5.74 PSCMP results of test no. 2 using PSCMP heuristic method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | (mine |
|  |  |  |  |  |  |  |  |
| 1 | 657 | 282,945 | 911,679 | $1,194,624$ | 9 | 3 | 32.47 |
| 2 | 579 | 253,231 | 985,650 | $1,238,881$ | 10 | 4 | 26.54 |
| 3 | 909 | 380,283 | $1,549,392$ | $1,929,675$ | 9 | 4 | 56.13 |
| 4 | 746 | 294,662 | $1,148,208$ | $1,442,870$ | 9 | 3 | 47.22 |
| 5 | 698 | 301,331 | $1,003,066$ | $1,304,397$ | 9 | 4 | 38.32 |
| 6 | 592 | 257,768 | 910,612 | $1,168,380$ | 10 | 4 | 29.44 |
| 7 | 604 | 266,677 | $1,063,871$ | $1,330,548$ | 9 | 4 | 39.53 |
| 8 | 840 | 350,158 | $1,341,585$ | $1,691,743$ | 10 | 4 | 55.37 |
| 0 | 602 | 252,304 | $1,082,079$ | $1,334,383$ | 10 | 4 | 23.50 |
| 10 | 733 | 305,721 | 965,584 | $1,271,305$ | 9 | 3 | 43.01 |
| 11 | 854 | 361,892 | $1,430.563$ | $1,792,455$ | 8 | 4 | 54.42 |
| 12 | 657 | 282,752 | $1,053.265$ | $1,336,017$ | 9 | 4 | 46.28 |
| 13 | 634 | 279,464 | 967,626 | $1,247,090$ | 9 | 4 | 21.10 |

Table 5.75 PSCMP results of test no. 3 using PSCMP heuristic method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 817 | 343,837 | 703,378 | 1,047,215 | 10 | 3 | 51.06 |
| 2 | 768 | 318.249 | 1,070,965 | 1,389,214 | 10 | 3 | 28.59 |
| 3 | 818 | 334.392 | 1,274,990 | 1,609,382 | 10 | 3 | 39.48 |
| 4 | 740 | 327.419 | 1,110,288 | 1,437.707 | 10 | 4 | 45.06 |
| 5 | 665 | 291.668 | 1,097,497 | 1,389,165 | 10 | 4 | 27.33 |
| 6 | 879 | 375,354 | 1,348,261 | 1,723,615 | 9 | 4 | 58.09 |
| 7 | 734 | 311,855 | 1,264,781 | 1,576,636 | 10 | 4 | 37.44 |
| 8 | 662 | 280.438 | 893,608 | 1,174,046 | 8 | 3 | 19.06 |
| 9 | 701 | 301.799 | 1,256,895 | 1,558,694 | 10 | 4 | 35.50 |
| 10 | 603 | 274.527 | 939,943 | 1,214,470 | 8 | 4 | 20.16 |
| 11 | 879 | 372,899 | 1,482,525 | 1,855,424 | 9 | 4 | 43.36 |
| 12 | 648 | 268.806 | 986,875 | 1,255,681 | 9 | 3 | 19.21 |
| 13 | 702 | 311,199 | 1,147,948 | 1,459,147 | 10 | 4 | 26.33 |

Table 5.76 PSCMP results of test no.4 using PSCMP heuristic method

| Week No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 857 | 363,150 | 766,792 | 1,129,942 | 10 | 3 | 52.21 |
| 2 | 738 | 296,374 | 1,051.268 | 1,347.642 | 9 | 4 | 32.44 |
| 3 | 759 | 327,567 | 1,111.382 | 1.438.949 | 9 | 4 | 41.04 |
| 4 | 878 | 359.486 | 1.376 .762 | 1.736,248 | 9 | 3 | 40.21 |
| 5 | 688 | 285.968 | 1,169,221 | 1,455,189 | 9 | 4 | 34.43 |
| 6 | 715 | 303,062 | 1.070.504 | 1.373.566 | 10 | 3 | 32.57 |
| 7 | 656 | 294.414 | 90.937 | 1.285.351 | 8 | 4 | 16.05 |
| 8 | 743 | 311,955 | 1.329.472 | 1.641.427 | 10 | 4 | 51.46 |
| 9 | 585 | 255,613 | 956.810 | 1.212 .423 | 8 | 3 | 17.42 |
| 10 | 761 | 317.575 | 1.159 .960 | 1,477.535 | 9 | 3 | 49.48 |
| 11 | 638 | 281.484 | 1,067.584 | 1,349,068 | 10 | 4 | 27.46 |
| 12 | 680 | 293.933 | 977,560 | 1.271.493 | 10 | 4 | 56.25 |
| 13 | 715 | 292.730 | 985,803 | 1.278.533 | 9 | 4 | 46.14 |

Table 5.77 PSCMP results of test no.5 using PSCMP heuristic method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  | (minutes) |
| 1 | 617 | 282,584 | 414,172 | 696,756 | 10 | 4 | 19.47 |
| 2 | 706 | 296,989 | 944,400 | $1,241,389$ | 9 | 3 | 54.02 |
| 3 | 720 | 318,523 | 966,065 | $1,284,588$ | 10 | 3 | 46.19 |
| 4 | 872 | 368,895 | $1,487,582$ | $1,856,477$ | 10 | 4 | 26.14 |
| 5 | 613 | 266,765 | $1,008,737$ | $1,275,502$ | 9 | 4 | 14.52 |
| 6 | 763 | 335,231 | $1,279,954$ | $1,615,185$ | 9 | 4 | 50.29 |
| 7 | 704 | 307,573 | $1,030,240$ | $1,337,813$ | 10 | 4 | 50.25 |
| 8 | 744 | 308,477 | $1,205,615$ | $1,514,092$ | 8 | 4 | 49.35 |
| 9 | 735 | 314,008 | $1,262,997$ | $1,577,005$ | 8 | 3 | 38.42 |
| 10 | 617 | 277,365 | 988,664 | $1,266,029$ | 10 | 4 | 25.22 |
| 11 | 848 | 363,238 | $1,439,382$ | $1,802,620$ | 10 | 4 | 40.23 |
| 12 | 777 | 321,634 | $1,175,614$ | $1,497,248$ | 9 | 4 | 33.29 |
| 13 | 722 | 311,070 | $1,091,097$ | $1,402,167$ | 9 | 3 | 23.30 |

Table 5.78 PSCMP results of test no.6 using PSCMP heuristic method

| Week <br> No. | \# of <br> SO items | Cost I | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 761 | 322,075 | 527,086 | 849,161 | 10 | 3 | 49.03 |
| 2 | 757 | 321,913 | 1,229,741 | 1,551,654 | 9 | 4 | 56.02 |
| 3 | 809 | 353,826 | 1,016.402 | 1.370 .228 | 10 | 3 | 53.39 |
| 4 | 809 | 340,851 | 1,426,174 | 1,767.025 | 10 | 4 | 58.25 |
| 5 | 764 | 322,679 | 1,228,317 | 1.550 .996 | 10 | 4 | 30.32 |
| 6 | 739 | 328,213 | 1,235,101 | 1.563.314 | 9 | 4 | 47.46 |
| 7 | 880 | 385,900 | 1,383,912 | 1.769 .812 | 10 | 4 | 12.51 |
| 8 | 834 | 340,409 | 1,334,500 | 1,674,909 | 10 | 4 | 15.16 |
| 9 | 877 | 366,733 | 1,249,521 | 1,616.254 | 9 | 3 | 16.49 |
| 10 | 723 | 319,179 | 1,122,210 | 1,441,389 | 10 | 4 | 32.37 |
| 11 | 665 | 288,712 | 1,064,246 | 1,352,958 | 9 | 4 | 19.40 |
| 12 | 892 | 384,749 | 1.455 .584 | 1.840,333 | 9 | 4 | 17.36 |
| 13 | 804 | 336,827 | 1,245,135 | 1.581,962 | 9 | 4 | 54.40 |

Table 5.79 PSCMP results of test no. 7 using PSCMP heuristic method

| Week | \# of | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | SO items |  |  |  |  |  |  |
|  |  |  |  |  |  |  | Time |
|  |  |  |  |  |  |  |  |
| (minutes) |  |  |  |  |  |  |  |
| 1 | 827 | 350,992 | 675,041 | $1,026,033$ | 9 | 3 | 31.54 |
| 2 | 794 | 334,669 | $1,082,090$ | $1,416,759$ | 9 | 4 | 44.58 |
| 3 | 800 | 329,569 | $1,295,364$ | $1,624,933$ | 10 | 4 | 15.29 |
| 4 | 597 | 253,988 | $1,008,281$ | $1,262,269$ | 8 | 4 | 16.41 |
| 5 | 772 | 337,013 | $1,210,978$ | $1,547,991$ | 9 | 3 | 33.50 |
| 6 | 892 | 378,044 | $1,379,554$ | $1,757,598$ | 10 | 4 | 36.09 |
| 7 | 770 | 334,403 | $1,218,905$ | $1,553,308$ | 10 | 4 | 25.45 |
| 8 | 717 | 309,481 | $1,185,356$ | $1,494,837$ | 9 | 4 | 28.40 |
| 9 | 762 | 322,361 | $1,159,933$ | $1,482,294$ | 8 | 4 | 19.59 |
| 10 | 588 | 250,737 | 859,567 | $1,110,304$ | 9 | 4 | 19.27 |
| 11 | 710 | 303,538 | $1,265,290$ | $1,568,828$ | 10 | 4 | 30.15 |
| 12 | 741 | 318,493 | $1,297,973$ | $1,616,466$ | 8 | 4 | 34.17 |
| 13 | 681 | 279,829 | 875,896 | $1,155,725$ | 10 | 3 | 40.28 |

Table 5.80 PSCMP results of test no.8 using PSCMP heuristic method

| Week <br> No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU <br> Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 700 | 306,942 | 452,271 | 759,213 | 10 | 3 | 37.49 |
| 2 | 775 | 342,257 | 1,122,473 | 1.464,730 | 10 | 4 | 42.09 |
| 3 | 795 | 326,606 | 1,192,353 | 1.518,959 | 9 | 3 | 52.02 |
| 4 | 850 | 340,097 | 1,402,155 | 1,742.252 | 9 | 4 | 35.30 |
| 5 | 652 | 290,777 | 940.879 | 1.231,656 | 10 | 4 | 21.26 |
| 6 | 848 | 351,872 | 1.517 .811 | 1,869,683 | 9 | 4 | 25.30 |
| 7 | 770 | 323.204 | 1,192,080 | 1.515.284 | 8 | 4 | 40.58 |
| 8 | 771 | 332,749 | 1,134,355 | 1.467,104 | 10 | 4 | 55.40 |
| 9 | 723 | 310.279 | 1,281,327 | 1,591,606 | 8 | 4 | 43.06 |
| 10 | 868 | 349,986 | 1,323.246 | 1.673,232 | 10 | 4 | 41.03 |
| 11 | 837 | 355,731 | 1,504.270 | 1.860,001 | 9 | 4 | 24.39 |
| 12 | 698 | 304,599 | 968,323 | 1,272,922 | 9 | 4 | 19.46 |
| 13 | 734 | 303.496 | 1,131,038 | 1,434,534 | 9 | 4 | 33.46 |

Table 5.81 PSCMP results of test no.9 using PSCMP heuristic method

| Week No. | \# of SO items | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | CPU Time <br> (minutes) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 755 | 322.852 | 671.672 | 994,524 | 9 | 4 | 21.21 |
| 2 | 695 | 298,632 | 853.521 | 1,152,153 | 9 | 4 | 18.28 |
| 3 | 801 | 319,049 | 1,263,022 | 1,582,071 | 8 | 4 | 41.31 |
| 4 | 755 | 324,956 | 1,156,597 | 1,481,553 | 9 | 4 | 38.38 |
| 5 | 593 | 272,065 | 955.333 | 1,227,398 | 9 | 4 | 18.52 |
| 6 | 671 | 269825 | 1,292,007 | 1,561,832 | 8 | 4 | 17.23 |
| 7 | 705 | 302,138 | 1,070,308 | 1,372,446 | 9 | 4 | 48.43 |
| 8 | 903 | 384,346 | 1,449,158 | 1,833,504 | 9 | 4 | 31.15 |
| 9 | 798 | 337,744 | 1,193,738 | 1,531,482 | 10 | 4 | 45.38 |
| 10 | 653 | 298,588 | 1,006,541 | 1,305,129 | 10 | 4 | 28.44 |
| 11 | 674 | 288,904 | 1,172,242 | 1,461,146 | 10 | 4 | 31.02 |
| 12 | 753 | 325,228 | 1,177,576 | 1,502,804 | 9 | 4 | 33.43 |
| 13 | 788 | 344,996 | 1,236,746 | 1,581,742 | 9 | 4 | 25.19 |

Table 5.82 PSCMP results of test no.10 using PSCMP heuristic method

| Week <br> No. | $\begin{gathered} \text { \# of } \\ \text { SO items } \end{gathered}$ | Cost 1 | Cost 2 | Total Costs | \# of Whs. | \# of Plants | $\begin{gathered} \text { CPU } \\ \text { Time } \\ \text { (minutes) } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 628 | 279,743 | 428.343 | 708.086 | 9 | 3 | 36.50 |
| 2 | 767 | 325.826 | 1.108.838 | 1.434.664 | 9 | 4 | 49.18 |
| 3 | 656 | 291,735 | 1,046,054 | 1,337,789 | 9 | 3 | 50.36 |
| 4 | 676 | 277,634 | 952,929 | 1,230,563 | 10 | 4 | 31.07 |
| 5 | 656 | 292,039 | 1,028,338 | 1.320.377 | 9 | 4 | 30.01 |
| 6 | 733 | 304,068 | 1,382.907 | 1.686 .975 | 8 | 4 | 29.45 |
| 7 | 680 | 283,774 | 901.117 | 1.184.891 | 8 | 4 | 30.39 |
| 8 | 784 | 322,595 | 1,294,514 | 1.617 .109 | 10 | 4 | 52.37 |
| 9 | 698 | 286.815 | 978,872 | 1.265.687 | 8 | 4 | 30.06 |
| 10 | 791 | 326,708 | 1,258,442 | 1,585.150 | 10 | 4 | 30.30 |
| 11 | 621 | 289,760 | 1,070,165 | 1,359,925 | 9 | 4 | 19.24 |
| 12 | 604 | 257,312 | 970,016 | 1,227,328 | 9 | 3 | 19.42 |
| 13 | 716 | 296,195 | 1,192,485 | 1.488.680 | 9 | 4 | 41.38 |

Table 5.83 shows a comparison of the results for PSCMP total supply chain costs
over 13 weeks that were solved using all four methods. The performance measure employed in this comparison was quality of solutions. As indicated by the table, PSCMP heuristic
solutions for all 10 tests problems outperformed that of the other three methods. The shortest distance in the worst case came within $17.63 \%$ and in the best case came within $8.52 \%$ of the solution obtained by PSCMP heuristic. The lowest transportation cost in the worst case came within $13.36 \%$ and in the best case came within $5.33 \%$ of solution obtained by PSCMP heuristic. The single warehouse preference in the worst case came within $14.17 \%$ and in the best case came within $6.34 \%$ of the solution obtained by PSCMP heuristic. However, in all cases the other three methods outperformed PSCMP heuristic in the CPU time it looks to find the best solution in each week. PSCMP heuristic in the worst case took 58.25 minutes and in the best case took 12.51 minutes to find the solution, please refer to Table 5.78. While comparing among the other three methods, namely, shortest distance, the lowest transportation cost, and the single warehouse preference methods in term of the quality of solutions, the lowest transportation cost outperformed the shortest distance method in all 10 test problems. The lowest transportation cost also outperformed the single warehouse preference method in 7 out of 10 test problems. The single warehouse preference outperformed the shortest distance in 9 out of 10 test problems. The shortest distance method in the worst case came within $9.08 \%$ and in the best case came within $1.44 \%$ of solution obtained by the lowest transportation cost method. The shortest distance method in the worst case came within $7.02 \%$ and in the best case came within $-1.46 \%$ of solution obtained by the single warehouse preference. The single warehouse preference in the worst case came within $4.41 \%$ and in the best case came within $-0.99 \%$ of solution obtained by the lowest transportation cost. There was not a significant difference in CPU time requirement among these three methods. Note that the percentage difference in solution is computed as ((Method II - Method I) $\div$ Method I) * $100 \%$.

Table 5.83 Comparison of the PSCMP weekly cumulative costs over 13 weeks using shortest distance, lowest transportation cost, single warehouse preference and PSCMP heuristic methods

| No. | Shortest Distance <br> (1) | Lowest <br> Trans. Cost (2) | Single Wh. Pref. <br> (3) | PSCMP <br> Heuristic <br> (4) | \% <br> Diff <br> in <br> Sol. <br> (1) <br> vs. <br> (2) | \% <br> Diff <br> in <br> Sol. <br> (1) vs. <br> (3) | \% <br> Diff <br> in <br> Sol. <br> (3) vs. <br> (2) | \% <br> Diff <br> in <br> Sol. <br> (1) <br> vs. <br> (4) | \% <br> Dift <br> in <br> Sol. <br> (2) <br> vs. <br> (4) | \% <br> Diff <br> in <br> Sol. <br> (3) <br> vs. <br> (4) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 21,877,016 | 20,740,640 | 21,289,966 | 18,945,895 | 5.48 | 2.76 | 2.65 | 15.47 | 9.47 | 12.37 |
| 2 | 20,085,354 | 19,592.250 | 19,441,054 | 18,282,368 | 2.52 | 3.31 | -0.77 | 9.86 | 7.16 | 6.34 |
| 3 | 20,281,898 | 19,685,861 | 20,257,304 | 18,690,396 | 3.03 | 0.12 | 2.90 | 8.52 | 5.33 | 8.38 |
| 4 | 20,345,012 | 19,199,973 | 20,548,167 | 17,997,366 | 5.96 | -0.99 | 7.02 | 13.04 | 6.68 | 14.17 |
| 5 | 20,906,938 | 20,492,623 | 20,215,470 | 18,366,871 | 2.02 | 3.42 | -1.35 | 13.83 | 11.57 | 10.06 |
| 6 | 22,735,714 | 21,355,116 | 22,034,185 | 19,929,995 | 6.46 | 3.18 | 3.18 | 14.08 | 7.15 | 10.56 |
| 7 | 21,680.460 | 19,993.183 | 20,938,721 | 18,617,345 | 8.44 | 3.54 | 4.73 | 16.45 | 7.39 | 12.47 |
| 8 | 22,311,472 | 21,993,721 | 21,671,637 | 19,401,176 | 1.44 | 2.95 | -1.46 | 15.00 | 13.36 | 11.70 |
| 9 | 21,864,241 | 20,044,897 | 20,990,726 | 18,587,784 | 9.08 | 4.16 | 4.72 | 17.63 | 7.84 | 12.93 |
| 10 | 20,258,257 | 18,811,170 | 19,402,103 | 17,447,224 | 7.69 | 4.41 | 3.14 | 16.11 | 7.82 | 11.20 |

Table 5.84 The weekly cumulative cost of all four methods based on test problem no. 10

| Week No. | Shortest Distance | Lowest Trans. Cost | Single Wh. Preference | PSCMP Heuristic |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 856,418 | 865.880 | 869.262 | 708.086 |
| 2 | 2,524,264 | 2.404.203 | 2,475.508 | 2.142.750 |
| 3 | 3,851,840 | 3,595,010 | 3,721,448 | 3.480 .539 |
| 4 | 5,672,908 | 5.038 .443 | 5,389.463 | 4,711.102 |
| 5 | 7,222,226 | 6,614.838 | 6,830,073 | 6,031.479 |
| 6 | 8,805,338 | 8,154,085 | 8,469,677 | 7,718,454 |
| 7 | 10.275,987 | 9,503,388 | 9,917,178 | 8,903,345 |
| 8 | 12.152 .828 | 11.392 .555 | 11,844,457 | 10.520 .454 |
| 9 | 13,672,286 | 12.673.915 | 13,174,081 | 11.786,141 |
| 10 | 15,702,135 | 14.616 .749 | 15.149.455 | 13,371,291 |
| 11 | 17.134,957 | 15,750,542 | 16,456,819 | 14,731,216 |
| 12 | 18.514.691 | 17,210,337 | 17.655,569 | 15.958.544 |
| 13 | 20.258,257 | 18,811,170 | 19,402,103 | 17,447,224 |

Table 5.84 shows the weekly cumulative cost for all four methods based on the results of test problem 10 presented in Tables $5.52,5.62,5.72$, and 5.82. The results of test problem 10 is shown as a representative of the results obtained with the other remaining 9
problems as shown in Tables 5.43-5.81. The pattern of the results of problem 10 is similar to those of problems 1 through 9 .

Figure 5.3 provides a perspective on how the cumulative total costs of pull-based supply chain system in multiple product cases may vary as the number of weeks increases based on the results presented in Table 5.84. The four curves shown represent the four solution approaches tested. From Figure 5.3, it can be seen that the pattern for the cumulative cost are very similar for all the approaches. However, the cost pattern for the PSCMP method has the flattest slop and the shortest distance method the steepest slop, and consequently, the worst cost record. The curve patterns for the lowest transportation cost and the single warehouse preference methods lie between that of the PSCMP heuristic and the shortest distance method. It also can be seen that the gap between these two curves is very small, and with the two curves almost running parallel to one another from the eighth week through the thirteenth week, the end of the study period. This indicates that as the number of weeks increase, the performance difference between the two approaches will remain relatively stable. On the other hand, when the cumulative cost curve of the PSCMP heuristic relative to those of the other three methods is compared to the cumulative cost curve of the PSCSP method relative to its counterpart approaches, PSCMP curve shows the best slope. PSCMP heuristic has started to dominate the other three methods after fourth week as is evident on the graph. It can be seen that the gaps between PSCMP heuristic curve and the other three curves are much wider when the number of weeks increase. This means that the solution quality of PSCSP heuristic method keeps improving tremendously overtime as one might expect. For a decision maker, the results imply that the adoption of the PSCMP heuristic method for a pull-based supply chain system with multiple products offers the
greatest opportunity for the overall minimization of cost when compared to the other approaches tested.


Figure 5.3 Graph of result from table 5.84

## CHAPTER 6

## SUMMARY AND CONCLUSION

In this study, the problem of integrating decisions along a customer demand driven or pull-based supply chain network involving single product or multiple products in a multiechelon distribution system was addressed. Two main objectives were pursued in the study. The first objective was to present a general framework for the design and configuration of a supply chain network at the strategic and tactical planning levels for a single-product or multiple-product multiple-echelon supply chain system. The second objective was to develop a pull-based algorithm for the management of a pull-based supply chain system both for a single-product and multi-product multi-echelon system at the operational level. In both objectives, the procedures developed sought to minimize the system-wide supply chain cost. Four mixed integer linear programming models were developed in an effort to obtain optimal solution. The first model was based on the single-product capacitated two-echelon facility location problem (SCTFL). The second model was based on the multi-product capacitated two-echelon facility location problem (MCTFL). The third model was based on a pull-based supply chain for a single-product problem (PSCSP) and the last model was based on a pullbased supply chain for a multi-product problems (PSCMP). Because the mixed integer linear programming models were shown to be computationally intensive as the number of products, customers, warehouses, and manufacturing plants increased, decomposition heuristic procedures were developed to solve problems of practical sizes more efficiently.

The performances of the four mixed integer linear programming models and the heuristic procedures were demonstrated on four sets of randomly generated problems. Each
set of problems consisted of 10 test problems, 500 customers, 10 distribution centers/warehouses, and 4 manufacturing plants. In the multi-product problems, MCTFL and PSCMP, the sets consisted of 15 products. All problems were solved via a program coded on Microsoft SQL/Visual Basic version 6.0, on a personal computer with Intel Pentium III- 800 MHz CPU running under the Windows 2000 professional operating system. Quality of solution and CPU time of solution were the performance measures of interest. Also, three additional heuristic solution methods were used to check the quality of heuristic procedures: The three additional procedures were (1) the shortest distance method, (2) the lowest transportation cost method, and (3) the single warehouse preference method.

### 6.1 Summary of Results

The single product capacitated supply chain facility location, SCTFL, problem was tested and compared with other solution methods using 10 problems with randomly generated data. The results of the 10 problems using SCTFL heuristic were presented in Table 5.3. The results using the shortest distance and the lowest transportation cost methods were presented in Table 5.1 and 5.2, respectively. The comparison results between SCTFL heuristic and the two other methods were presented in Table 5.4. In all problems, the solutions obtained from the SCTFL heuristic consistently outperformed the solutions of the two other methods and the difference in solution was very significant. On the other hand, the CPU time required by the two other methods to solve the problems were significantly smaller than those obtained with the SCTFL heuristic.

The multiple products capacitated supply chain facility location, MCTFL, problem was also tested and compared with three other methods using another 10 test problems.

Each problem consisted of 15 products and 500 customers. The results obtained for the 10 problems using MCTFL heuristic were presented in Table 5.8. The results using the shortest distance, the lowest transportation cost, and the single warehouse preference methods were presented in Table 5.5-5.7. The comparison results were presented in Table 5.9 and 5.10. Based on the results obtained for the problems, the MCTFL heuristic consistently outperformed the three other methods. Also, in all problems, the difference in solution was very significant. In contrast, the CPU time required in solving the problems by the three other methods were significantly lower than those obtained using the MCTFL heuristic.

The results of the pull-based supply chain system for the single product case, PSCSP were also tested and compared against those obtained from two other methods using another set of 10 test problems. The results obtained from the PSCSP heuristic were presented in Table 5.31-5.40. The results of the shortest distance and the lowest transportation cost methods were presented in Tables 5.11-5.30. The comparison results were presented in Table 5.41 and 5.42. In all problems, the solution obtained under the PSCSP heuristic were consistently superior to those obtained from the two other methods. In all problems, the difference in solution was also very significant. However, when the CPU time required in solving the problems are used as the basis for performance comparison, the two other methods were much better than that of PSCSP heuristic. A profile of the performance of each method when used over a period of time was presented in Figure 5.2. The graph showed that a company that employs the PSCSP heuristic in managing its supply chain would enjoy much greater improvement in performance over time as compared to that which would be obtained using any of the two other methods

Finally, the pull-based supply chain in multiple product case, PSCMP, was tested and compared with three other methods using another set of 10 test problems. In each problem, there were 15 products and 500 customers involved. The results of PSCMP heuristic were presented in Tables $5.73-5.82$. The results of the shortest distance method, the lowest transportation cost method, and the single warehouse preference method were presented in Tables 5.43-5.72. The comparison results of the four methods were presented in Table 5.41 and 5.42. In all problems, the solution under PSCMP heuristic consistently outperformed those of the three other methods. Also, in most problems, the difference in solution was very significant. However, the CPU time required by the PSCMP heuristic was much longer than those of the other three methods. Again, the performance profile of each solution method over time was presented in Figure 5.3. The graph indicated that a company's supply chain cost would enjoy the most improvement if the PSCMP heuristic is used as against using any of the three other techniques tested.

### 6.2 Conclusion

In this research the problem of integrating decisions in a supply chain system at the strategic, tactical, and operational levels was addressed. Four mathematical models along with heuristic solution algorithms for solving the problems were developed. The effectiveness of the heuristic algorithms were demonstrated by solving some sets of test problems. The results of the test problems also suggest that the heuristics are effective in soiving fairly large size problems with reasonable computational time. One of the most important features of the heuristic algorithms is that they are also suitable for use in any binary location and allocation problems. Other important features of the algorithms include
the ease of implementation, user friendliness, ability to provide a systematic way for improving and tightening a company's supply chain, ability to reduce the total supply chain cost in filling customers' orders, ability for planning and replenishment of systemwide inventories, and the planning of systemwide production. The contributions of the research in the area of supply chain management are significant and are detailed in section 1.5.

It can be concluded that the heuristic algorithms developed for the supply chain network configuration in both the single and muitiple product cases, SCTFL and MCTFL, produced superior performance as compared to the other techniques that were tested. Although the SCTFL and MCTFL algorithms require considerable more time to solve problems, when the computer time is properly weighted against the resulting cost savings that is derived in using the algorithm, the use of the SCTFL and MCTFL heuristics would still prove to be the preferred choice for application in a supply chain system. The choice of SCTFL and MCTFL could be further strengthen by the fact that although an optimal solution is not guaranteed, SCTFL and MCTFL produce very good solutions and can be implemented quite easily.

It can also be concluded that the heuristic algorithms developed for the pull-based supply chain system involving single and multiple products, PSCSP and PSCMP, generate far better results than their counterpart techniques that were also tested. The same conclusion can also be drawn even after considering the effect of the larger computational time required by the heuristics. Like SCTFL and MCTFL, the choice of the PSCSP and PSCMP over their competitors tested is strengthened by the fact that they (i.e., the PSCSP and PSCMP heuristics) produce very good solutions and can be easily implemented. More importantly, they can be used as weekly execution tool.

### 6.3 Insights Gained

When using SCTFL and PSCSP, the number of warehouses and plants played a critical role in overall solutions. In all problems, SCTFL and PSCSP heuristics produced solutions that required fewer warehouses and plants as compared to the solutions obtained with the shortest distance and the lowest transportation cost methods. This is because SCTFL and PSCSP methods do consider warehouse and plant fixed costs in their assignments of orders. This implies the use of SCTFL and PSCSP can produce significant cost savings in systems with high fixed facility costs.

Unlike SCTFL and PSCSP, the number of overall facilities required for the solutions obtained under the MCTFL and PSCMP algorithms were not much different from those obtained with the other heuristic methods tested. This is because the aggregation of different product demands takes place at both the warehouse and plant levels.

Judging from the results obtained from the test problems, one is more likely to obtain a better sotution in terms of total supply chain cost with less CPU time for problems with fewer number of customers and larger number of products per customer as compared to problems with larger number of customers and fewer number of products per customer. In other words, it is easier to obtain good solutions for problem with fewer number of customers and large number of products than for problems with a larger number of customers and fewer number of products.

### 6.4 Possible Extensions

The quest for optimal solutions to supply chain configuration and pull-base supply chain problems of large sizes still remains a formidable task; the problem is not close to
being solved. Because of the computational complexity involved in obtaining optimal solutions, the trend toward the acceptance of near optimal solutions is increasing.

The supply chain network for this research represented a scenario where two echelon systems were integrated and evaluated to satisfy customer demands. Furthermore, the system evaluated was operated under several limiting assumptions: there were known customer demands, all distribution centers were resupplied only from the plants, there were no late shipments, and importantly only a single transportation mode was used. Further research might address these limitations by relaxing them separately or in combinations. The benefits that might be derived from such relaxation include improvement of customer service standards, improvement of inventory positioning, and better transportation system selection and routing. Also, not considered in this study was express orders or some sort of priority orders. As anyone in industry can attest to, priority orders are common in practice and therefore ought to be considered in the planning of supply chain systems. However, the implementation of this extension will mean the development of more complex models that explicitly capture stochastic events.

## APPENDIX A EXAMPLE OF CUSTOMER ORDERS

## Report No. 003 Customer Order Sorted by Sales Order Numbers

| SO. No. | Customer Name | Product Name | Order Oty. | Amount | Promised Date |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 | A\&LSUPPLY |  |  |  |  |
|  |  | ADMIRAL/WS16 | 6.00 | \$324.00 | 01/01/2001 |
|  |  | BIOGANFE/WS20 | 21.00 | \$1,491.00 | 01/01/2001 |
|  |  |  |  | \$1,815.00 |  |
| 20 SEED BIOTICS |  |  |  |  |  |
|  |  | ADMIRALW/WSI6 | 38.00 | \$2,204,00 | 01/01/2001 |
|  |  | AG36/D055 | 3.00 | \$1,041.00 | 01/01/2001 |
|  |  | AG36/GL04 | 72.00 | \$2,808.00 | 01/01/2001 |
|  |  |  |  | \$6,053.00 |  |

21 WILBUR ELLIS
AG145/GL.04
BIOGANFECAW/WS20

| 14.00 | $\$ 588.00$ | $01 / 01 / 2001$ |
| :--- | ---: | :--- |
| 18.00 | $\$ 1,728.00$ | $01 / 01 / 2001$ |
|  | $\$ 2,316.00$ |  |

22 TURF SUPPLY COMPANY
AG145/QT01 96.00

| 96.00 | $\$ 1,728.00$ | $01 / 01 / 2001$ |
| ---: | ---: | ---: |
| 19.00 | $\$ 1,995.00$ | $01 / 01 / 2001$ |
| 10.00 | $\$ 710.00$ | $01 / 01 / 2001$ |
|  | $\$ 4,433.00$ |  |

23 M.D. PRICE
AG36/GL04
75.00
$\$ 2.925 .00$
$01 / 01 / 2001$
\$2,925.00

24 MIDDLE SMITHFIELD MATERIALS
ADMIRAL/D030
ADMIRALW/WS16

| 2.00 | $\$ 766.00$ | $01 / 01 / 2001$ |
| ---: | ---: | ---: |
| 27.00 | $\$ 1,566.00$ | $01 / 01 / 2001$ |
|  | $\$ 2,332.00$ |  |

25 CHEM TECH

| ADMIRAL/D030 | 7.00 | $\$ 2,681.00$ | $01 / 01 / 2001$ |
| :--- | ---: | ---: | ---: |
| AG36/GL04 | 68.00 | $\$ 2,652.00$ | $01 / 01 / 2001$ |
| BIOGAIN/WS40 | 17.00 | $\$ 901.00$ | $01 / 01 / 2001$ |

Printed Date: 10/23/2002

Repor No. 003 Customer Order Sorted by Sales Order Numbers

SO. No. Customer Name Product Name

26 TMX $\operatorname{NDDUSTRIES}$
ADMIRAL/GL04 AG36/GL04

27 SPRAY TECH MANUFACTURNG AG36/G202 AG36/QT12 AVO1090/D030

Order Oty. Amount Promised Date
\$6,234.00

| 44.00 | $\$ 2.420 .00$ | $01 / 01 / 2001$ |
| :--- | :--- | :--- |
| 63.00 | $\$ 2.457 .00$ | $01 / 01 / 2001$ |
|  | $\$ 4,877.00$ |  |


| 48.00 | $\$ 2,976.00$ | $01 / 01 / 2001$ |
| ---: | ---: | ---: |
| 40.00 | $\$ 3.120 .00$ | $01 / 01 / 2001$ |
| 8.00 | $\$ 3,832.00$ | $01 / 01 / 2001$ |
|  | $\$ 9,928.00$ |  |



| 8.00 | $\$ 2.776 .00$ | $01 / 01 / 2001$ |
| ---: | ---: | ---: |
| 6.00 | $\$ 2,874.00$ | $01 / 01 / 2001$ |
| 38.00 | $\$ 2.052 .00$ | $01 / 01 / 2001$ |
|  | $\$ 7,702.00$ |  |


| 44.00 | $\$ 2.376 .00$ |
| ---: | :--- | $01 / 01 / 2001$

31 F\&GREALTY

| ADMIRAL/D030 | 8.00 | $\$ 3,064.00$ | $01 / 01 / 2001$ |
| :--- | ---: | ---: | ---: |
| ADMIRAL/GL04 | 97.00 | $\$ 5,335.00$ | $01 / 01 / 2001$ |
|  |  | $\$ 8,399.00$ |  |

32 WILLIAMSBURG RECYCLING - DO N AG36/QT12
$\begin{array}{rrr}20.00 & \$ 1,560.00 & 01 / 01 / 2001 \\ 8.00 & \$ 640.00 & 01 / 01 / 2001\end{array}$

## Report No. 003 Customer Order Sorted by Sales Order Numbers

SO. No. Customer Name | Product Name |
| :--- | :--- |
| BIOGAINFECA/WS20 |

Order Oty. Amount Promised Date


33 SPS TRANSPORTATION LTD
AG145/GL04

| $21.00 \quad \$ 882.00$ |
| ---: | :--- | $01 / 01 / 2001$

34 ARTISAN LANDSCAPING
BASOLLBLUE25/D005


35 POCONO TURF SUPPLY CO NC
ADMIRAL/D030


36 KIMBALL TREE SERVICE
ADMIRAL/D030
BASOLBLUE25/D005


37 SUPERIOR SERVICES
AG145/QT01
BIOGAINFE/WS20


38 NEW ENGLAND BARK MULCH
AG36/QT01

| $291.00 \quad \$ 2.328 .00$ |
| ---: |

01/02/2001
10.00
\$3,470.00
01/02/2001
$206.00 \quad \$ 1,648.00$
01/02/2001
\$5,118.00

Printed Date: 10/23/2002

# Repor No. 003 Customer Order Sorted by Sales Order Numbers 

| SO. No. Customer Name | Product Name |
| ---: | :--- |
| 40 HOLLISTON SAND COMPANY |  |
|  | AG145/QT12 |
|  | BIOGAINFECA/WS20 |

Order Oty. Amount Promised Date


41 BJORNSON OIL COMPANY
BIOGAINFE/WS20


42 ARBORCHEM PRODUCTS CO
AG36/D055
AVO1090/D030
BASOLLBLUE25/D005


43 IOWA STATE UNIVERSITY ATHLETI
ADMIRAL/WS16
AG36/G202
$31.00 \quad \$ 1,674.00 \quad 01 / 02 / 2001$
BASOILBLUE25/D005
$37.00 \quad \$ 2.294 .00 \quad 01 / 02 / 2001$
$3.00 \quad \$ 2,649.00 \quad 01 / 02 / 2001$
\$6,617.00

44 MINNESOTA DISTRIBUTING
AG145/QT01
AG36/G202
BIOGAIN/WS40


45 BEST SAND CORPORATION
AG36/GL04
BASOILBLUE25/D005

| 34.00 | $\$ 1,326.00$ | $01 / 02 / 2001$ |
| ---: | ---: | ---: |
| 5.00 | $\$ 4,415.00$ | $01 / 02 / 2001$ |
|  | $\$ 5,741.00$ |  |

46 BOSS SUPPLY INC
$\begin{array}{llll}\text { AG145/D055 } & 9.00 & \$ 3,123.00 & 01 / 02 / 2001\end{array}$

Printed Date: 10/23/2002

# Report No. 003 Customer Order Sorted by Sales Order Numbers 

SO. No. Customer Name Product Nam
47 ZUMBRO VALLEY FORESTRY
AG36/D055
BIOGAINCA
48 VIRGINIA GROUND COVERS
AG36/GL04

Order Otv. Amount Promised Date

\$3,123.00

47 ZUMBRO VALLEY FORESTRY
AG36/D055
BIOGAINCA/WS40

| 5.00 | $\$ 1,735.00$ | $01 / 02 / 2001$ |
| ---: | ---: | ---: |
| 50.00 | $\$ 2.700 .00$ | $01 / 02 / 2001$ |
|  | $\$ 4,435.00$ |  |



49 BROOKVILLE WOOD PRODUCTS AG145/G202


50 CTC LLC
AG36/G202
AG36/GL06
BIOGAINCA/WS40

| 16.00 | $\$ 992.00$ | $01 / 02 / 2001$ |
| :--- | ---: | ---: |
| 19.00 | $\$ 1,140.00$ | $01 / 02 / 2001$ |
| 54.00 | $\$ 2.916 .00$ | $01 / 02 / 2001$ |
|  | $\$ 5,048.00$ |  |

51 E.H. GRIFFITH NC
ADMIRAL/D030
AG145/GL04 BASOILBLUE/GL04

| 3.00 | $\$ 1,149.00$ | $01 / 02 / 2001$ |
| ---: | ---: | ---: |
| 51.00 | $\$ 2,142.00$ | $01 / 02 / 2001$ |
| 12.00 | $\$ 1,188.00$ | $01 / 02 / 2001$ |
|  | $\$ 4,479.00$ |  |

52 AMERICAN CLAY WORKS AND SU
AG145/D055

| 3.00 | $\$ 1.041 .00$ | $01 / 03 / 2001$ |
| :--- | :--- | :--- |
| 3.00 | $\$ 1,437.00$ | $01 / 03 / 2001$ |
|  | $\$ 2,478.00$ |  |

53 FORSHAW DISTR. INC

Printed Date: 10/23/2002

## Report No. 003 Customer Order Sorted by Sales Order Numbers

| SO. No. Customer Name | Product Name |
| :--- | :--- |
|  | ADMIRAL/WS16  <br>  BIOGAIN/JR12 <br>  BIOGAINFECAW/WS20$\ggg$ |


| Order Oty. | Amount | Promised Date |
| :---: | :---: | :---: |
| 7.00 | \$378.00 | 01/03/2001 |
| 16.00 | \$1.680.00 | 01/03/2001 |
| 23.00 | \$2,208.00 | 01/03/2001 |
|  | \$4,266.00 |  |


| 49.00 | $\$ 2.646 .00$ | $01 / 03 / 2001$ |
| ---: | ---: | ---: |
| 40.00 | $\$ 720.00$ | $01 / 03 / 2001$ |
|  | $\$ 3,366.00$ |  |

55 WETSEL INC

## ADMIRAL/GL04 AG145/GL04 AG36/D055

| 48.00 | $\$ 2,640.00$ | $01 / 03 / 2001$ |
| ---: | ---: | ---: |
| 35.00 | $\$ 1.470 .00$ | $01 / 03 / 2001$ |
| 8.00 | $\$ 2,776.00$ | $01 / 03 / 2001$ |
|  | $\$ 6,886.00$ |  |

56 EXTERIOR DESIGNS
ADMIRAL/D030
AVO1090/D030
BASOLLBLUE25/D005

57 SAN JOAQUIN HELICOPTERS
ADMIRAL/D030
AG36/G202
BIOGAIN/JR12

$\begin{array}{r}7.00 \quad \$ 2.681 .00 \\ \hline\end{array}$
01/03/2001
1.00 $\$ 3,243.00$

01/03/2001

Printed Date: 10/23/2002

Repor No. 003 Customer Order Sorted by Sales Order Numbers

| SO. No. | Customer Name | Product Name | Order 0ty. | Amount | Promised Date |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 60 TERRE CO THE |  |  |  |  |  |
|  |  | BASOILBLUE25/D005 | 4.00 | \$3,532.00 | 01/04/2001 |
|  |  | BIOGAINFECA/WS20 | 33.00 | \$2,310.00 | 01/04/2001 |
|  |  |  |  | \$5,842.00 |  |

61 MIDLAND IRON \& STEEL
ADMIRAL/GL04


62 SAN JOAQUIN HELICOPTERS
AVO1090/D030
BIOGAINFECA/WS20

| 5.00 | $\$ 2,395.00$ | $01 / 04 / 2001$ |
| ---: | ---: | ---: |
| 18.00 | $\$ 1,260.00$ | $01 / 04 / 2001$ |
|  | $\$ 3,655.00$ |  |

63 ENVIRONMENTAL SIGHT DEVELOP AB9/D030
AG36/QT12
BASOILRED/PT12


64 TARGET SPECIALTY PRODUCTS
AG145/GL04
AG145/GL06
BIOGAN/JR12

| 52.00 | $\$ 2,184.00$ | $01 / 04 / 2001$ |
| ---: | ---: | ---: |
| 8.00 | $\$ 496.00$ | $01 / 04 / 2001$ |
| 23.00 | $\$ 2,415.00$ | $01 / 04 / 2001$ |
|  | $\$ 5,095.00$ |  |

65 TWOMBLY NURSERY NC.
ADMIRAL/WSI6
AG145/GL04
AVO1090/D030

| 39.00 | $\$ 2.106 .00$ | $01 / 04 / 2001$ |
| ---: | ---: | ---: |
| 41.00 | $\$ 1,722.00$ | $01 / 04 / 2001$ |
| 5.00 | $\$ 2,395.00$ | $01 / 04 / 2001$ |
|  | $\$ 6,223.00$ |  |

66 HELDERBURG MOUNTAIN MULCH C

| AG145/D055 | 8.00 | $\$ 2,776.00$ | $01 / 04 / 2001$ |
| :--- | ---: | ---: | ---: |
| AG36/G202 | 28.00 | $\$ 1,736.00$ | $01 / 04 / 2001$ |
| BIOGAINFECAW/WS20 | 24.00 | $\$ 2,304.00$ | $01 / 04 / 2001$ |

Printed Date: 10/23/2002

# Report no. 003 Customer Order Sorted by Sales Order Numbers 

SO. No. Custome
67 SOUTHE
68 CAMCO
ADMIRAL/D030
AG145/G202
BASOILBLUE25/D005

| 2.00 | $\$ 766.00$ | $01 / 04 / 2001$ |
| ---: | ---: | ---: |
| 43.00 | $\$ 2,666.00$ | $01 / 04 / 2001$ |
| 4.00 | $\$ 3.532 .00$ | $01 / 04 / 2001$ |
|  | $\$ 6,964.00$ |  |

69 RYAN OIL COMPANY INC

| AG145/G202 | 46.00 | $\$ 2,852.00$ | $01 / 04 / 2001$ |
| :--- | ---: | ---: | ---: |
| AG36/G202 | 31.00 | $\$ 1.922 .00$ | $01 / 04 / 2001$ |
| AG36/QT01 | 84.00 | $\$ 672.00$ | $01 / 04 / 2001$ |
|  |  | $\$ 5,446.00$ |  |

70 FULLER PETROLEUM COMPANY

| 27.00 | $\$ 2.106 .00$ |
| ---: | :--- |
| $\$ 2,106.00$ |  | $01 / 04 / 2001$

71 Bueshing Peat Moss
BIOGAIN/JRI2

| 22.00$\$ 2.310 .00$ $01 / 05 / 2001$ |
| :---: |

72 NATIONAL LIQUID FERTILIZER
AB9/D030
BASOILBLUE/GL04
BIOGAINFE/WS20

| 2.00 | $\$ 1.472 .00$ | $01 / 05 / 2001$ |
| ---: | ---: | ---: |
| 17.00 | $\$ 1.683 .00$ | $01 / 05 / 2001$ |
| 13.00 | $\$ 923.00$ | $01 / 05 / 2001$ |
|  | $\$ 4,078.00$ |  |

73 ADVANCED BIOLOGICAL SOLUTI
BIOGAINFE/WS20
37.00
\$2,627.00
$01 / 05 / 2001$

Printed Date: 10/23/2002

# Report No. 003 Customer Order Sorted by Sales Order Numbers 

SO. No. Customer Name Product Name

74 CAMCO $\quad$|  |  |
| :--- | :--- |
|  | AG36/G202 |
|  | AG36/GL04 |
|  | BIOGAINFE/WS20 |

Order Oty. Amount Promised Date
\$2,627.00

| 31.00 | $\$ 1,922.00$ | $01 / 05 / 2001$ |
| :--- | :--- | :--- |
| 46.00 | $\$ 1.794 .00$ | $01 / 05 / 2001$ |
| 30.00 | $\$ 2.130 .00$ | $01 / 05 / 2001$ |
|  | $\$ 5,846.00$ |  |


| 14.00 | $\$ 868.00$ | $01 / 05 / 2001$ |
| ---: | ---: | ---: |
| 37.00 | $\$ 2,627.00$ | $01 / 05 / 2001$ |
|  | $\$ 3,495.00$ |  |


| 40.00 | $\$ 3,840.00$ |
| ---: | :--- |
|  | $\mathbf{\$ 3 , 8 4 0 . 0 0}$ |

77 PRECISION TURF AND CHEMICAL AG145/QT12 AVO1090/D030
BASOILBLUE25/D005

| 19.00 | $\$ 1.596 .00$ | $01 / 05 / 2001$ |
| ---: | ---: | ---: |
| 3.00 | $\$ 1.437 .00$ | $01 / 05 / 2001$ |
| 2.00 | $\$ 1.766 .00$ | $01 / 05 / 2001$ |
|  | $\$ 4,799.00$ |  |


| 59.00 | $\$ 2.301 .00$ |
| ---: | :--- | $01 / 05 / 2001$

80 HUNGERFORD BROS
BIOGAINFECAW/WS20
24.00
$\$ 2.304 .00$
01/05/2001
$\$ 2,304.00$

81 FECON INC.
AVO1090/D030

| 9.00$\$ 4,311.00$ <br> $\$ 4,311.00$ |
| :--- |

Printed Date: 10/23/2002

## APPENDIX B EXAMPLE RESULTS OF SUPPLY CHAIN NETWORK

## Supply Chain Network using the Shortest Distance Method



Supply Chain Network using the Lowest Transportation Cost Method


Supply Chain Network using the Single Warehouse Preference Method


Supply Chain Network using PSCMP Heuristic Method


## APPENDIX C <br> EXAMPLE RESULTS OF A PULL-BASED SUPPLY CHAIN DECISIONS FROM THIS STUDY

| Customer Name ProductName | SO.No | Order Qty | Amount | Promised Date | Shipping Warchouse S | Shipping Qty |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A\& L SUPPLY |  |  |  |  |  |  |
| BIOGAINFE/WS20 | 19 | 21 | \$1,491.00 | 1/1/2001 | INLAND EMPIRE | 21 |
| ADMIRAL/WS16 | 19 | 6 | \$324.00 | 1/1/2001 | INLAND EMPIRE | 6 |
| ADVANCED BIOLOGICAL SOLUTIONS |  |  |  |  |  |  |
| BIOGAINFE/WS20 | 73 | 37 | \$2,627.00 | 1/5/2001 | BECKER UNDERWOOD | 37 |
| AMERICAN CLAY WORKS AND SUPPLY CO |  |  |  |  |  |  |
| AVO1090/D030 | 52 | 3 | \$1,437.00 | 1/3/2001 | BECKER UNDERWOOD | 3 |
| AG145/D055 | 52 | 3 | \$1,041.00 | 1/3/2001 | BECKER UNDERWOOD | 3 |
| ARBORCHEM PRODUCTS CO |  |  |  |  |  |  |
| AVO1090/D030 | 42 | 9 | \$4,311.00 | 1/2/2001 | JACOBSON WAREHOUSE CO | 9 |
| AG36/D055 | 42 | 5 | \$1,735.00 | 1/2/2001 | JACOBSON WAREHOUSE CO | 5 |
| BASOILBLUE25/D005 | 42 | 5 | \$4,415.00 | 1/2/2001 | JACOBSON WAREHOUSE CO | - 5 |
| ARTISAN LANDSCAPING |  |  |  |  |  |  |
| BASOILBLUE25/D005 | 34 | 4 | \$3,532.00 | 1/1/2001 | GRANTEC | 4 |
| Bellmawr Ecological Center |  |  |  |  |  |  |
| ADMIRAL/T275 | 59 | 1 | \$3,243.00 | 1/3/2001 | JACOBSON WAREHOUSE CO | 1 |
| BEST SAND CORPORATION |  |  |  |  |  |  |
| AG36/GL04 | 45 | 34 | \$1,326.00 | 1/2/2001 | GRANTEC | 34 |

Shipping Information Sorted by Promised Date


| Report No .007 |  | Shipping Information Sorted by Sales Order Numbers |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| So.No. | Customer Name | Product Name Or | Order Qty. | Amount | Promised Date | Shipping Warehouse Shi | Shipping Qty. |
| 19 | A \& L SUPPLY |  |  |  |  |  |  |
|  |  | BIOGAINFE/WS20 | 21 | \$1,491.00 | 1/1/2001 | INLAND EMPIRE | 21 |
|  |  | ADMIRAL/WS16 | 6 | \$324.00 | 1/1/2001 | INLAND EMPIRE | 6 |
| 20 | SEED BIOTICS |  |  |  |  |  |  |
|  |  | AG36/GL04 | 72 | \$2,808.00 | $1 / 1 / 2001$ $1 / 1 / 2001$ | INLAND EMPIRE INLAND EMPIRE | 72 3 |
|  |  | ADMIRAL/W/WS 16 | 38 | \$2,204.00 | 1/1/2001 | INLAND EMPIRE | 38 |
| 21 | WILBUR ELLIS |  |  |  |  |  |  |
|  |  | AG145/GL04 | - 14 |  | 1/1/2001 |  |  |
|  |  | BIOGAINFECAW/WS20 | $0 \quad 18$ | $\$ 1,728.00$ | 1/1/2001 | STERLING QUALITY LOGISTICS | $18$ |
| 22 | TURF SUPPLY C | PANY |  |  |  |  |  |
|  |  | BIOGAINFE/WS20 | 10 | \$710.00 | 1/1/2001 | GRANTEC | 10 |
|  |  | AG145/QT01 | 96 | \$1,728.00 | 1/1/2001 | GRANTEC | 96 |
|  |  | BIOGAIN/JR12 | 19 | \$1,995.00 | 1/1/2001 | GRANTEC | 19 |
| 23 | M.D. PRICE |  |  |  |  |  |  |
|  |  | AG36/GL04 | 75 | \$2,925.00 | 1/1/2001 | GRANTEC | 75 |

[^0]


Inventory Replenishment Sorted by Warehouse Names

| Warehouse Name | Product Name | Replenishment Qty | From Plant Name |
| :--- | :--- | :--- | :--- | :--- |
| INLAND EMPIRE |  |  |  |
|  | AGG6/D055 |  |  |

## Inventory Replenishment Sorted by Product Names



| Report No. 012 | Inventory Replenishment Sorted by Plant Names |  |
| :--- | :--- | :--- |
| From Plant Name | To Warehouse Name | Product Name |
| Becker Underwood | JACOBSON WAREHOUSE CO. (PA) |  |
| Inland Empire | ANLAND EMPIRE |  |
|  |  |  |
| STERLING QUALITY LOGISTICS | AG36/D055 |  |

## Report No. 013 Production Plan Summary Report

| Product Name | Becker Underwood | Inland Empire | Total |
| :---: | ---: | ---: | ---: | ---: |
| ADMIRAL/D030 | $\mathbf{4 0 . 0 0}$ | 0.00 | $\mathbf{4 0 . 0 0}$ |
| AG36/D055 | 0.00 | 83.00 | $\mathbf{8 3 . 0 0}$ |

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# Repor No. 014 Production Plan Sorted by Plant Names 

| PlantName | ProductName | NumberofUnits |
| :---: | :---: | :---: |
| Becker Underwood |  |  |
|  | ADMIRAL/D030 | 40.00 |
| Inland Empire |  |  |
|  | AG36/D055 | 51.00 |
|  | AG36/D055 | 32.00 |

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